## Aptitude Shortcuts

Friends, here I am sharing some shortcut methods which I came across these days. I hope these may helpful for you.

1. Multiplying 2 digit numbers which are starting with the same digit and the sum of the last 2 digits gives sum as 10 .

Eg1. 52x58
(Here the numbers start with same digit as well as the sum of last digits $2+8=10$ )
Method :
Step 1-Here both the numbers 52 and 58 starts with 5 .So take the very next digit of 5 i.e $(5+1)=6$.

Step 2-Multiply $5 \times 6.5 \times 6=30$.This 30 is the left part of our answer.
Step 3-Multiply the other 2 digits.i.e $2 \times 8=16$, which is the right part of our answer.
So answer is 3016 .
In short
$52 \times 58 \rightarrow 5 \times(5+1)$ and $2 \times 8=30$ and $16=3016$.

## Eg2.63x67

Step 1-Here both the numbers 63 and 67 starts with 6 .So take the very next digit of 6 i.e $(6+1)=7$.

Step 2-Multiply $6 \times 7.6 \times 7=42$. This 42 is the left part of our answer.
Step 3-Multiply the other 2 digits.i.e $3 \times 7=21$, which is the right part of our answer.
Answer is 4221 .
Eg3. $72 \times 76$

Here both the numbers start with 7, but the second condition to use the above method,i.e $2+6=8$, not equal to 10 . So we cannot use this method.
2. Shortcut technique to find the Sum of powers of 2.

We know that,
$2^{0}=1$
$2^{1}=2$
$2^{2}=4$
$2^{3}=8$
$2^{4}=16 \ldots \ldots$.etc

Now we want to find
Eg1. $2^{0}+2^{1}$
Method : $2^{0}+2^{1}=1+2=3$ and it is same as $2^{2}$-1, i.e $2^{2}-1=4-1=3$.
Eg2. $2^{0}+2^{1}+2^{2}$
Method : $2^{0}+2^{1}+2^{2}=1+2+4=7$ and it is same as $2^{3}-1$, i.e $8-1=7$
Eg3. $2^{0}+2^{1}+2^{2}+2^{3}$
Method : $2^{0}+2^{1}+2^{2}+2^{3}=1+2+4+8=15$ and it is same as $2^{4}-1$ i.e $16-1=15$.
In short $2^{0}+2^{1}+2^{2}+2^{3}+2^{4}+\ldots \ldots \ldots \ldots+2^{n}=2^{n+1}-1$.
3.Sum of first $\mathbf{n}$ odd numbers.

We know that the squares
$1^{2}=1$
$2^{2}=4$
$3^{2}=9$
$4^{2}=16$
$5^{2}=25 \ldots$.etc
But we can write $1^{2}=1$
$2^{2}=1+3=4$
$3^{2}=1+3+5=9$
$4^{2}=1+3+5+7=16$
$5^{2}=1+3+5+7+9=25$
That means square of a number n is equal to the sum of first n odd numbers.
Eg. 1 Find the sum of first 5 odd numbers.
Method/Ans: Here first 5 odd numbers means 1,3,5,7,9.From the above method, it is clear that $5^{2}$ is equal to sum of the first 5 odd numbers. So answer is $5^{2}$,i.e 25.

Eg2. Find the sum of first 10 odd numbers.
Method/Ans : Sum of first 10 odd numbers means take $10^{2}$,i.e 100 .
In general,for finding the sum of first $n$ odd numbers, take the square of $n, i, e n^{2}$.

