# 2005 JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY 

IV B.TECH. II SEMESTER SUPPLEMENTARY EXAMINATIONS<br>BOUNDARY LAYER THEORY<br>(AERONAUTICAL ENGINEERING)

## Answer any FIVE Questions All Questions carry equal marks

1. Simplify the equation of continuity in cylindrical coordinates $(r, \mu z)$ to the case of steady compressible ${ }^{\circ}$ ow in polar coordinates $(@=@ z=0)$ and derive a stream function for this case.
2. Derive the Navier-stokes equations.
3. Explain the ${ }^{\circ}$ ow at a rotating disc.
4. Derive the two-dimensional Poisson relation for pressure, analogous Poisson, assuming unsteady incompressible ${ }^{\circ}$ ow.
5. Investigate the use of the Crank-Nicolson (1947) method for computer analysis of a laminar boundary layer, as implemented, e.g., by Blottner (1970). What are its numerical advantages and disadvantages?
6. For the separating Falkner-Skan wedge- ${ }^{\circ}$ ow boundary layer, ${ }^{-}=-0.19884$, use any appropriate correlation to estimate the position Rex where transition ${ }^{-r s t}$ occurs?
Assume free stream turbulence level of 1 percent.
7. By direct substitution of the ${ }^{\circ}$ uctuation de ${ }^{-}$nitions and use of the averaging rules, develop the three-dimensional time-averaged $x$-momentum equation and show what reductions occur in a steady two-dimensional turbulent boundary layer.
8. As part of a low-temperature thermal-power design, a long 5-m diameter vertical circular cylinder is placed in the ocean. The current across the cylinder is $60 \mathrm{~cm} / \mathrm{s}$. At a point 1 km downstream of the cylinder, estimate
(a) the wake width (in $m$ ) and
(b) the maximum velocity $\operatorname{defect}$ (in $\mathrm{cm} / \mathrm{s}$ ).
