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## 2005 JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY

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IV B.TECH I SEMESTER SUPPLEMENTARY EXAMINATIONS DIGITAL SIGNAL PROCESSING (ELECTRICAL & ELECTRONIC ENGINEERING AND INFORMATION TECHNOLOGY) NOVEMBER 2005 TIME: 3 HOURS MAX MARKS: 80 **Answer any FIVE Questions** All Questions carry equal marks ????? 1. (a) Consider a LSI system with unit sample response h(n)n = nu(n) where is real and 0 < < 1. If the input is x(n) = n u(n), 0 < || < 1, determine the output f(n) in the form y(n) = (kT n + k2 nu(n)) by explicitly evaluating the convolution sum. (b) Define causality and stability of LSI system and state the conditions for stability. [12+4]2. (a) If x(n) ! x(ej!) Constitute a Fourier transform pair. Prove the following: Sequence Fourier Transform i. x\*(n) X (e-j! ii. xo(n) jIm[X(ej!] (b) Let x(n) and X(ej!) represent a sequence and its transform. Determine, in terms of X(ei!), the transform of each of the following sequences : i. g(n) =x(n/2) n even 0 n odd ii.  $x_2(n)$ [8+8] 3. (a) Prove the following properties i. arg[X(K)] = -arg[X((-K)N)RN(K)]ii. Im[X(K)] = -Im[X((-K))NRN(K)](b) If X(K) denotes the N-point DFT of N-Point sequence x(n), show that with N even and if x(n) = x(N-1-n) then X(N/2)=0. [8+8]

4. (a) Explain the inverse FFT algorithm to compute inverse DFT of a N=8. Draw the flow graph for the same.

[8+8]

5. (a) An LTI system is described by the equation y(n)=x(n)+0.81x(n-1)-0.81x(n-2)-0.45y(n-2). Determine the transfer function of the system. Sketch the poles and zeroes on the Z-plane.

(b) Define stable and unstable system test the condition for stability of the first order IIR filter governed by the equation y(n)=x(n)+bx(n-1).

6. Design a Digital IIR low pass filter with pass band edge at 1000 Hz and stop band edge at 1500 Hz for a sampling frequency of 5000 Hz. The filter is to have a pass

band ripple of 0.5 db and stop band ripple below 30 db. Design Butter worth filler using both impulse invariant and Bilinear transformations.

7. A low pass filter is to be designed with the following desired frequency response. Hd(ej!) = e-j2!, - /4 ! /40, /4 |!| Determine the filter coefficients hd(n) if the window function is defined as !(n) = 1, 0 n 40, otherwise Also determine the frequency response H(ej!) of

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