Marking Scheme Class X Session 2024-25 MATHEMATICS STANDARD (Code No.041)

TIME: 3 hours

MAX.MARKS: 80

| Q.No. | Section A | | | | | |
|-------|---|---|--|--|--|--|
| 1. | D) -6,6 | 1 | | | | |
| 2. | B) -5 | 1 | | | | |
| 3. | D) From a point inside a circle only two tangents can be drawn. | 1 | | | | |
| 4. | A) 7 | 1 | | | | |
| 5. | B) 20 cm | 1 | | | | |
| 6. | A) ¹¹ / ₉ | 1 | | | | |
| 7. | C) 140 ⁰ | 1 | | | | |
| 8. | B) 8 <i>x</i> ² - 20 | 1 | | | | |
| 9. | C) 30 | 1 | | | | |
| 10. | B) isosceles and similar | 1 | | | | |
| 11. | A) Irrational and distinct | 1 | | | | |
| 12. | C) $\frac{3}{\sqrt{3}}$ | 1 | | | | |
| 13. | B) $\frac{594}{7}$ | 1 | | | | |
| 14. | B) $\frac{3}{8}$ | 1 | | | | |
| 15. | B) (-4, 0) | 1 | | | | |
| 16. | A) median | 1 | | | | |
| 17. | C) (3,0) | 1 | | | | |
| 18. | D) $\frac{3}{26}$ | 1 | | | | |
| 19. | В) | 1 | | | | |
| 20. | D) | 1 | | | | |

| | Section B | | | | | | |
|---------|---|------------|--|--|--|--|--|
| 21. (A) | $480 = 2^{5} \times 3 \times 5$ 720 = 2 ⁴ × 3 ² × 5 | 1/2 1/2 | | | | | |
| | LCM (480,720) = $2^5 \times 3^2 \times 5 = 1440$ | 1⁄2 | | | | | |
| | HCF (480, 720) = $2^4 \times 3 \times 5 = 240$ | | | | | | |
| | OR | | | | | | |
| (B) | 85 = 5x17, 238 = 2x7x17 HCF(85, 238) = 17 | 1 | | | | | |
| | 17 = 85xm -238 m = 3 | 1 | | | | | |
| 22.(A) | Total number of possible outcomes = 6x6=36 For a product to be odd, both the numbers should be odd. Favourable outcomes are (7,7) (7,9) (7,11) (9,7) (9,9) (9, 11) (11,7) (11,9) (11,11) no. of favourable outcomes = 9 | 1/2 | | | | | |
| | P (product is odd) = $\frac{9}{36}$ Or $\frac{1}{4}$ | 1 ½ | | | | | |
| | OR | | | | | | |
| (B) | Total number of three-digit numbers = 900. Numbers with hundredth digit 8 & and unit's digit 5 are 805,815, | 1/2 | | | | | |
| | 825,,895 Number of favourable outcomes = 10 P(selecting one such number) = $\frac{10}{900}$ Or $\frac{1}{90}$ | | | | | | |
| 23. | $2 \left(\frac{\sqrt{3}}{2}\right)^2 - \left(\frac{1}{\sqrt{2}}\right)^2$ | 1 ½ | | | | | |
| | $\frac{2 \left(\frac{\sqrt{3}}{2}\right)^2 - \left(\frac{1}{\sqrt{3}}\right)^2}{\left(\sqrt{2}\right)^2} = \frac{7}{12}$ | 1⁄2 | | | | | |
| 24 | Let the required point be (x,0) | 1⁄2 | | | | | |
| | $\sqrt{(8-x)^2 + 25} = \sqrt{41}$ => $(8-x)^2 = 16$ => $8 - x = \pm 4$ | 1⁄2 | | | | | |
| | => x = 4 , 12 Two points on the x-axis are (4,0) & (12,0). | 1 | | | | | |



| | $\triangle AQR \sim \triangle ACD$ | |
|--------|--|-----|
| | AQ RQ | |
| | $=>\frac{AQ}{AC}=\frac{RQ}{DC}\qquad \dots \dots \qquad (ii)$ | |
| | | 1 |
| | Now, $\frac{AP}{AB} = \frac{AQ}{AC}$ (iii) | |
| | AB AC PP PO | |
| | Using (i), (ii) & (iii), $\frac{PR}{BD} = \frac{RQ}{DC}$ | 1 |
| | But, $BD = DC$ | |
| | => PR = RQ or AD bisects PQ | |
| 27. | Let the numbers be x and 18-x. | 1/2 |
| | | 1 |
| | $\frac{1}{x} + \frac{1}{18 - x} = \frac{9}{40}$ | |
| | $= 18 \times 40 = 9 \times (18 - x)$ | |
| | $= x^2 - 18 x + 80 = 0$ | |
| | => (x-10)(x-8) = 0 | 1 |
| | => <i>x</i> =10, 8. | |
| | => 18- <i>x</i> =8, 10 | 1/2 |
| | Hence two numbers are 8 and 10. | |
| 28. | From given polynomial $\alpha + \beta = \frac{5}{2} - \alpha \beta = \frac{1}{2}$ | 1 |
| | From given polynomial $\alpha + \beta = \frac{5}{6}$, $\alpha\beta = \frac{1}{6}$ | |
| | $\alpha^2 + \beta^2 = (\frac{5}{6})^2 - 2 \times \frac{1}{6} = \frac{13}{36}$ | 1 |
| | 6 36 6 36 | |
| | 1 1 | 1/2 |
| | And $\alpha^2 \beta^2 = (\frac{1}{6})^2 = \frac{1}{36}$ | |
| | 6 36 | |
| | 2 13 1 | |
| | $x^2 - \frac{13}{36}x + \frac{1}{36}$ | 1/2 |
| | \Rightarrow Required polynomial is $36x^2 - 13x + 1$ | |
| | | |
| 29. | $(\cos\theta + \sin\theta)^{2} + (\cos\theta - \sin\theta)^{2} = 2(\cos^{2}\theta + \sin^{2}\theta) = 2$ | |
| _ | $(\cos \theta + \sin \theta)^{2} + (\cos \theta - \sin \theta)^{2} = 2$ | 1 ½ |
| | $=>(\cos\theta - \sin\theta)^2 = 1$ | 1 |
| | $\Rightarrow \cos\theta - \sin\theta = \pm 1$ | 1/2 |
| 30.(A) | Angle described by minute hand in 5 min = 30° . | |
| . , | length of minute hand $=18$ cm $=$ r. | |
| | Area swept by minute hand in 35 minutes | _ |
| | $=(\frac{22}{7} \times 18 \times 18 \times \frac{30}{360}) \times 7$ | 2 |
| | $= 594 \ cm^2$. | 1 |
| | OR | |
| | Area of minor commont - Ar Sector OAB Ar 4 OAB | |
| (B) | Area of minor segment = Ar. Sector OAB- Ar. \triangle OAB | 2 |
| | $=\frac{60}{360} \times \frac{22}{7} \times 14 \times 14 - \frac{\sqrt{3}}{4} \times 14 \times 14$ | 2 |
| | $= 17.89 \mathrm{cm}^2$ | |

| 31. | Let $\sqrt{3}$ be a rational number. | 1/2 | | | | | |
|--------|---|--------------------------|--|--|--|--|--|
| | ∴ $\sqrt{3} = \frac{p}{a}$, where q≠0 and let p & q be co-prime. | /2 | | | | | |
| | $3q^2 = p^2 \implies p^2$ is divisible by $3 \implies p$ is divisible by $3 (i)$ $\implies p = 3a$, where 'a' is some integer | | | | | | |
| | \Rightarrow p = 3a, where a is some integer $9a^2 = 3q^2 \Rightarrow q^2 = 3a^2 \Rightarrow q^2$ is divisible by 3 \Rightarrow q is divisible by 3 (ii) (i) and (ii) leads to contradiction as 'n' and 'd' are as prime | | | | | | |
| | (i) and (ii) leads to contradiction as 'p' and 'q' are co-prime. | | | | | | |
| | Section D | | | | | | |
| 32.(A) | x+2y=3, 2x-3y+8=0 Correct graph of each equation Solution x=-1 and y=2 | 2+2 = 4 1 | | | | | |
| | OR | | | | | | |
| (B) | Let car I starts from A with speed x km/hr and car II Starts from B with speed y km/hr (x>y) | | | | | | |
| | Case I- when cars are moving in the same direction. Distance covered by car I in 9 hours = 9x. Distance covered by car II in 9 hours = 9y Therefore 9 (x-y) = 180 => x-y= 20(i) | 2 | | | | | |
| | case II- when cars are moving in opposite directions. | | | | | | |
| | Distance covered by Car I in 1 hour = x Distance covered by Car II in 1 hour = y | | | | | | |
| | Therefore x + y=180 (ii) | 2 | | | | | |
| | Solving (i) and (ii) we get, x=100 km/hr, y=80 km/hr. | 1 | | | | | |
| 33. | Correct given, to prove, construction, figure | 1 | | | | | |
| | Correct proof | 2 | | | | | |
| | AR = AQ = 7cm BP = BR = AB-AR = 3cm CP = CQ = 5cm BC = BP+PC = 3+5 = 8 cm | 1/2 1/2 1/2 1/2 | | | | | |
| | | | | | | | |

| 34. | A | 60° 30° X G | h | C h F 1.35 E | 5 m | | | Correct figure 1mark |
|-----|---|-------------------|-------|--------------------------|---------------------------|-----------|-----|----------------------------|
| | Let A be the eye level & B, C are positions of balloon Distance covered by balloon in 12 sec = $3x12 = 36$ m BC = GF = 36 m | | | | | | | 1 |
| | tan $60^{0} = \sqrt{3} = \frac{h}{x}$ => h = x $\sqrt{3}$ (i) | | | | | | | 1 |
| | $\tan 30^0 = \frac{1}{\sqrt{3}} = \frac{h}{x+36}$ | | | | | | | 1 |
| | => h = $\frac{x+36}{\sqrt{3}}$ (ii) Solving (i) and (ii) h= $18\sqrt{3}$ = 31.14 m Height of balloon from ground = 1.35 + 31.14 = 32.49 m | | | | | | 1 | |
| 35. | | | | | | | | Correct |
| | | Class | x | f | $u = \frac{x - 102.5}{5}$ | fu | cf | table 2marks |
| | | 85-90 | 87.5 | 15 | -3 | -45 | 15 | |
| | | 90-95 | 92.5 | 22 | -2 | -44 | 37 | |
| | | 95-100 | 97.5 | 20 | -1 | -20 | 57 | |
| | | 100-105 | 102.5 | 18 | 0 | 0 | 75 | |
| | | 105-110 | 107.5 | 20 | 1 | 20 | 95 | |
| | | 110-115 | 112.5 | 25 | 2 | 50 | 120 | |
| | | | | <i>Σ</i> f = 120 | | Σfu = -39 | | |
| | Mean = \overline{x} = 102.5 - 5 x $\frac{39}{120}$ = 100.875 Median class is 100-105 Median = 100 + $\frac{5}{18}$ (60-57) = 100.83 | | | | | | | 1 ½ ½ 1 |
| | | | | | OR | | | |

| | Monthly Expenditure | £ | | f | | Corroct |
|-----------|---|-------------------------------------|----------------|-------------------------------|-----------|---------------|
| | Monuny Experiature | fi | Xi | f _i x _i | | Correct table |
| | 1000-1500 | 24 | 1250 | 30,000 | | 2marks |
| | 1500-2000 | 40 | 1750 | 70,000 | | |
| | 2000-2500 | 33 | 2250 | 74,250 | | |
| | 2500-3000 | X=28 | 2750 | 77,000 | | |
| | 3000-3500 | 30 | 3250 | 97,500 | | |
| | 3500-4000 4000-4500 | 22 16 | 3750 4250 | 82,500 | | |
| | 4500-5000 | 7 | 4750 | 68,000 33,250 | | |
| | 1500 5000 | , | 1750 | 33,230 | | |
| | 172+x=200 | | | | | 1 |
| | X=28 | | | | | 1 |
| | Mean= $\frac{532500}{200}$ | | | | | |
| | = 2662.5 | | | | | 1 |
| | | | | | | |
| | | | Sectior | E | | |
| 36.(i) | First term a = 3, A. | | | | | 1/2 |
| | | common | difference d | = 6-3 = 3 | | 1/2 |
| (ii) | 34 = 3+ (n-1)3 | | | | | |
| () | => n = 34/3 = 11 | l ¹ / ₋ which | is not a posit | ive integer. | | 1/2 |
| | | 3 | | | attern is | 17 |
| | Therefore, it is not possible to have 34 jars in a layer if the given pattern is continued. | | | | | 1/2 |
| (iii)(A) | $S_n = \frac{n}{2} [2x3 + (n-1)3]$ | | | | | |
| | $S_n = \frac{n}{2} [2x3 + (n-1)3]$ $= \frac{n}{2} [6 + 3n-3]$ | ני | | | | 1 |
| | | | | | | 1 |
| | $=\frac{n}{2}[3+3n]$ | | | | | |
| | $= 3\frac{n}{2}[1+n]$ | | | | | |
| | $s_8 = 3 x \frac{8}{2} (1+8)$ | | | | | 1/2 |
| | = 108 | | | | | |
| | | | OR | | | |
| | A.P will be 6, 9, 12, | | | | | 17 |
| (iii) (B) | a= 6, d=3 | | | | | 1/2 |
| | $t = 6 \pm (5.1)^2$ | | | | | |
| | $t_5 = 6 + (5-1)3$ = 6 + 12 | | | | | 1 |
| | = 18 | | | | | 1/2 |
| | | | | | | /2 |
| 37. (i) | ∠DPQ = ∠DEF | | | | | |
| | ∠PDQ =∠EDF | | | | | |
| | | | . | | | 1 |
| (ii) | (ii) Therefore \triangle DPQ ~ \triangle DEF DE = 50 + 70 = 120 cm | | | | | |
| | | | | | | |
| | $\frac{DP}{DE} = \frac{PQ}{EF}$ | | | | | |
| | D1 | | | | | |

| | Therefore $\frac{PQ}{EF} = \frac{50}{120}$ or $\frac{5}{12}$ | 1⁄2 | | | | |
|-----------|---|---------------------------|--|--|--|--|
| (iii) (A) | $\frac{AB}{DE} = \frac{5}{2} = \frac{BC}{EF} = \frac{AC}{DF}$ $\Rightarrow AB = \frac{5}{2} DE$ | | | | | |
| | $\frac{perimeter \ of \ \triangle ABC}{perimeter \ of \ \triangle DEF} = \frac{\frac{5}{2}(DE + EF + FD)}{DE + EF + FD} = \frac{5}{2} \text{ (Constant)}$ | 1 | | | | |
| | OR | | | | | |
| (iii)(B) | A B M C E N F | Correct fig. ½ mark | | | | |
| | $\frac{AB}{DE} = \frac{BC}{EF} = \frac{BC/2}{EF/2} = \frac{BM}{EN}$ Also $\angle B = \angle E$ | 1 | | | | |
| | Therefore \triangle ABM ~ \triangle DEN. | 1⁄2 | | | | |
| 38. (i) | $ = \sqrt{r^2 + h^2} $ = $\sqrt{(1.5)^2 + (2)^2} $ | 1⁄2 | | | | |
| | $=\sqrt{2.25 + 4}$ = $\sqrt{6.25}$ | | | | | |
| (**) | = 2.5 m | 1⁄2 | | | | |
| (ii) | CSA of cone = Π rl = $\frac{22}{7} \times 1.5 \times 2.5$ | 1⁄2 | | | | |
| | $=$ 11.78 m^2 | 1⁄2 | | | | |
| (iii) (A) | CSA of cylinder = 2Π rh = $2 \times \frac{22}{7} \times 1.5 \times 7$ | 1 | | | | |
| | = 66 m^2 Cost of metal sheet used = 66 x 2000 = ₹1,32,000 | 1 | | | | |
| (iii) (B) | OR Volume of cylinder = $\pi r^2 h$ = $\frac{22}{7} \times (1.5)^2 \times 7$ | | | | | |
| | $= 49.5 m^3$ | 1⁄2 | | | | |

Volume of cone =
$$\frac{1}{3} \pi r^2 h$$

= $\frac{1}{3} \times \frac{22}{7} \times (1.5)^2 \times 2$
= 4.71 m³
Total capacity = 49.5 + 4.71 = 54.21 m³
 $\frac{1}{2}$