

**SECOND TERM EVALUATION 2022 - 2023**

**A**

**X - MATHEMATICS - DETAILED ANSWER KEY**

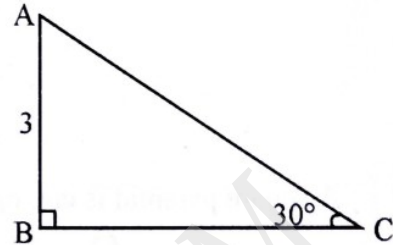
**E 1003**

**Each questions from 1 to 4 carries 2 scores.**

**1**

In the figure,  $\angle B = 90^\circ$ ,  $\angle C = 30^\circ$ ,  $AB = 3$  centimetres

- a) What is the measure of  $\angle A$ ?
- b) Find the length of  $BC$ .



**Answer**

- a)  $\angle A = 60^\circ$
- b)  $BC = 3\sqrt{3} \text{ cm}$

**2**

When each side of a square is increased by 1 metre, the area becomes 49 squaremetres. What is the length of one side of the original square?

**Answer**

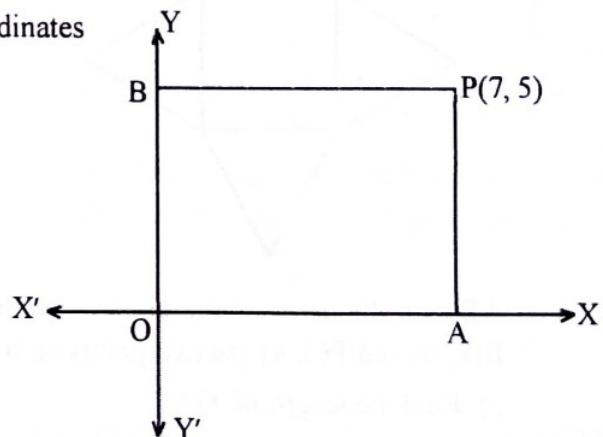
$$(x + 1)^2 = 49$$

$$x + 1 = \sqrt{49} = 7 \implies x = 7 - 1 = 6 \text{ m}$$

**3**

In the figure, OAPB is a rectangle. The coordinates of the point P are (7, 5).

- a) Write the coordinates of A.
- b) Write the coordinates of B.



**Answer**

- a) (7, 0)
- b) (0, 5)

4	<p>PT and PS are tangents of a circle with centre at O. <math>\angle SPT = 60^\circ</math>.</p> <p>a) Find the measure of <math>\angle SOT</math></p> <p>b) Find the measure of <math>\angle POT</math></p>	
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**Answer**

- a)  $\angle SOT = 120^\circ$  ( The centre of a circle touching two lines meeting at a point is on the bisector of the angle formed by the lines )
- b)  $\angle POT = 60^\circ$

**Each questions from 5 to 10 carries 3 scores.**

5	<p>In triangle ABC, <math>\angle B = 90^\circ</math>, AB = 3 centimetres, BC = 4 centimetres.</p> <p>a) What is the length of AC?</p> <p>b) Find sin A and cos A.</p>	
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**Answer**

- a)  $AC = \sqrt{4^2 + 3^2} = \sqrt{16 + 9} = \sqrt{25} = 5 \text{ cm}$
- b)  $\sin A = \frac{BC}{AC} = \frac{4}{5}$
- $\cos A = \frac{AB}{AC} = \frac{3}{5}$

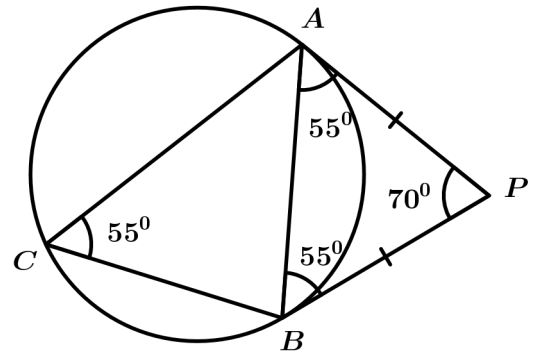
6	<p>In the figure, tangents through A and B meet at P. <math>\angle ACB = 55^\circ</math>.</p> <p>a) What is the measure of <math>\angle PAB</math> ?</p> <p>b) What is the measure of <math>\angle P</math>?</p>	
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**Answer**

a)  $\angle PAB = \angle ACB = 55^\circ$

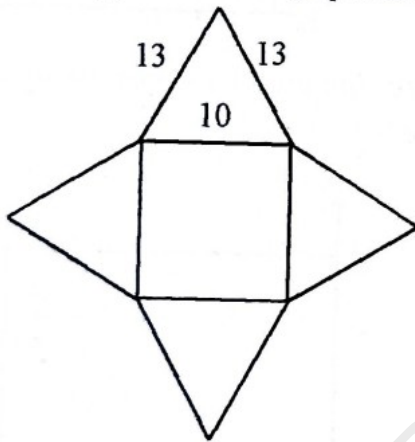
b)  $\angle PBA = \angle PAB = 55^\circ$  ( $PA = PB$ )

$$\begin{aligned}\angle P &= 180^\circ - (55^\circ + 55^\circ) \\ &= 180^\circ - 110^\circ = 70^\circ\end{aligned}$$



7

A square pyramid is cut, open and lay it flat as shown in the figure.



- a) What is the length of its base edge?
- b) Find the slant height of the pyramid

**Answer**

a)  $a = 10$

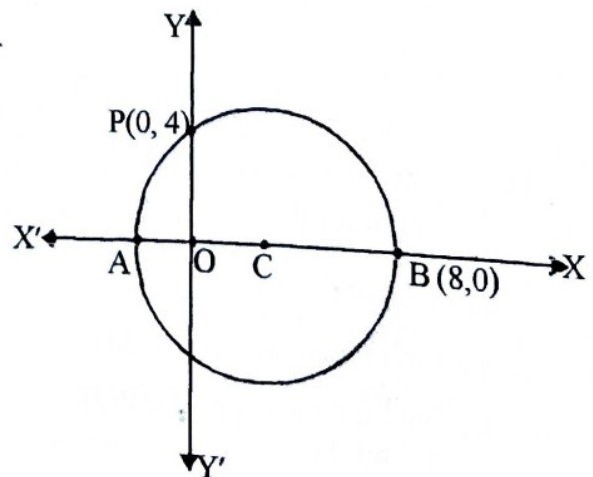
b)  $\left(\frac{a}{2}\right)^2 + l^2 = e^2 \implies \left(\frac{10}{2}\right)^2 + l^2 = 13^2 \implies 5^2 + l^2 = 13^2$

$$25 + l^2 = 169 \implies l^2 = 169 - 25 = 144 \implies l = \sqrt{144} = 12$$

8

AB is a diameter of the circle with centre C.  
B(8, 0) and P(0, 4) are two points on it.

- a) Find the length of OA.
- b) Write the coordinates of A.



**Answer**

a)  $OA \times OB = OP^2 \implies OA \times 8 = 4^2 \implies OA \times 8 = 16$

$$OA = \frac{16}{8} = 2$$

b) **Coordinates of A = (-2, 0)**

9

$x$  represents a natural number.

a) What number should be added to  $x^2 + 8x$  to make it a perfect square?

b) If  $x^2 + 8x = 20$ , then which number is  $x$ ?

**Answer**

a)  $\left(\frac{8}{2}\right)^2 = 16$

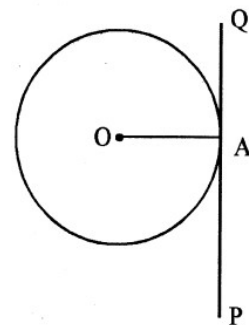
b)  $(x + 4)^2 = 20 + 16 \implies (x + 4)^2 = 36 \implies x + 4 = \sqrt{36} = 6$

$$x = 6 - 4 = 2$$

10

a) PQ is a tangent to the circle with centre at O. What is the measure of  $\angle OAQ$ ?

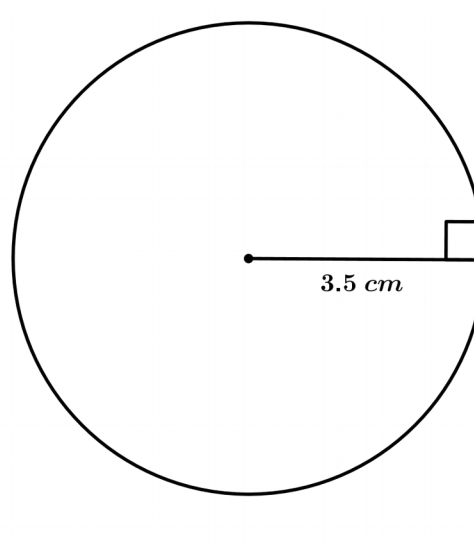
b) Draw a circle of radius 3.5 centimetres. Mark a point A on it. Draw tangent to the circle through A.



**Answer**

a)  $90^\circ$

b)



**Each questions from 11 to 21 carries 4 scores.**

**11**

The base area of a square pyramid is 144 square centimetres and its height is 8 centimetres.

- a) What is the length of one base edge of the pyramid?
- b) What is its slant height?
- c) Find the lateral surface area of the pyramid.

**Answer**

a)  $a = \sqrt{144} = 12 \text{ cm}$

b)  $\left(\frac{a}{2}\right)^2 + h^2 = l^2 \implies \left(\frac{12}{2}\right)^2 + 8^2 = l^2 \implies 36 + 64 = l^2 \implies l^2 = 100$

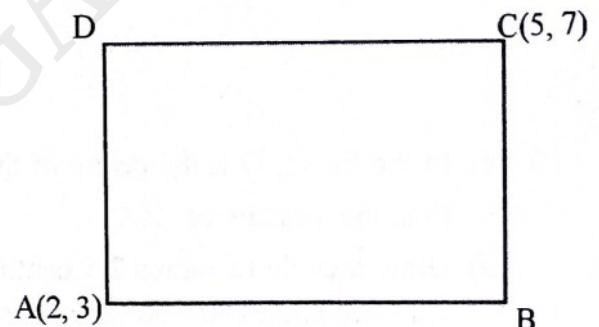
$l = \sqrt{100} = 10 \text{ cm}$

c) **Lateral surface area** =  $2al = 2 \times 12 \times 10 = 240 \text{ sq. cm}$

**12**

In the figure, sides of the rectangle are parallel to the axes. The coordinates of one pair of opposite vertices are A(2, 3) and C(5, 7).

- a) Find the coordinates of the other two vertices.
- b) Find the length of AC.



**Answer**

a) **Coordinates of B** = (5, 3)

**Coordinates of D** = (2, 7)

b)  $AC = \sqrt{(5-2)^2 + (7-3)^2} = \sqrt{25} = 5$

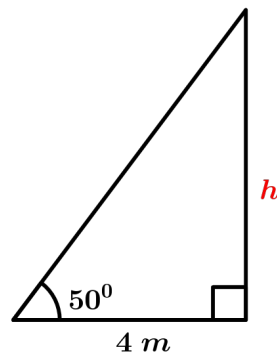
**13**

A ladder is leaned against a wall. It makes an angle  $50^\circ$  with the floor. The foot of the ladder is 4 metres away from the wall. The other end of the ladder touches the top of the wall.

- a) Draw a rough figure representing this.
- b) Find the height of the wall.  
( $\sin 50 = 0.77$ ,  $\cos 50 = 0.64$ ,  $\tan 50 = 1.19$ )

Answer

a)



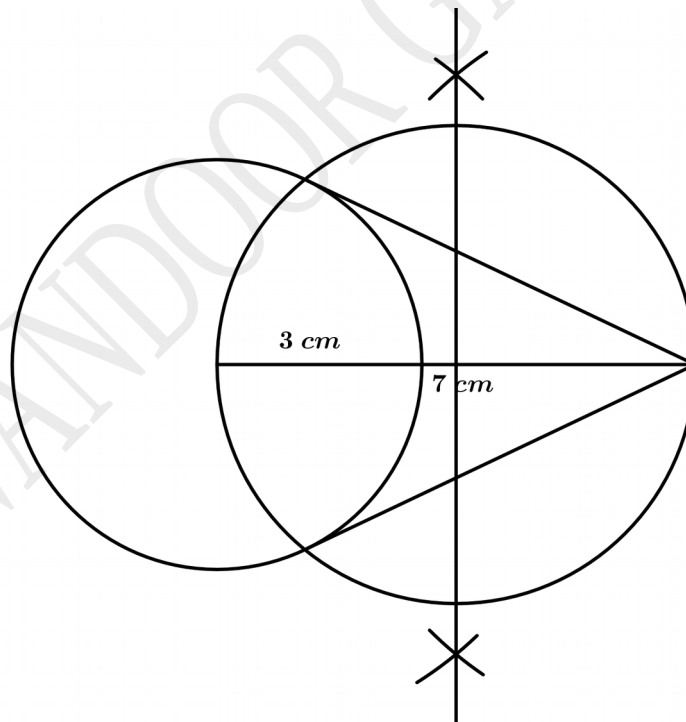
b)  $\tan 50^\circ = \frac{\text{Opposite side of } 50^\circ}{\text{Adjacent side of } 50^\circ} \implies \tan 50^\circ = \frac{h}{4} \implies 1.19 = \frac{h}{4}$

$h = 4 \times 1.19 = 4.76 \text{ m}$

14

Draw a circle of radius 3 centimetres. Mark a point P which is at a distance 7 centimetres away from the centre. Draw the tangents to the circle from P.

Answer



15

The perimeter of a rectangle is 26 centimetres and its area is 40 square centimetres.

a) What is length + width?

b) Taking the breadth of the rectangle as  $x$ , write the length in terms of  $x$

c) Find the length and breadth of the rectangle.

**Answer**

a)  $2 \text{ length} + 2 \text{ breadth} = 26 \text{ cm} \implies \text{length} + \text{breadth} = \frac{26}{2} = 13 \text{ cm}$

b)  $\text{breadth} = x \implies \text{length} = 13 - x$

c)  $x(13 - x) = 40 \implies 13x - x^2 = 40 \implies x^2 - 13x + 40 = 0$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-13) \pm \sqrt{(-13)^2 - 4 \times 1 \times 40}}{2 \times 1}$$

$$= \frac{13 \pm \sqrt{169 - 160}}{2} = \frac{13 \pm \sqrt{9}}{2} = \frac{13 \pm 3}{2}$$

$$x = \frac{13 + 3}{2}$$

OR

$$x = \frac{13 - 3}{2}$$

$$x = \frac{16}{2} = 8$$

$$x = \frac{10}{2} = 5$$

$\text{breadth} = 5 \text{ cm}$

$\text{length} = 13 - 5 = 8 \text{ cm}$

**Another method**

$$x^2 - 13x + 40 = 0$$

$$x^2 - 13x = -40$$

$$x^2 - 13x + \left(\frac{13}{2}\right)^2 = -40 + \left(\frac{13}{2}\right)^2$$

$$\left(x - \frac{13}{2}\right)^2 = -40 + \left(\frac{169}{4}\right) \implies \left(x - \frac{13}{2}\right)^2 = \frac{-160 + 169}{4}$$

$$\left(x - \frac{13}{2}\right)^2 = \frac{9}{4}$$

$$x - \frac{13}{2} = \sqrt{\frac{9}{4}}$$

$$x - \frac{13}{2} = \frac{3}{2}$$

OR

$$x - \frac{13}{2} = \frac{-3}{2}$$

$$x = \frac{3}{2} + \frac{13}{2}$$

$$x = \frac{-3}{2} + \frac{13}{2}$$

$$x = \frac{3 + 13}{2}$$

$$x = \frac{-3 + 13}{2}$$

$$x = \frac{16}{2} = 8$$

$$x = \frac{10}{2} = 5$$

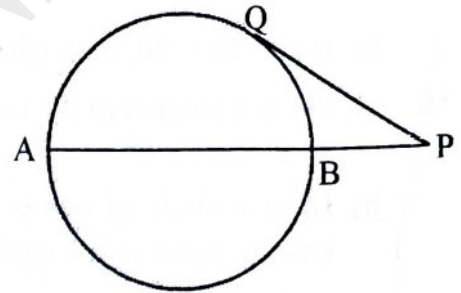
*breadth* = 5 cm

*length* = 13 - 5 = 8 cm

16

In the figure, AB is the diameter of the circle. PQ is a tangent to the circle drawn from P. PA = 12 centimetres and PQ = 6 centimetres.

- Find the length of PB.
- What is the diameter of the circle?



**Answer**

$$\text{a) } PA \times PB = PQ^2 \implies 12 \times PB = 6^2 \implies 12 \times PB = 36$$

$$PB = \frac{36}{12} = 3 \text{ cm}$$

$$\text{b) } AB = PA - PB = 12 - 3 = 9 \text{ cm}$$

17

(6, 4) is a point on a circle drawn with the centre at (3, 0).

- Find the radius of the circle.
- Write the coordinates of the points at which the circle cuts the x axis.

**Answer**

$$\text{a) } \text{Radius} = \sqrt{(6 - 3)^2 + (4 - 0)^2} = \sqrt{25} = 5$$

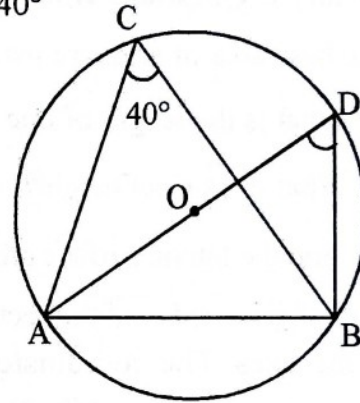
$$\text{b) } (3 + 5, 0) = (8, 0) \quad , \quad (3 - 5, 0) = (-2, 0)$$



18

AD is the diameter of a circle with centre at O,  $\angle C = 40^\circ$

- a)  $\angle D = \underline{\hspace{2cm}}$   
 b)  $\angle ABD = \underline{\hspace{2cm}}$   
 c) If the diameter of the circle is 6 centimetres, find the length of AB.  
 ( $\sin 40 = 0.64$ ,  $\cos 40 = 0.77$ ,  $\tan 40 = 0.84$ )



**Answer**

a)  $\angle D = 40^\circ$  (All angles made by an arc on its alternate arc are equal )

b)  $\angle ABD = 90^\circ$  (Angle in a semicircle is right )

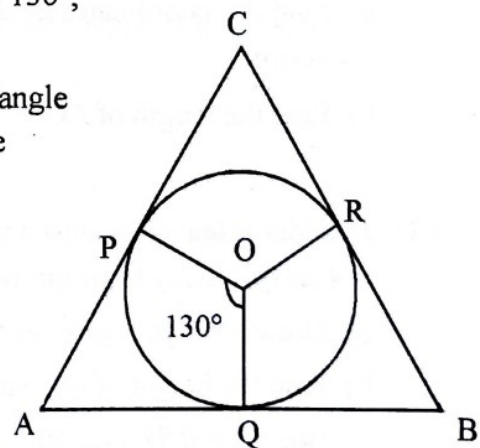
c) In triangle ABD ,  $\sin 40^\circ = \frac{\text{Opposite side of } 40^\circ}{\text{hypotenuse}}$   $\implies \sin 40^\circ = \frac{AB}{6}$

$$0.64 = \frac{AB}{6}$$

$$AB = 0.64 \times 6 = 3.84 \text{ cm}$$

19

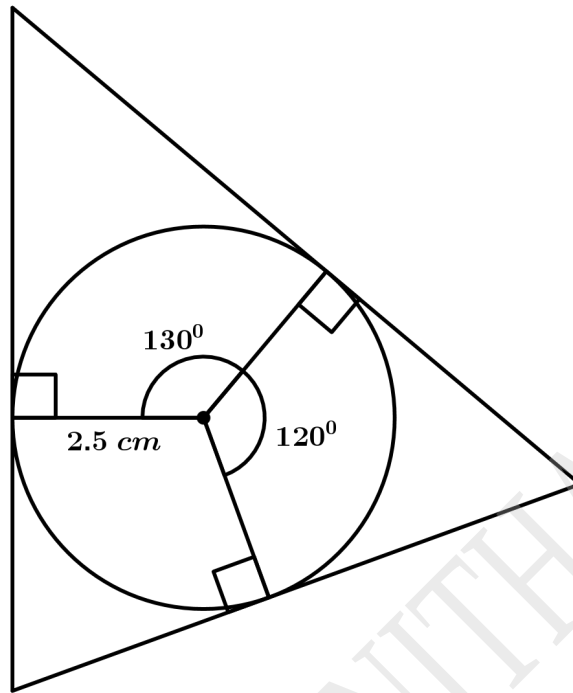
- a) In the figure, O is the centre of the circle.  $\angle POQ = 130^\circ$ , Find the measure of  $\angle A$ ?  
 b) Draw a circle of radius 2.5 centimetres. Draw a triangle with two angles  $50^\circ$ ,  $60^\circ$  and the sides of the triangle touch the circle.



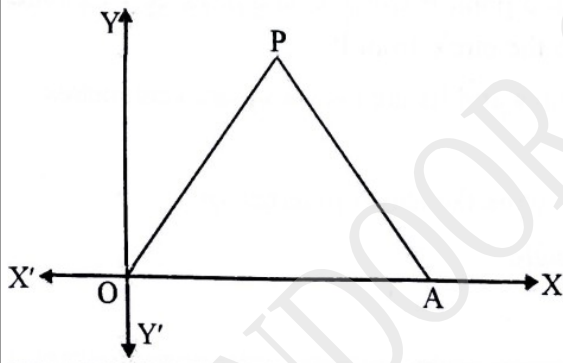
**Answer**

a)  $\angle A = 50^\circ$

b)



20. In the figure, OAP is an equilateral triangle. OA = 6 units.



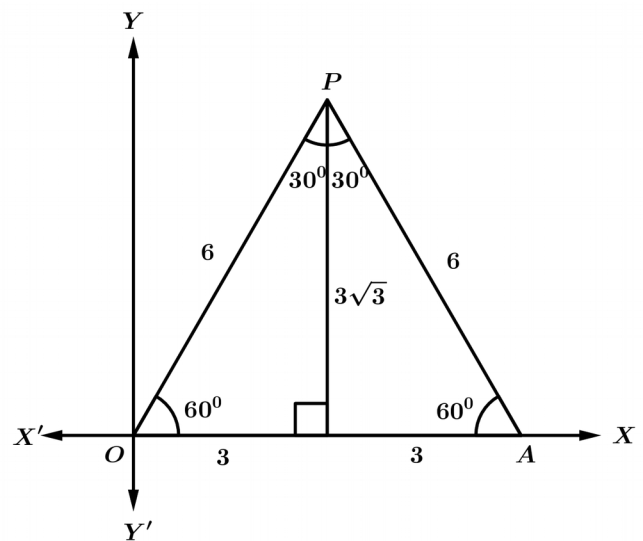
- Write the coordinates of A.
- Find the perpendicular distance from P to the x axis.
- Write the coordinates of P.

**Answer**

a)  $(6, 0)$

b)  $3\sqrt{3}$

c)  $(3, 3\sqrt{3})$

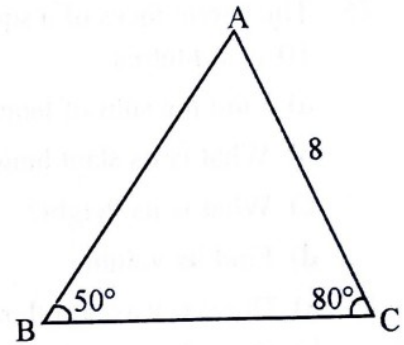


21

In triangle ABC, AC = 8 centimetres  $\angle B = 50^\circ$ ,  $\angle C = 80^\circ$

- What is the measure of  $\angle A$ ?
- Find the length of BC.
- Find the area of the triangle.

$$(\sin 80 = 0.98, \cos 80 = 0.17, \tan 80 = 5.67)$$

**Answer**

$$\text{a) } \angle A = 180^\circ - (50^\circ + 80^\circ) = 180^\circ - 130^\circ = 50^\circ$$

$$\text{b) } BC = 8 \text{ cm} \quad (\angle A = \angle B)$$

- Draw AP perpendicular to BC .

In triangle APC ,

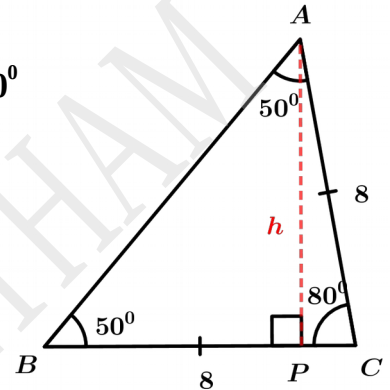
$$\sin 80^\circ = \frac{\text{Opposite side of } 80^\circ}{\text{hypotenuse}}$$

$$\sin 80^\circ = \frac{AP}{AC} \implies 0.98 = \frac{h}{8}$$

$$h = 0.98 \times 8 = 7.84 \text{ cm}$$

$$\text{Area of the triangle ABC} = \frac{1}{2} \times BC \times h$$

$$= \frac{1}{2} \times 8 \times 7.84 = 31.36 \text{ sq. cm}$$

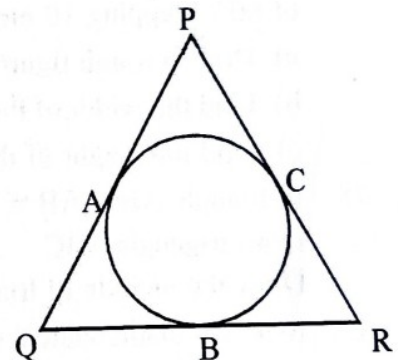


**Each questions from 22 to 29 carries 5 scores.**

22

The sides of triangle PQR touches the circle at the points A, B and C. PQ = 10 centimetres, BR = 4 centimetres.

- What is the length of CR?
- What is QB + PC ?
- Find the perimeter of triangle PQR.
- Find the area of a triangle with perimeter 28 centimetres and radius of the incircle is 2 centimetres.



**Answer**

a)  $CR = 4 \text{ cm}$

b)  $QB + PC = QA + PA = PQ = 10 \text{ cm}$

c) Perimeter of the triangle PQR

$$= PQ + QR + PR$$

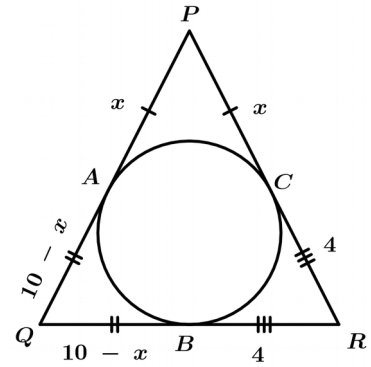
$$= 10 + (QB + BR) + (CR + CP)$$

$$= 10 + QB + 4 + 4 + CP$$

$$= 10 + 8 + QB + CP$$

$$= 10 + 8 + 10 = 28 \text{ cm}$$

d)  $A = \frac{P}{2} \times r \implies \text{Area} = \frac{28}{2} \times 2 = 28 \text{ sq. cm}$



23

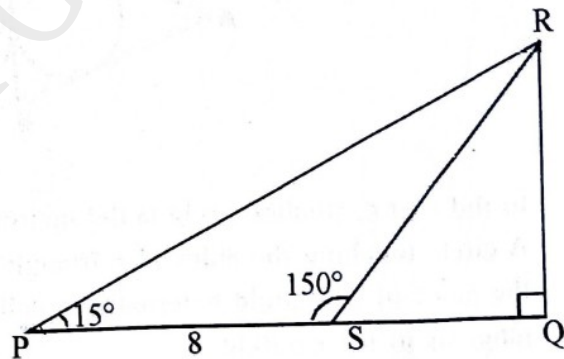
In triangle PQR,  $\angle Q = 90^\circ$ ,  $\angle P = 15^\circ$ ,  $\angle PSR = 150^\circ$ ,  $PS = 8$  centimetres.

a) What is  $\angle PRS$ ?

b) What is the length of SR?

c) Find  $\angle QSR$ .

d) Find the lengths of QS and QR.



**Answer**

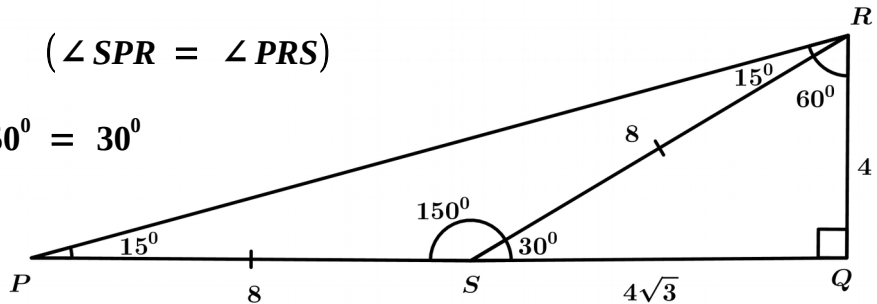
a)  $\angle PRS = 180^\circ - (15^\circ + 150^\circ) = 180^\circ - 165^\circ = 15^\circ$

b)  $SR = 8 \text{ cm}$  ( $\angle SPR = \angle PRS$ )

c)  $\angle QSR = 180^\circ - 150^\circ = 30^\circ$

d)  $QS = 4\sqrt{3} \text{ cm}$

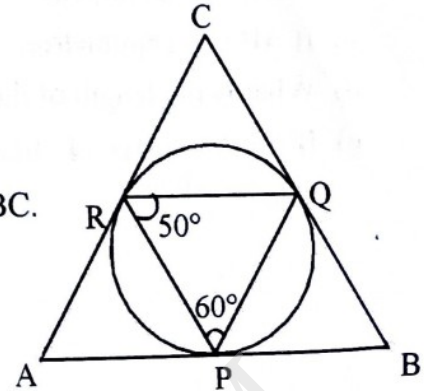
$QR = 4 \text{ cm}$



24

In figure, the sides of triangle ABC touches the circle at the points P, Q and R  
 $\angle QPR = 60^\circ$ ,  $\angle PRQ = 50^\circ$ .

- What is the measure of  $\angle BPQ$ ?
- What is the measure of  $\angle B$ ?
- Find the measures of other two angles of triangle ABC.



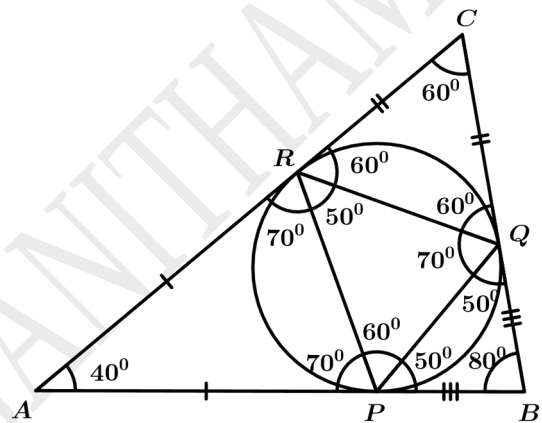
**Answer**

- $\angle BPQ = 50^\circ$
- $\angle BPQ = \angle BQP = 50^\circ$   
 $\angle B = 180^\circ - (50^\circ + 50^\circ)$   
 $= 180^\circ - 100^\circ = 80^\circ$

- $\angle CQR = 60^\circ$

$$\angle CQR = \angle CRQ = 60^\circ \implies \angle C = 180^\circ - (60^\circ + 60^\circ) = 180^\circ - 120^\circ = 60^\circ$$

$$\angle A = 180^\circ - (80^\circ + 60^\circ) = 180^\circ - 140^\circ = 40^\circ$$



25

The lateral faces of a square pyramid are equilateral triangles. The length of its base edge is 10 centimetres.

- Find the sum of lengths of all its edges.
- What is its slant height?
- What is its height?
- Find its volume

**Answer**

a) Sum of the lengths of all edges =  $8 \times 10 = 80 \text{ cm}$

( $a = e = 10 \text{ cm}$ )

b)  $l = 5\sqrt{3} \text{ cm}$

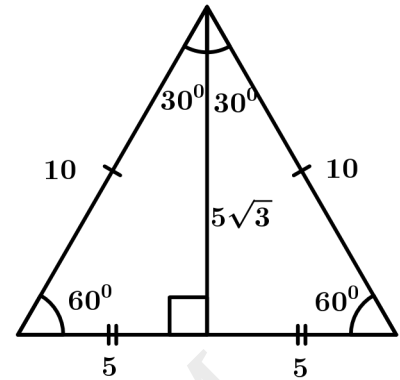
c)  $\left(\frac{a}{2}\right)^2 + h^2 = l^2 \implies \left(\frac{10}{2}\right)^2 + h^2 = (5\sqrt{3})^2$

$$25 + h^2 = 25 \times 3$$

$$h^2 = 75 - 25 = 50$$

$$h = \sqrt{50} = \sqrt{25 \times 2} = \sqrt{50} = 5\sqrt{2} \text{ cm}$$

d) Volume =  $\frac{1}{3} \times a^2 h = \frac{1}{3} \times 10^2 \times 5\sqrt{2} = \frac{500\sqrt{2}}{3} \text{ cubic . cm}$

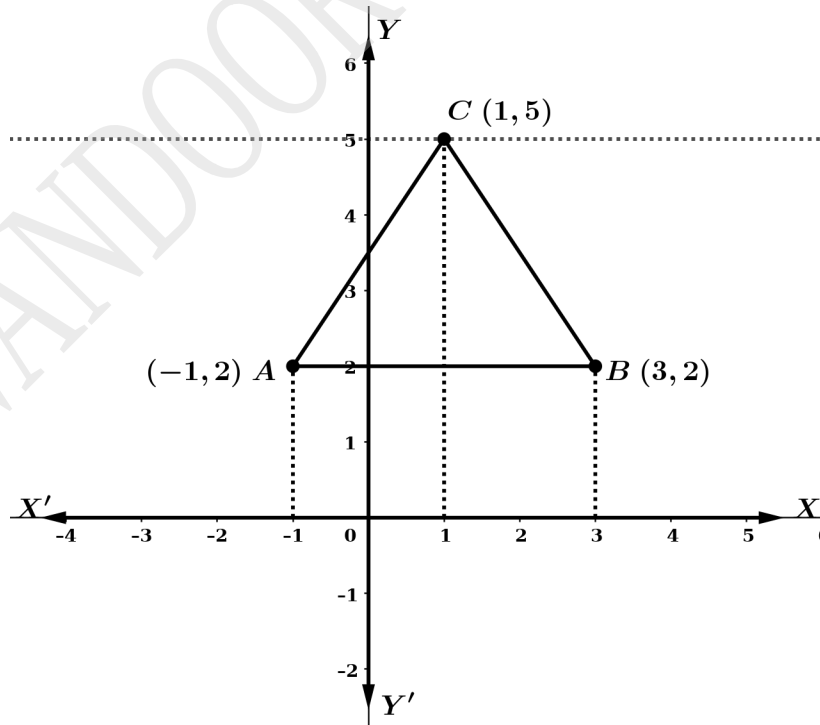


26

- Draw  $x, y$  axes and mark the points  $A(-1, 2)$ ,  $B(3, 2)$  and  $C(1, 5)$
- Draw the triangle joining these points.
- Write the coordinates of any point on the line passing through  $C$  and parallel to  $AB$ .

**Answer**

a)



b)

c)  $(2, 5)$  ( OR any point with  $y$  coordinate 5 )

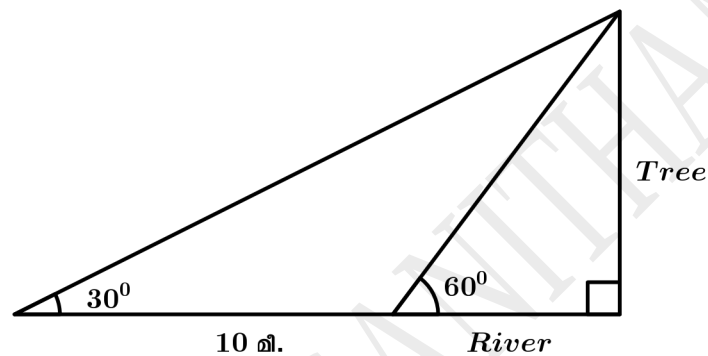
27

A boy standing at the edge of a river sees the top of a tree on the other edge at an elevation of  $60^\circ$ . Stepping 10 metres back, he sees it at an elevation of  $30^\circ$ .

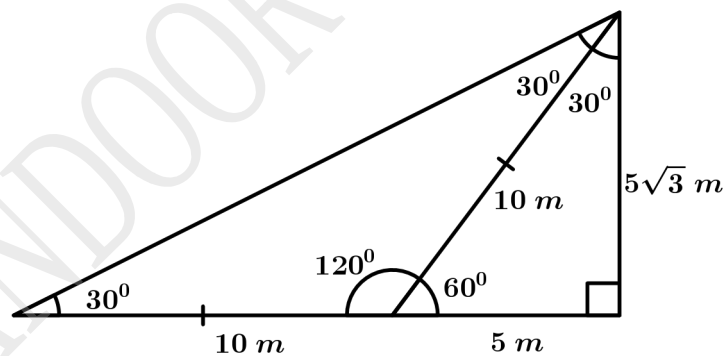
- Draw a rough figure based on the given details.
- Find the width of the river.
- Find the height of the tree.

**Answer**

a)



b)



**Width of the river = 5 m**

**c) Height of the tree =  $5\sqrt{3} m$**

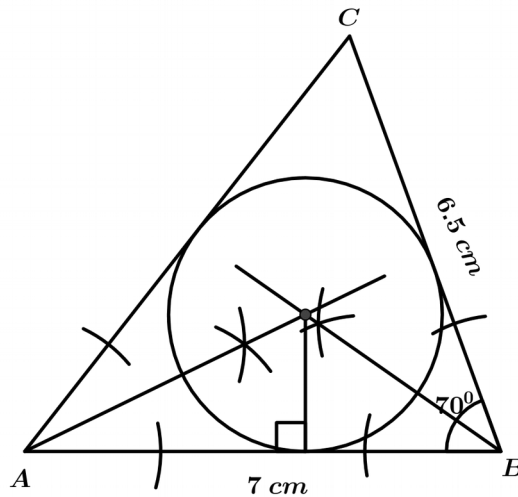
28

In triangle ABC,  $AB = 7$  centimetres,  $BC = 6.5$  centimetres,  $\angle B = 70^\circ$ .

Draw triangle ABC.

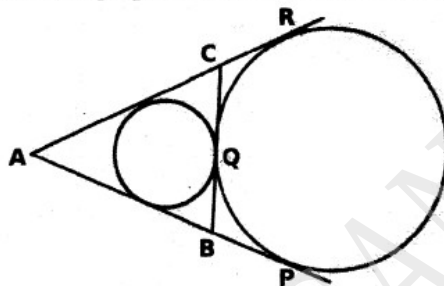
Draw the incircle of triangle ABC.

**Answer**



29

Read the mathematical concept given below and answer the following questions.



In the figure, smaller circle is the incircle of triangle ABC and larger circle is its excircle. A circle touching the sides of a triangle internally is called the incircle. A circle touching the sides of a triangle externally is called excircle. Here AP, AR, CQ, CR, BQ, BP are tangents to the excircle.

- If  $BQ = 3$  centimetres, what is the length of  $BP$ ?
- If  $CQ = 2$  centimetres, what is the length of  $CR$ ?
- If  $AB = 6$  centimetres,  $AC = 7$  centimetres, what is the perimeter of triangle ABC?
- What is the length of the tangent  $AP$ ?
- If the perimeter of triangle ABC is 30 centimetres, what would be the length of the tangent  $AP$ ?

**Answer**

a) 3 cm

b) 2 cm

c)  $13 + BC$

d) Half the perimeter of the triangle ABC .

e)  $\frac{30}{2} = 15$  cm