## SSLC MODEL EXAMINATION- 2023

## Mathematics

## Std X

Score 80<br>Time $21 / 2$ hours

## set 2

Questions from 1 to 4 carries two scores. Answer any three. $3 \times 2=6$

1) Consider the arithmetic sequence $1,5,9 \ldots$
a) What are the next two terms of the sequence ?
b) Write the algebraic form of the sequence.
2) In the figure $A B$ is the diameter of the circle.Line $D E$ is perpendicular to $A E$ and $B D$.

a) What is the measure of $\angle A C B$ ?
b) Suggest a suitable name to $A C D E$
3) Each of the numbers from 1 to 10 are written in small paper pieces and kept in a box. One is taken from the box without looking.
a) What is the probability of getting a multiple of 3 ?
b) What is the probability of getting a prime number?
4) Sum of a counting number and its square is 2 .
a) If $x$ is the number then write the equation
b) Find the number

Questions from 5 to 10 carries three scores. Answer any four . $4 \times 3=12$
5) $A B C$ is an equilateral triangle of perimeter 30 cm

a) What is the length of its side?
b) What is the altitude of the triangle?
6) $A B C$ is a triangle right angled at $A(1,1)$. Another vertex $B$ has co-ordinates $(4,1)$ and $B C=5$

a) What is the length of the side $A B$ ?
b) Find $A C$ and write the co-ordinates of $C$
c) What is the area of the triangle?
7) In the figure $A B$ and $A C$ are tangents from $A$ to the circle with center $O$.


Length of the tangent $A B$ is 7 cm and radius of the circle 3 cm
a) What is the perimeter of $A B O C$ ?
b) What is the measure of $\angle B$ and $\angle C$ ?
c) If $\angle B O C=130^{\circ}$ then what is the measure of $\angle B A C$ ?
8) The base edge of a square pyramid is 10 cm and lateral edge 13 cm

It is made by cutting along the edges of the outline drawn on a square paper.

a) What is the slant height of the square pyramid?
b) What is the side of the square paper on which the outline is drawn
c) Calculate the total surface area of the square pyramid.
9) $(1,1)$ is a point on the circle with center at the origin.

a) What is the radius of the circle?
b) What are the points where the circle cut the axes?
c) Write the equation of the circle.
10) $p(x)=a x^{3}+b x^{2}+c x+d$ is a third degree polynomial.
$p(x)$ has a second degree factor $x^{2}-1$
a) What are the two first degree factors of $p(x)$ ?
b) What is $a+b+c+d$ ?

Questions from $\mathbf{1 1}$ to $\mathbf{2 1}$ carries four scores. Answer any eight. $8 \times 4=32$
11) One side of a rectangle is 12 more than twice the other side.Area of the rectangle is $80 \mathrm{sq} . \mathrm{cm}$. If the smaller side is $x$ then
a) Write the equation.
b) Find the sides.
12) The difference between fifth term and first term of an increasing arithmetic sequence is 12 .
a) What is the difference between second term and sixth term of this sequence?
b) If the third term is 10 then what is 7 th term?
c) What is the common difference of this sequence ?
13) In the figure $A B$ is the diameter of a circle. $\angle A B C=60^{\circ}$

a) What is the measure of $\angle A C B$ ?
b) What is the measure of $\angle A D C$ ?
c) If $A D=C D$ then find $\angle B C D$
d) Find the measure of $\angle D A B$
14) A box contains 4 white balls and 3 black balls.One is taken from the box without looking
a) What is the probability of getting white ball?
b) What is the probability of getting black ball?
c) How many black balls should be added into the box to become the probability of getting black $\frac{5}{7}$
15) Sum of the areas of two circles is $58 \pi$

Radius of one circle is 1 more than two times the other. If the radius of small circle is $x$ then
a) Form an equation.
b) Find the radii of both circles.
16) The window $A$ of a building can be seen at the angle of elevation $32^{\circ}$ at the distance 100 away from the foot of the building.
Window $B$ can be seen at the angle of elevation $45^{\circ}$ from the same point.
a) Draw a suitable diagram
b) What is the height from the foot of the building to the window $B$ ?
c) Calculate the distance between the windows.
$\sin 32^{\circ}=0.52, \cos 32=0.84, \tan 32=0.62$
17) $A(-3,2), B(7,2), C(5,11)$ are the vertices of a triangle.
a) What is the length of the side parallel to $x$ axis ?
b) What is the altitude to that side?
c) Calculate the area of triangle.
18) In triangle $A B C, A B=6 \mathrm{~cm}, \angle A=\angle B=40^{\circ}$
a) Draw the triangle and construct the incircle
b) Write the radius of the incircle by measuring it.
19) A circular sheet of radius 24 cm is cut into two sectors of central angles $120^{\circ}$ and $240^{\circ}$. Sectors are rolled into cones.
a) What is the slant height of both the cones?
b) Find the base radius of the cones.
c) Calcualte the curved surface area of the cones so formed.
20) $y=6$ and $y=2$ are two parallel lines. Both are parallel to $x$ axis.

These lines are tangents to a circle with center $(3,2)$

a) What are the co-ordinates of the points the circle touches the lines ?
b) What is the radius of the circle
c) Write the equation of a tangent perpendicular to both the given lines
d) Write the equation of the circle.

Questions from 22 to 29 carries five scores. Answer any seven. $6 \times 5=30$
21) The table shows the marks scored by the students of a class in an examination.

| Marks | Number of children |
| :---: | :---: |
| $0-10$ | 5 |
| $10-20$ | 11 |
| $20-30$ | 10 |
| $30-40$ | 12 |
| $40-50$ | 7 |

a) If the students are arranged in the ascending order of marks at what position the median mark occurs?
b) What is the mark of 17 th student as the assumption of calculating median
c) Calculate median
22) The difference between fifth term and first term of an increasing arithmetic sequence is 16 .Third term is 19
a) What is the difference between second term and sixth term of this sequence?
b) What is 7 th term?
c) What is the common difference of this sequence ?
d) Write the algebraic form of the sequence.
23) Two angles of a triangle are $70^{\circ}$ and $50^{\circ}$. The verices of the triangle are on a circle of radius 4 cm Construct the triangle .
24) $A B C D$ is a square of side 4 cm .Line $A Q$ touches the semicircle at $P$

a) What is the length $A P$ ?
b) If $Q P=x$ then write $Q C$ and $Q B$ in $x$
c) Find $x$ by considering triangle $A B Q$ and write the length of $A Q$.
25) In the figure chord $A B$ of the circle is extented and marked a point $P$. The line $P C$ is a tangent to the circle.

a) What is $P A \times P B$ ?
b) If $P B=x$ then what is $P A$ ?
c) Find $P B$ and $P A$.
26) In triangle $A B C, \angle C=30^{\circ}, \angle A B C=120^{\circ}, B C=10 \mathrm{~cm}$

a) What is the measure of $\angle B A C$ ?
b) What is the altitude from $A$ to $B C$ ?
c) Find the area of triangle $A B C$.
27) In the figure $A B C D$ is a parallelogram. $A$ is on $y$ axis at the distance 2 from the origin. The vertices $B(4,2)$ and $(8,5)$ are marked in the figure.

a) Write the co-ordinates of $A$ and $D$
b) What is the distance between the parallel sides $A B$ and $C D$ ?
c) What is the area of $A B C D$ ?
28) The second degree polynomial $p(x)=x^{2}+4 x-21$ is written as $p(x)=(x+a)(x+b)=x^{2}+(a+b) x+a b$
a) What is $a+b$ and $a b$
b) Find $a$ and $b$. Write the polynomial as the product of two first degree factors.
c) Find the solution of the equation $x^{2}+4 x-21=0$
29) Look at the sequence of natural numbers.
$1,2,3,4 \cdots$
This is grouped by taking 2 at a time as below
$(1,2),(3,4),(5,6),(7,8) \cdots$
Sequence of the sum of numbers in the group is $3,7,11 \ldots$
This is an arithemtic sequence having common difference 4.
Think about the groups by taking 3 at a time
$(1,2,3),(4,5,6),(7,8,9) \cdots$
Sequence formed by adding them is $6,15,, 24 \cdots$
This is an arithmetic sequence having common difference 9
a) Write the sequence by taking 4 numbers as above.
b) What is the common difference of the sequence so formed by adding the numbers?
c) How many numbers should grouped to get the common difference of the arithemtic sequence 25 ?
d) What is the difference between the sum of first 10 natural numbers and the sum of next 10 natural numbers?
e) Difference between the sum of first $n$ natural numbers and sum of the next $n$ natural numbers is 400. What is $n$ ?

