# SSLC PRE MODEL EVALUATION JANUARY 2023 MATHEMATICS 

Time: $\mathbf{1}^{1 ⁄ 2} \mathbf{~ H r s}$
( English )
Score: 40

Answer any 3 questions from 1 to 4. Each question carries 2 scores . $(3 \times 2=6)$

1. (a) Write down the coordinates of the origin .
(b) What is the y coordinate of any point on the x axis ?
2. In triangle $\mathrm{ABC}, \angle \mathrm{B}=90^{\circ}, \mathrm{BC}=\mathrm{a}, \mathrm{AC}=\mathrm{b}, \mathrm{AB}=\mathrm{c}$
(a) Find $\tan A$
(b) Prove that $\tan A \times \tan C=1$.

3. Calculate the volume of a hemisphere of radius 6 centimetres .
4. What is the inrdius of a triangle of sides $3,4,5$ centimetres ?

Answer any 4 questions from 5 to 10 .Each question carries 3 scores .
$(4 \times 3=12)$
5. Draw a circle of radius 3 centimetres and mark a point on it. Draw a tangent to the circle through that point
6. A sector of radius 12 centimetres and central angle $60^{\circ}$ is rolled up to make a cone
(a) What is the slant height of the cone ?
(b) What is the base radius of the cone ?
7. In parallelogram $\mathrm{ABCD}, \mathrm{AB}=12$ centimetres
$\mathrm{AD}=6$ centimetres and $\angle \mathrm{A}=150^{\circ}$
(a) What is the perpendicular distance from D to AB ?
(b) Calculate the area of the parallelogram .
8. The base area of square pyramid is 144 square centimetres and its volume is 384 cubic centimetres .What are its height and slant height ?
9.


In the picture , ABCD is a rectangle .Its sides are parallel to the axes and origin is its mid point. What are the coordinates of other three vertices ?
10. In the picture, $\mathrm{A}, \mathrm{B}, \mathrm{C}$ are points on the circle .

The tangents through the points A and B meet at P The chord Bc is extended to D and
$\angle \mathrm{OCD}=115^{\circ}$. What are the measures of $\angle \mathrm{BCO}, \angle \mathrm{AOB}$ and $\angle \mathrm{P}$ ?


Answer any 3 questions from 11 to 16 . Each question carries 4 scores. $(3 \times 4=12)$
11. Draw a circle of radius 3.5 centimetres and mark a point $\mathrm{P}, 8$ centimetres away from the centre of the circle. Draw tangents from P to the circle .
12. When sun is at an elevation $30^{\circ}$, the length of the shadow of a tree is $23 \sqrt{3}$ metres
(a) Draw a rough figure using the given detail .
(b) Compute the height of the tree .
(c) What would be the length of the shadow of the same tree, when the sun is at an elevation $25^{\circ}$ ?

$$
\left[\sin 25^{\circ}=0.42, \cos 25^{\circ}=0.91, \tan 25^{\circ}=0.46\right]
$$

13. In the picture, the circle touches the sides of the quadrilateral PQRS at the points $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and D . $\mathrm{PA}=2.6$ centimetres, $\mathrm{QB}=3.3$ centimetres , $\mathrm{RC}=1.3$ centimetres , , $\mathrm{SD}=1.5$ centimetres ,
(a) What are the lengths of the lines PB and QR ?
(b) Calculate the perimeter of the quadrilateral .

14. Draw the $x$ and $y$ axes and mark the points $A(1,0), B(3,0), C(5,0)$ and $D(3,2 \sqrt{3})$
15. From a solid hemisphere of radius 9 centimetres, a cone of maximum possible size is carved out .
(a) What are the base radius and height of the cone ?
(b) What fraction the volume of the hemisphere is the volume of the cone?
16. In the picture , $\mathrm{AB}=9.4$ centimetres , $\angle \mathrm{B}=50^{\circ}, \angle \mathrm{C}=70^{\circ}$.
(a) What is the measure of $\angle \mathrm{A}$ ?
(b) What is the diameter of the circle ?
(c) Compute the lengths of the other two sides of the triangle ?


$$
\begin{aligned}
& {\left[\sin 50^{\circ}=0.76, \quad \cos 50^{\circ}=0.64, \tan 50^{\circ}=1.19\right.} \\
& \left.\sin 70^{\circ}=0.94, \quad \cos 70^{\circ}=0.34, \tan 70^{\circ}=2.74\right]
\end{aligned}
$$

Answer any 2 questions from 17 to 21 . Each question carries 4 scores.

$$
(2 \times 5=10)
$$

17. (a) In the picture, circle centred at $O$ touches the sides of the triangle at the points $\mathrm{P}, \mathrm{Q}$ and $\mathrm{R} . \angle \mathrm{B}=40^{\circ}$ What is the measure of $\angle \mathrm{POQ}$ ?

(b) Draw a circle of radius 2.5 centimetres . Draw a triangle with two angles $40^{\circ}$ and $90^{\circ}$ and all its sides as tangents to this circle .
18. The base radius and length of a metal cylinder are 4 centimetres and 10 centimetres . It is melted and recast into 15 small spheres of equal size .
(a) Calculate the volume of the cylinder .
(b) Calculate the volume of a small sphere .
(c) How many spheres can be made ?
19. 

 In the picture, the chord $A B$ is extended to meet the tangent through $C$ at the point $P$.
(a) If $\angle \mathrm{BCP}=35^{\circ}$, what will be the measure of $\angle \mathrm{BAC}$ ?
(b) Check whether the angles of the triangles APC and BPC are equal or not .
(c) Prove that $P A \times P B=P C^{2}$.
20. In the picture, $D E=4 \sqrt{3}$ centimetres, $\angle \mathrm{E}=60^{\circ}$ and $\angle \mathrm{F}=45^{\circ}$.
(a) What is the measure of $\angle \mathrm{D}$ ?
(b) What is the perpendicular distance from D
 to EF ?
(c) What is the length of EF ?
(d) If the ratio of the angles of a triangle is $3: 4: 5$, what is the ratio of their sides?
21. In the picture, the circle touches the sides of the triangle at $K, L, M$ $\angle \mathrm{LKM}=55^{\circ}$ and $\angle \mathrm{KML}=70^{\circ}$. Write down the measures of the following angles
(a) $\angle \mathrm{CLM}$
(b) $\angle \mathrm{KLB}$
(c) $\angle B$
(d) $\angle \mathrm{A}$

