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MCQ 1.1 GATE ME 2009 ONE MARK
For a matrix $[M] = \begin{bmatrix} 3/5 & 4/5 \\ x & 3/5 \end{bmatrix}$, the transpose of the matrix is equal to the inverse of the matrix, $[M]^T = [M]^{-1}$. The value of x is given by

(A)
$$-\frac{4}{5}$$
 (B) $-\frac{3}{5}$
(C) $\frac{3}{5}$ (D) $\frac{4}{5}$
Option (A) is correct.
Given : $M = \begin{bmatrix} \frac{3}{5} & \frac{4}{5} \\ x & \frac{3}{5} \end{bmatrix}$ (D) $\frac{4}{5}$
And $[M]^T = [M]^{-1}$

We know that when $[A]^T = [A]^{-1}$ then it is called orthogonal matrix.

$$[M]^{T} = \frac{I}{[M]}$$
$$[M]^{T}[M] = I$$

Substitute the values of $M \& M^T$, we get

$$\begin{bmatrix} \overrightarrow{3} & \overrightarrow{3} \\ \frac{4}{5} & \overrightarrow{3} \\ \frac{4}{5} & \frac{3}{5} \end{bmatrix} \checkmark \begin{bmatrix} \frac{3}{5} & \frac{4}{5} \\ x & \frac{3}{5} \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$
$$\begin{bmatrix} \left(\frac{3}{5} \times \frac{3}{5}\right) + x^2 & \left(\frac{3}{5} \times \frac{4}{5}\right) + \frac{3}{5}x \\ \left(\frac{4}{5} \times \frac{3}{5}\right) + \frac{3}{5}x & \left(\frac{4}{5} \times \frac{4}{5}\right) + \left(\frac{3}{5} \times \frac{3}{5}\right) \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$
$$\begin{bmatrix} \frac{9}{25} + x^2 & \frac{12}{25} + \frac{3}{5}x \\ \frac{12}{25} + \frac{3}{5}x & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

Comparing both sides a_{12} element,

$$\frac{12}{25} + \frac{3}{5}x = 0$$

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SOL 1.1

Page 2

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 $x = -\frac{12}{25} \times \frac{5}{3} = -\frac{4}{5}$ The divergence of the vector field $3xzi + 2xyj - yz^2k$ at a point (1,1,1) is equal to **MCQ 1.2** (A) 7(B) 4GATE ME 2009 ONE MARK (C) 3 (D) 0 Option (C) is correct. **SOL 1.2** $V = 3xzi + 2xyj - yz^2k$ Let, We know divergence vector field of V is given by $(\nabla \cdot V)$ $\nabla \cdot \mathbf{V} = \left(\frac{\partial}{\partial x}i + \frac{\partial}{\partial y}j + \frac{\partial}{\partial z}k\right) \cdot \left(3xz\mathbf{i} + 2xy\mathbf{j} - yz^2\mathbf{k}\right)$ So, $\nabla \cdot \mathbf{V} = 3z + 2x - 2yz$ At point P(1,1,1) $(\nabla \cdot V)_{P(1.1.1)} = 3 \times 1 + 2 \times 1 - 2 \times 1 \times 1 = 3$ The inverse Laplace transform of $1/(s^2 + s)$ is **MCQ 1.3** (A) $1 + e^{t}$ (B) $1 - e^{t}$ GATE ME 2009 ONE MARK **<u>g**at</u>e^{(D) 1+ e^{-t}} (C) $1 - e^{-t}$ Option (C) is correct. **SOL 1.3** $f(s) = \mathcal{L}^{-1} \left[\frac{1}{s^2 + s} \right]$ Let First, take the function $\frac{1}{s^2 + s}$ & break it by the partial fraction, $\frac{1}{s^2 + s} = \frac{1}{s(s+1)} = \frac{1}{s} - \frac{1}{(s+1)} \qquad \qquad \begin{cases} \text{Solve by} \\ \frac{1}{(s+1)} = \frac{A}{s} + \frac{B}{s+1} \end{cases}$ $\mathcal{L}^{-1}\left(\frac{1}{s^2+s}\right) = \mathcal{L}^{-1}\left[\frac{1}{s} - \frac{1}{(s+1)}\right]$ So, $= \mathcal{L}^{-1} \left[\frac{1}{s} \right] - \mathcal{L}^{-1} \left[\frac{1}{s+1} \right] = 1 - e^{-t}$ If three coins are tossed simultaneously, the probability of getting at least one head **MCQ 1.4** GATE ME 2009 is ONE MARK (A) 1/8(B) 3/8(D) 7/8 (C) 1/2Option (D) is correct. **SOL 1.4**

Total number of cases $= 2^3 = 8$

& Possible cases when coins are tossed simultaneously.

- Η Η Η Η Η Т Η Т Η Т Η Η Η Т Т Т Η Т Т Т Η
- т т т

From these cases we can see that out of total 8 cases 7 cases contain at least one head. So, the probability of come at least one head is $=\frac{7}{8}$



If a closed system is undergoing an irreversible process, the entropy of the system

- GATE ME 2009 (A) must increase ONE MARK
 - (B) always remains constant
 - (C) Must decrease
 - (D) can increase, decrease or remain constant
- **SOL 1.5** Option (A) is correct.

We consider the cycle shown in figure, where A and B are reversible processes and C is an irreversible process. For the reversible cycle consisting of A and B.

help



$$\int_{R} rac{dQ}{T} = \int_{A1}^{2} rac{dQ}{T} + \int_{B2}^{1} rac{dQ}{T} = 0$$
 $\int_{A1}^{2} rac{dQ}{T} = -\int_{B2}^{1} rac{dQ}{T}$

or

For the irreversible cycle consisting of A and C, by the inequality of clausius,

$$\oint \frac{dQ}{T} = \int_{A_1}^2 \frac{dQ}{T} + \int_{C_2}^1 \frac{dQ}{T} < 0 \qquad \dots (ii)$$

From equation (i) and (ii)

$$-\int_{B2}^{1} \frac{dQ}{T} + \int_{C2}^{1} \frac{dQ}{T} < 0$$
$$\int_{B2}^{1} \frac{dQ}{T} > \int_{C2}^{1} \frac{dQ}{T} \qquad \dots(iii)$$

Since the path B is reversible,

$$\int_{B2}^{1} \frac{dQ}{T} = \int_{B2}^{1} ds$$

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...(i)

Since entropy is a property, entropy changes for the paths B and C would be the same.

Therefore,

$$\int_{B2}^{1} ds = \int_{C2}^{1} ds \qquad \dots (iv)$$

From equation (iii) and (iv), $\int_{C^2}^1 ds > \int_{C^2}^1 \frac{dQ}{T}$

Thus, for any irreversible process.

$$ds > \frac{dQ}{T}$$

So, entropy must increase.

MCQ 1.6 GATE ME 2009 ONE MARK

temperature of 100°C. The boundary layer temperature distribution at a given location on the plate may be approximated as $T = 30 + 70 \exp(-y)$ where y (in m) is the distance normal to the plate and T is in $^{\circ}$ C. If thermal conductivity of the fluid is 1.0 W/mK, the local convective heat transfer coefficient (in $\text{W/m}^2\text{K}$) at that location will be

A coolant fluid at 30°C flows over a heated flat plate maintained at constant

SOL 1.6 Option (B) is correct.
Given :
$$T_1 = 30^{\circ}$$
 C, $T_2 = 100^{\circ}$ C, $k = 1.0$ W/mK
 $T = 30 + 70 \exp(-y)$

$$T_1=30^{\circ}C$$

Under steady state conditions,

Heat transfer by conduction = Heat transfer by convection

$$-kA\frac{dT}{dy} = hA\Delta T \qquad \qquad A \to \text{Area of plate}$$
$$-kA\frac{d}{dy}(30+70e^{-y}) = hA\Delta T$$

On solving above equation, we get

$$-kA\left(-70\,e^{-y}\right) = hA\Delta T$$

At the surface of plate, y = 0 $70kA = hA\Delta T$ Hence,

$$h = \frac{70kA}{A\Delta T} = \frac{70k}{\Delta T} = \frac{70 \times 1}{(100 - 30)} = 1 \text{ W/m}^2 \text{ K}$$

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...(i)

Page 5	ME GATE-09	www.gatehelp.com
MCQ 1.7 GATE ME 2009 ONE MARK	A frictionless piston-cylinder device contains a gas initially at 0 It expands quasi-statically at constant temperature to a fina. The work output (in kJ) during this process will be(A) 8.32(B) 12.00(C) 554.67(D) 8320.00	
SOL 1.7	Option (A) is correct. Given : $p_1 = 0.8$ MPa, $\nu_1 = 0.015 \text{ m}^3$, $\nu_2 = 0.030 \text{ m}^3$, $T = \text{Const}$. We know work done in a constant temperature (isothermal) p $W = p_1 \nu_1 \ln\left(\frac{\nu_2}{\nu_1}\right) = (0.8 \times 10^6) (0.015) \ln\left(\frac{0.0}{0.0}\right)$ $= (0.012 \times 10^6) \times 0.6931 = 8.32 \text{ kJ}$	process
MCQ 1.8 GATE ME 2009 ONE MARK	In an ideal vapour compression refrigeration cycle, the specific er (in kJ/kg) at the following states is given as: Inlet of condenser :283 Exit of condenser :116 Exit of evaporator :232 The COP of this cycle is (A) 2.27 (C) 3.27 Gate (B) 2.75 (D) 3.75	nthalpy of refrigerant
SOL 1.8	Option (A) is correct. First of all we have to make a $p - h$ curve for vapour composite $p_1 = p_3$ 3 Cond. $p_2 = p_3$ 3 Cond. $p_1 = p_4$ 4 Evap. h_1 h_2 Enthalpy The given specific enthalpies are Inlet of condenser $h_2 = 283$ kJ/kg Frit of condenser $h_2 = 116$ kL/kg = h	pression refrigeration

Exit of condenser $h_3 = 116 \text{ kJ/kg} = h_4$ Exit of evaporator $h_1 = 232 \text{ kJ/kg}$ Now, $COP = \frac{\text{Refrigerating effect}}{\text{Work done}} = \frac{h_1 - h_4}{h_2 - h_1}$

From p-h curve

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Substitute the values, we get

$$COP = \frac{232 - 116}{283 - 232} = \frac{116}{51} = 2.27$$

MCQ 1.9 GATE ME 2009 TWO MARK

A compressor undergoes a reversible, steady flow process. The gas at inlet and outlet of the compressor is designated as state 1 and state 2 respectively. Potential and kinetic energy changes are to be ignored. The following notations are used : $\nu =$ Specific volume and p = pressure of the gas.

The specific work required to be supplied to the compressor for this gas compression process is

(A)
$$\int_{1}^{2} p d\nu$$
 (B) $\int_{1}^{2} \nu dp$
(C) $\nu_{1}(p_{2} - p_{1})$ (D) $-p_{2}(\nu_{1} - \nu_{2})$

SOL 1.9

Option (B) is correct.



Steady flow energy equation for a compressor (Fig a) gives,

 $h_1 + dQ = h_2 + dW_x \qquad \dots (i)$

Neglecting the changes of potential and kinetic energy. From the property relation $Tds\,=\,dh-\nu dp$

For a reversible process,

So.

And

$$Tds = dQ$$

$$dQ = dh - \nu dp$$
 ...(ii)

If consider the process is reversible adiabatic then dQ = 0From equation (i) and (ii),

$$h_2 = dW_x \quad \Rightarrow dh = h_2 - h_1 = -dW_x \qquad \dots (iii)$$

...(iv)

From equation (iii) and (iv),

 $h_1 -$

$$-dW_x =
u dp \ W_x = -\int
u dp$$

 $dh = \nu dp$

Negative sign shows the work is done on the system (compression work) for initial & Final Stage $W_x = \int_1^2 \nu dp$

between the block and the horizontal surface is $\mu = 0.2$. A vertical cable attached to the block provides partial support as shown. A man can pull horizontally with a force of 100 N. What will be the tension, T (in N) in the cable if the man is just able to move the block to the right ?



Using the balancing of forces, we get In x direction $\Sigma F_x = 0$

$$\mu R_N = 100 \text{ N}$$
$$R_N = \frac{100}{\mu} = \frac{100}{0.2} = 500 \text{ N}$$

and $\Sigma F_y = 0$ or downward forces = upward forces $W = T + R_N$ $T = W - R_N = 981 - 500 = 481 \text{ N}$

MCQ 1.11If the principal stresses in a plane stress problem are $\sigma_1 = 100$ MPa, $\sigma_2 = 40$ MPa,GATE ME 2009
ONE MARKthe magnitude of the maximum shear stress (in MPa) will be
(A) 60
(C) 30(B) 50
(D) 20

SOL 1.11 Option (C) is correct.

Given : $\sigma_1 = 100 \text{ MPa}$, $\sigma_2 = 40 \text{ MPa}$ We know, the maximum shear stress for the plane complex stress is given by

$$\tau_{\max} = \frac{\theta_1 - \theta_2}{2}$$

$$\tau_{\max} = \frac{100 - 40}{2} = \frac{60}{2} = 30 \text{ MPa}$$

MCQ 1.12 GATE ME 2009 ONE MARK A simple quick return mechanism is shown in the figure. The forward to return ratio of the quick return mechanism is 2:1. If the radius of crank O_1P is 125 mm, then the distance 'd' (in mm) between the crank centre to lever pivot centre point should be



Substitute the value of Forward to return ratio, we have

$$\frac{2}{1} = \frac{360 - \alpha}{\alpha}$$

$$2\alpha = 360 - \alpha \qquad \Rightarrow \alpha = 120^{\circ}$$

$$\stackrel{}{=} \frac{RO_1O_2}{2} = \frac{\alpha}{2} = \frac{120^{\circ}}{2} = 60^{\circ}$$

Now we are to find the distance 'd' between the crank centre to lever pivot centre point $(O_1 O_2)$. From the $\Delta R O_2 O_1$

$$\sin\left(90^{\circ} - \frac{\alpha}{2}\right) = \frac{O_1 R}{O_1 O_2} = \frac{r}{O_1 O_2}$$
$$\sin\left(90^{\circ} - 60^{\circ}\right) = \frac{r}{O_1 O_2}$$
$$O_1 O_2 = \frac{r}{\sin 30^{\circ}} = \frac{125}{1/2} = 250 \text{ mm}$$

And angle

The rotor shaft of a large electric motor supported between short bearings at both the ends shows a deflection of 1.8 mm in the middle of the rotor. Assuming the rotor to be perfectly balanced and supported at knife edges at both the ends, the likely critical speed (in rpm) of the shaft is

- (A) 350 (C) 2810 (B) 705 (C) 2810 (C) 2810 (C) 4430
- **SOL 1.13** Option (B) is correct. Given $\delta = 1.8 \text{ mm} = 0.0018 \text{ m}$ The critical or whiching speed is given

The critical or whirling speed is given by,

$$\begin{split} \omega_c &= \sqrt{\frac{g}{\delta}} \\ \frac{2\pi N_c}{60} &= \sqrt{\frac{g}{\delta}} \\ N_c &= \frac{60}{2\pi} \sqrt{\frac{g}{\delta}} = \frac{60}{2 \times 3.14} \sqrt{\frac{9.81}{0.0018}} \\ &= 9.55 \sqrt{5450} = 704.981 \simeq 705 \, \text{rpm} \end{split}$$

MCQ 1.14 A solid circular shaft of diameter d is subjected to a combined bending moment Mand torque, T. The material property to be used for designing the shaft using the relation $\frac{16}{\pi d^3}\sqrt{M^2 + T^2}$ is

- (A) ultimate tensile strength (S_u) (B) tensile yield strength (S_y)
- (C) torsional yield strength (S_{sy}) (D) endurance strength (S_e)
- **SOL 1.14** Option (C) is correct.



We know that, for a shaft of diameter d is subjected to combined bending moment M and torque T, the equivalent Torque is,

$$T_e = \sqrt{M^2 + T^2}$$

Induced shear stress is,

$$\tau = \frac{16T}{\pi d^3} = \frac{16}{\pi d^3} \times \sqrt{M^2 + T^2}$$

Now, for safe design, τ should be less than $\frac{S_{sy}}{N}$

Where, S_{sy} = Torsional yield strength and N = Factor of safety

MCQ 1.15 GATE ME 2009 ONE MARK

SOL 1.15

The effective number of lattice points in the unit cell of simple cubic, body centered cubic, and face centered cubic space lattices, respectively, are (A) 1, 2, 2(B) 1, 2, 4(D) 2, 4, 4 (C) 2, 3, 4D Option (B) is correct. (i)Simple cubic Atom

Effective Number of lattice $=\frac{1}{8} \times 8 = 1$ Effective Number $=\frac{1}{8} \times 8 + 1 = 2$ (iii)FCC



of activity time is based upon three different time estimates made for each activity. These are as follows.

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- t_o = the optimistic time, is the shortest possible time to complete the activity if all goes well.
- t_p = the pessimistic time, is the longest time that an activity could take if every thing goes wrong
- t_l = the most likely time, is the estimate of normal time an activity would take.

The expected time (t_e) of the activity duration can be approximated as the arithmetic mean of $(t_o + t_p)/2$ and $2t_l$. Thus

$$(t_e) = \frac{1}{3} \left[2t_l + \frac{(t_o + t_p)}{2} \right] = \frac{t_o + 4t_l + t_p}{6}$$

MCQ 1.19 Which of the following is the correct data structure for solid models ?

- GATE ME 2009 (A) solid part \rightarrow faces \rightarrow edges \rightarrow vertices ONE MARK
 - (B) solid part \rightarrow edges \rightarrow faces \rightarrow vertices
 - (C) vertices \rightarrow edges \rightarrow faces \rightarrow solid parts
 - (D) vertices \rightarrow faces \rightarrow edges \rightarrow solid parts
- **SOL 1.19** Option (C) is correct. Correct data structure for solid models is given by, Vertices \rightarrow edges \rightarrow faces \rightarrow solid parts

MCQ 1.20Which of the following forecasting methods takes a fraction of forecast error into
account for the next period forecast ?ONE MARK(A) is the result of the last of the last

- (A) simple average method (B) moving average method
- (C) weighted moving average method (D) exponential smoothening method

SOL 1.20 Option (D) is correct.

Exponential smoothing method of forecasting takes a fraction of forecast error into account for the next period forecast.

The exponential smoothed average u_t , which is the forecast for the next period (t+1) is given by.

$$u_{t} = \alpha y_{t} + \alpha (1 - \alpha) y_{t-1} + \dots \alpha (1 - \alpha)^{n} y_{t-n} + \dots \infty$$

= $\alpha y_{t} + (1 - \alpha) [\alpha y_{t-1} + \alpha (1 - \alpha) y_{t-2} + \dots + \alpha (1 - \alpha)^{n} y_{t-(n-1)} + \dots]$
= $u_{t-1} + \alpha (y_{t} - u_{t-1})$
= $u_{t-1} + \alpha e_{t}$

where $e_t = (y_t - u_{t-1})$ is called error and is the difference between the least observation, y_t and its forecast a period earlier, u_{t-1} . The value of α lies between 0 to 1.

MCQ 1.21 An analytic function of a complex variable z = x + iy is expressed as GATE ME 2009 TWO MARK f(z) = u(x, y) + iv(x, y) where $i = \sqrt{-1}$. If u = xy, the expression for v should be

(A)
$$\frac{(x+y)^2}{2} + k$$

(B) $\frac{x^2 - y^2}{2} + k$
(C) $\frac{y^2 - x^2}{2} + k$
(D) $\frac{(x-y)^2}{2} + k$

SOL 1.21 Option (C) is correct.

Given : z = x + iy is a analytic function f(z) = u(x, y) + iv(x, y)u = xy...(i)

We know that analytic function is satisfy the Cauchy-Riemann equation.

$$\frac{\partial u}{\partial x} = \frac{\partial v}{\partial y} \quad \& \quad \frac{\partial u}{\partial y} = -\frac{\partial v}{\partial x}$$

So from equation (i),

$$\frac{\partial u}{\partial x} = y \quad \Rightarrow \qquad \frac{\partial v}{\partial y} = y$$
$$\frac{\partial u}{\partial y} = x \quad \Rightarrow \qquad \frac{\partial v}{\partial x} = -x$$

Let v(x, y) be the conjugate function of u(x, y)

$$dv = \frac{\partial v}{\partial x}dx + \frac{\partial v}{\partial y}dy = (-x) dx + (y) dy$$

Integrating both the sides

$$\int dv = -\int x dx + \int y dy \mathbf{P} \mathbf{P}$$

$$v = -\frac{x^2}{2} + \frac{y^2}{2} + k = \frac{1}{2}(y^2 - x^2) + k$$

MCQ 1.22 The solution of $x\frac{dy}{dx} + y = x^4$ with the condition $y(1) = \frac{6}{5}$ is

TWO MARK

(A)
$$y = \frac{x^4}{5} + \frac{1}{x}$$
 (B) $y = \frac{4x^4}{5} + \frac{4}{5x}$
(C) $y = \frac{x^4}{5} + 1$ (D) $y = \frac{x^5}{5} + 1$

SOL 1.22

.22 Option (A) is correct.

Given

$$x\frac{dy}{dx} + y = x^{4}$$
$$\frac{dy}{dx} + \left(\frac{1}{x}\right)y = x^{3}$$
...(i)

It is a single order differential equation. Compare this with $\frac{dy}{dx} + Py = Q$ & we get $P = \frac{1}{x}$ $Q = x^3$

And its solution will be

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$$y(I.F.) = \int Q(I.F.) dx + C$$

$$I.F. = e^{\int Pdx} = e^{\int \frac{1}{x}dx} = e^{\log_e x} = x$$
And complete solution is given by,

$$yx = \int x^3 \times x dx + C$$

$$= \int x^4 dx + C = \frac{x^5}{5} + C \qquad \dots (ii)$$
And $y(1) = \frac{6}{5}$ at $x = 1 \Rightarrow y = \frac{6}{5}$ From equation (ii),

$$\frac{6}{5} \times 1 = \frac{1}{5} + C$$

$$C = \frac{6}{5} - \frac{1}{5} = 1$$

Then, from equation (ii), we get

$$yx = \frac{x^5}{5} + 1 \Rightarrow y = \frac{x^4}{5} + \frac{1}{x}$$

MCQ 1.23 GATE ME 2009 TWO MARK







The equation of circle with unit radius & centre at origin is given by,

Option (B) is correct.

Finding the integration of $(x + y)^2$ on path AB traversed in counter-clockwise sense

So using the polar form Let: $x = \cos \theta$, $y = \sin \theta$ r = 1So put the value of x & y & limits in first quadrant between 0 to $\pi/2$. Hence,

$$I = \int_0^{\pi/2} (\cos\theta + \sin\theta)^2 d\theta$$
$$= \int_0^{\pi/2} (\cos^2\theta + \sin^2\theta + 2\sin\theta\cos\theta) d\theta = \int_0^{\pi/2} (1 + \sin 2\theta) d\theta$$

On integrating above equation, we get

$$= \left[\theta - \frac{\cos 2\theta}{2}\right]_{0}^{\pi/2}$$
$$= \left[\left(\frac{\pi}{2} - \frac{\cos \pi}{2}\right) - \left(0 - \frac{\cos \theta}{2}\right)\right]$$
$$= \left(\frac{\pi}{2} + \frac{1}{2}\right) - \left(-\frac{1}{2}\right) = \frac{\pi}{2} + 1$$

The distance between the origin and the point nearest to it on the surface $z^2 = 1 + xy$ **MCQ 1.24** GATE ME 2009 is TWO MARK

(A) 1
(C)
$$\sqrt{3}$$

Option (A) is correct.
(B) $\frac{\sqrt{3}}{2}$
Gate (D) 2
Lolo

 $z^2 = 1 + xy$

SOL 1.24

Let

...(i)

Let P(x, y, z) be the nearest point on the surface (i), then distance from the origin is $d = \sqrt{(x-0)^2 + (y-0)^2 + (z-0)^2}$

пеір

$$d^{2} = x^{2} + y^{2} + z^{2}$$

$$z^{2} = d^{2} - x^{2} - y^{2}$$
 ...(ii)

From equation (i) & (ii), we get $d^2 - x^2 - y^2 - 1 + xy$ d^2

The given equation of surface is

$$\begin{aligned} -x^2 - y^2 &= 1 + xy \\ d^2 &= x^2 + y^2 + xy + 1 \\ f(x,y) &= d^2 &= x^2 + y^2 + xy + 1 \end{aligned} \qquad \dots (iii)$$

The f(x, y) be the maximum or minimum according to d^2 maximum or minimum. Differentiating equation (iii) w.r.t x & y respectively, we get

 $\frac{\partial f}{\partial x} = 2x + y \text{ or } \frac{\partial f}{\partial y} = 2y + x$ Applying maxima – minima principle & put $\frac{\partial f}{\partial x}$ & $\frac{\partial f}{\partial y}$ equal to zero, $\frac{\partial f}{\partial x} = 2x + y = 0 \text{ or } \frac{\partial f}{\partial y} = 2y + x = 0$

on solving these equations, we get x = 0, y = 0So, x = y = 0 is only one stationary point. $\partial^2 f$ $\mathbf{2}$ Now

$$p = \frac{\partial f}{\partial x^2} =$$



Similarly put y = 0 in curve $x^2 = 4y$ $x^2 = 4 \times 0 = 0 \Rightarrow x = 0$ And Put y = 4 $x^2 = 4 \times 4 = 16$ x = 4

So,

Therefore the intersection points of the curves are (0,0) & (4,4). So the enclosed area is given by

$$A = \int_{x_1}^{x_2} (y_1 - y_2) \, dx$$

x = 4.0

Put $y_1 \& y_2$ from the equation of curves $y^2 = 4x \& x^2 = 4y$

$$A = \int_0^4 \left(\sqrt{4x} - \frac{x^2}{4}\right) dx$$

= $\int_0^4 \left(2\sqrt{x} - \frac{x^2}{4}\right) dx = 2\int_0^4 \sqrt{x} \, dx - \frac{1}{4}\int_0^4 x^2 \, dx$

Integrating the equation, we get

$$A = 2\left[\frac{2}{3}x^{3/2}\right]_{0}^{4} - \frac{1}{4}\left[\frac{x^{3}}{3}\right]_{0}^{4}$$

Substituting the limits, we get

$$A = \frac{4}{3} \times 4^{3/2} - \frac{1}{4} \times \frac{4^3}{3}$$
$$= \frac{4}{3} \times 8 - \frac{16}{3} = \frac{16}{3}$$

The standard deviation of a uniformly distributed random variable between 0 and **MCQ 1.26** 1 is GATE ME 2009 TWO MARK $B = \frac{1}{2}$ (A) <u>1</u>

(C)
$$\frac{5}{\sqrt{12}}$$
 (D) $\frac{7}{\sqrt{12}}$

SOL 1.26 Option (A) is correct.

The cumulative distribution function

$$f(x) = \begin{cases} 0, & x \le a \\ \frac{x-a}{b-a}, & a < x < b \\ 0, & x \ge b \end{cases}$$

and density function

$$f(x) = \begin{cases} \frac{1}{b-a}, & a \le x \le b\\ 0, & a > x, x > b \end{cases}$$

Mean

$$E(x) = \sum_{x=a}^{b} xf(x) = \frac{a+b}{2}$$

Variance = $x^2 f(x) - \overline{x}^2 = x^2 f(x) - [xf(x)]^2$

Substitute the value of f(x)

$$= \sum_{x=a}^{b} x^{2} \frac{1}{b-a} dx - \left\{ \sum_{x=a}^{b} x \frac{1}{b-a} dx \right\}^{2}$$

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$$\begin{split} &= \left[\frac{x^3}{3(b-a)}\right]_a^b - \left[\left\{\frac{x^2}{2(b-a)}\right\}_a^b\right]^2 \\ &= \frac{b^3 - a^3}{3(b-a)} - \frac{(b^2 - a^2)^2}{4(b-a)^2} \\ &= \frac{(b-a)(b^2 + ab + a^2)}{3(b-a)} - \frac{(b+a)^2(b-a)^2}{4(b-a)^2} \\ &= \frac{4(b^2 + ab + a^2) + 3(a+b)^2}{12} \\ &= \frac{4(b^2 + ab + a^2) + 3(a+b)^2}{12} \\ &= 4a^2 + 4b^2 + 4ab - 3a^2 - 3b^2 - 6ab/12 \\ &= \frac{(b-a)^2}{12} \\ &= \frac{(b-a)^2}{12} \\ \end{split}$$
Standard deviation = $\sqrt{\text{Variance}} = \sqrt{\frac{(b-a)^2}{12}} \\ &= \frac{(b-a)}{\sqrt{12}} \\ &= \frac{(b-a)}{\sqrt{12}} \\ &\text{Given : } b = 1, a = 0 \\ \text{So, standard deviation} = \frac{1-0}{\sqrt{12}} \\ &= \frac{1}{\sqrt{12}} \\ \text{Consider steady, incompressible and irrotational flow through the set of the s$

MCQ 1.27 GATE ME 2009 TWO MARK

Con gh a reducer in a horizontal pipe where the diameter is reduced from 20 cm to 10 cm. The pressure in the 20 cm pipe just upstream of the reducer is 150 kPa. The fluid has a vapour pressure of 50 kPa and a specific weight of 5 kN/m^3 . Neglecting frictional effects, the maximum discharge $(in m^3/s)$ that can pass through the reducer without causing cavitation is

(A) 0.05	(B) 0.16
(C) 0.27	(D) 0.38

SOL 1.27 Option (B) is correct.

So,



Reducer

Given : $p_V = 50 \text{ kPa}$, $w = 5 \text{ kN/m}^3 = \rho g$

Consider steady, incompressible & irrotational flow & neglecting frictional effect. First of all applying continuity equation at section (1) & (2).

$$egin{aligned} &A_1\,V_1\,=\,A_2\,V_2\ &rac{\pi}{4}(d_1)^2 imes\,V_1\,=rac{\pi}{4}(d_2)^2 imes\,V_2 \end{aligned}$$

Substitute the values of $d_1 \& d_2$, we get

$$\frac{\pi}{4}(20)^2 \times V_1 = \frac{\pi}{4}(10)^2 \times V_2$$

400 V₁ = 100 V₂ \Rightarrow V₂ = 4 V₁ ...(i)

Cavitation is the phenomenon of formation of vapor bubbles of a flowing liquid in a region where the pressure of liquid falls below the vapor pressure $[p_L < p_V]$ So, we can say that maximum pressure in downstream of reducer should be equal or greater than the vapor pressure. For maximum discharge

$$p_V = p_2 = 50 \text{ kPa}$$

Applying Bernoulli's equation at point (1) & (2)

$$\frac{p_1}{\rho g} + \frac{V_1^2}{2g} + z_1 = \frac{p_2}{\rho g} + \frac{V_2^2}{2g} + z_2$$

Here $z_1 = z_2$ for horizontal pipe & $w = \rho g = 5 \text{ kN/m}^2$

$$\frac{150}{5} + \frac{V_1^2}{2g} = \frac{50}{5} + \frac{(4V_1)^2}{2g} \text{ From equation (i) } V_2 = 4V_1$$

$$\frac{150}{5} - \frac{50}{5} = \frac{16V_1^2}{2g} - \frac{V_1^2}{2g} \text{ help}$$

$$20 = \frac{15V_1^2}{2g}$$

$$V_1^2 = \frac{40 \times 9.81}{15} = 5.114 \text{ m/sec}$$

And $V_2 = 4 V_1 = 4 \times 5.114 = 20.46 \text{ m/sec}$ Maximum discharge,

$$\begin{aligned} Q_{\max} &= A_2 V_2 = \frac{\pi}{4} (d_2)^2 V_2 = \frac{\pi}{4} (10 \times 10^{-2})^2 \times 20.46 \\ &= \frac{\pi}{4} \times 10^{-2} \times 20.46 = 0.16 \text{ m}^3/\text{sec} \end{aligned}$$

In a parallel flow heat exchanger operating under steady state, the heat capacity rates (product of specific heat at constant pressure and mass flow rate) of the hot and cold fluid are equal. The hot fluid, flowing at 1 kg/s with $c_p = 4 \text{ kJ/kg K}$, enters the heat exchanger at 102° C while the cold fluid has an inlet temperature of 15° C. The overall heat transfer coefficient for the heat exchanger is estimated to be 1 kW/m^2 K and the corresponding heat transfer surface area is 5 m^2 . Neglect heat transfer between the heat exchanger and the ambient. The heat exchanger is characterized by the following relations:

$$2\varepsilon = -\exp\left(-2\,\mathrm{NTU}\right)$$

The exit temperature (in $^{\circ}$ C) for the cold fluid is

(A) 45	(B) 55
(C) 65	(D) 75

SOL 1.28 Option (B) is correct.

Given : $\dot{C}_h = \dot{C}_c$, $\dot{m}_h = 1 \text{ kg/sec}$, $c_{ph} = 4 \text{ kJ/kg K}$, $t_{h1} = 102^{\circ} \text{ C}$, $t_{c1} = 15^{\circ} \text{ C}$ $U = 1 \text{ kW/m}^2 \text{ K}$, $A = 5 \text{ m}^2$

The figure shown below is for parallel flow.



$$\dot{C}_h = \dot{m}_h c_{ph} = 4 ext{ kJ/sK}$$

The heat exchanger is characterized by the following relation,

$$\varepsilon = \frac{1 - \exp\left(-2NTU\right)}{2} \qquad \dots (i)$$

For parallel flow heat exchanger effectiveness is given by

$$\varepsilon = \frac{1 - \exp\left[-\operatorname{NTU}\left(1 + C\right)\right]}{1 + C} \qquad \dots (\mathrm{ii})$$

On comparing equation (i) and equation (ii), we get capacity ratio

$$C = \frac{C_c}{C_h} = \frac{C_{\min}}{C_{\max}} = 1 \qquad \dots (\text{iii})$$

On applying energy balance for a parallel flow

$$C_{h}(t_{h1} - t_{h2}) = C_{c}(t_{c2} - t_{c1})$$

$$\frac{C_{c}}{C_{h}} = \frac{t_{h1} - t_{h2}}{t_{c2} - t_{c1}} = 1$$

From equation(iii)

 $t_{h1} - t_{h2} = t_{c2} - t_{c1}$

Number of transfer units is given by,

NTU =
$$\frac{UA}{C_{\min}} = \frac{1 \times 5}{4} = 1.25$$

Effectiveness, $\varepsilon = \frac{1 - \exp(-2 \times 1.25)}{2} = \frac{1 - 0.0820}{2} = 0.46$

Maximum possible heat transfer is,

$$Q_{\max} = C_{\min}(t_{h1} - t_{c1})$$

= 4 × [(273 + 102) - (273 + 15)] = 348 kW

But Actual Heat transfer is,

$$Q_a = \varepsilon Q_{\text{max}} = 0.46 \times 348 = 160 \,\text{kW}$$

And

$$egin{aligned} Q_a &= C_c (t_{c2} - t_{c1}) \ 160 &= 4 \, (t_{c2} - 15) \ t_{c2} &= 40 + 15 = 55\,^\circ \mathrm{C} \end{aligned}$$

In an air-standard Otto-cycle, the compression ratio is 10. The condition at the **MCQ 1.29** beginning of the compression process is 100 kPa and 27°C . Heat added at constant GATE ME 2009 TWO MARK volume is 1500 kJ/kg, while 700 kJ/kg of heat is rejected during the other constant volume process in the cycle. Specific gas constant for air = 0.287 kJ/kgK. The mean effective pressure (in kPa) of the cycle is (A) 103 (B) 310 (D) 1032 (C) 515 **SOL 1.29** Option (D) is correct. Given : r = 10, $p_1 = 100 \text{ kPa}$, $T_1 = 27^{\circ} \text{C} = (27 + 273) \text{ K} = 300 \text{ K}$ $Q_s = 1500 \text{ kJ/kg}, Q_r = 700 \text{ kJ/kg}, R = 0.287 \text{ kJ/kg K}$ Mean Effective pressure $p_m = rac{ ext{Net work output}}{ ext{Swept Volume}}$...(i) $\nu_1 - \nu_2 = \nu_2(r-1)$ Swept volume, where $\nu_1 = \text{Total volume and } \nu_2 = \text{Clearance volume}$ Applying gas equation for the beginning process, $\nu_1 = 10 \mathbf{C} \Rightarrow \nu_1 = 10 v_2$...(ii) $p_1\nu_1 = RT_1$ $\nu_1 = \frac{RT_1}{p_1} = \frac{0.287 \times 300}{100} = 0.861 \text{ m}^3/\text{kg}$ $\nu_2 = \frac{\nu_1}{10} = \frac{0.861}{10} = 0.0861 \text{ m}^3/\text{kg}$ $W_{net} = Q_s - Q_r$ $= (1500 - 700) \, \text{kJ/kg K} = 800 \, \text{kJ/kg K}$ From equation (i) $p_m = \frac{800}{\nu_2(r-1)} = \frac{800}{0.0861(10-1)}$ $=\frac{800}{0.7749}=1032.391 \text{ kPa} \simeq 1032 \text{ kPa}$ An irreversible heat engine extracts heat from a high temperature source at a rate **MCQ 1.30**

GATE ME 2009 TWO MARK An irreversible heat engine extracts heat from a high temperature source at a rate of 100 kW and rejects heat to a sink at a rate of 50 kW. The entire work output of the heat engine is used to drive a reversible heat pump operating between a set of independent isothermal heat reservoirs at 17° C and 75° C. The rate (in kW) at which the heat pump delivers heat to its high temperature sink is (A) 50 (B) 250

(\mathbf{A})	50	(D)	200	
(C)	300	(D)	360	

SOL 1.30 Option (C) is correct.





We know that coefficient of performance of a Heat pump for the given system is,

$$(COP)_{H.P.} = \frac{Q_3}{Q_3 - Q_4} = \frac{Q_3}{W}$$

For a reversible process,

$$\frac{Q_3}{Q_4} = \frac{T_3}{T_4}$$

$$(COP)_{H.P.} = \frac{T_3}{T_3 - T_4} = \frac{Q_3}{W}$$

$$\frac{348}{348 - 290} = \frac{Q_3}{50}$$

$$Q_3 = \frac{348 \times 50}{58} = 300 \text{ K}$$

MCQ 1.31You are asked to evaluate assorted fluid flows for their suitability in a given
laboratory application. The following three flow choices, expressed in terms of the
two dimensional velocity fields in the xy-plane, are made available.

$$\mathsf{P}: \quad u = 2y, \, v = -3x$$

 $Q: \quad u = 3xy, \, v = 0$

 $\mathbf{R}: \quad u = -2x, \, v = 2y$

Which flow(s) should be recommended when the application requires the flow to be incompressible and irrotational ?

(A) P and R	(B) Q

- (C) Q and R (D) R
- **SOL 1.31** Option (D) is correct. Given : P: u = 2y, V = -3x
 - Q: u = 3xy, V = 0
 - \mathbf{R} : u = -2x, V = 2y
 - For incompressible fluid.

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \qquad \dots (i)$$

For irrotational flow $\zeta_z = 0$,

$\zeta_z = rac{1}{2} \Bigl(rac{\partial v}{\partial x} - rac{\partial u}{\partial y} \Bigr)$	
$\frac{1}{2} \left(\frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right) = 0$	
$\frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} = 0$	(ii)
From equation (i) & (ii), check P, Q & R	
For P: $u = 2y$ $v = -3x$	
$\frac{\partial u}{\partial x} = 0 \qquad \qquad \frac{\partial v}{\partial y} = 0$	
$\frac{\partial v}{\partial x} = -3 \qquad \frac{\partial u}{\partial y} = 2$	
$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \Rightarrow \ 0 + 0 = 0$	(Flow is incompressible)
Or, $\frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} = 0$	
$-3 - 2 = 0 \Rightarrow -5 \neq 0$	(Rotational flow)
For Q: $u = 3xy$ $v = 0$ ∂u ∂v	
$\frac{\partial u}{\partial x} = 3y$ $\frac{\partial v}{\partial y} = 0$	
For Q: $ \begin{array}{ccc} -3-2 = 0 \Rightarrow -5 \neq 0 \\ u = 3xy & v = 0 \\ \frac{\partial u}{\partial x} = 3y & \frac{\partial v}{\partial y} = 0 \\ \frac{\partial v}{\partial x} = 0 & \frac{\partial u}{\partial y} = 3x \end{array} $	
$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \Rightarrow 3y \neq 0$	(Compressible flow)
Or, $\frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} = 0$	
$0 - 3x = 0 \Rightarrow -3x \neq 0$	(Rotational flow)
For R: $u = -2x$ $v = 2y$	× × ×
$\frac{\partial u}{\partial x} = -2 \qquad \qquad \frac{\partial v}{\partial y} = 2$	
$\frac{\partial v}{\partial x} = 0 \qquad \qquad \frac{\partial u}{\partial y} = 0$	
$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0$	
$-2+2=0 \Rightarrow \ 0=0$	(Incompressible flow)
Or, $\frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} = 0$	
$0 - 0 = 0 \Rightarrow 0 = 0$	(Irrotational flow)

So, we can easily see that R is incompressible & irrotational flow.

MCQ 1.32 GATE ME 2009 TWO MARK Water at 25° C is flowing through a 1.0 km long. G.I. pipe of 200 mm diameter at the rate of $0.07 \text{ m}^3/\text{s}$. If value of Darcy friction factor for this pipe is 0.02 and density of water is 1000 kg/m^3 , the pumping power (in kW) required to maintain

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the flow is	
(A) 1.8	(B) 17.4
(C) 20.5	(D) 41.0

SOL 1.32 Option (A) is correct. Given : L = 1 km = 1000 m, D = 200 mm = 0.2 m, $Q = 0.07 \text{ M}^3/\text{sec}$ $f = 0.02, \ \rho = 1000 \text{ kg/m}^3$ Head loss is given by,

$$h_{f} = \frac{fLV^{2}}{D \times 2g} = \frac{fL}{D \times 2g} \left(\frac{4Q}{\pi D^{2}}\right)^{2} \qquad \qquad Q = \frac{\pi D^{2}}{4} \times V$$
$$= \frac{16fLQ^{2}}{\pi^{2}D^{5} \times 2g} = \frac{8fLQ^{2}}{\pi^{2}D^{5}g}$$
$$= \frac{8 \times 0.02 \times 1000 \times (0.07)^{2}}{(3.14)^{2} \times (0.2)^{5} \times (9.81)} = \frac{0.784}{0.30} = 2.61 \,\mathrm{m} \text{ of water}$$

Pumping power required,

$$P = \rho g Q \times h_f = 1000 \times 9.81 \times 0.07 \times 2.61$$

= 1752.287 = 1.752 kW \approx 1.8 kW





Given: $h_i = 20 \text{ W/m}^2 \text{K}$, $h_o = 50 \text{ W/m}^2 \text{K}$; $T_{\infty,i} = 20^{\circ} \text{C}$; $T_{\infty,o} = -2^{\circ} \text{C}$, $k_1 = 20 \text{ W/mK}$; ; $k_2 = 50 \text{ W/mK}$; $L_1 = 0.30 \text{ m}$ and $L_2 = 0.15 \text{ m}$. Assuming negligible contact resistance between the wall surfaces, the interface temperature, T (in $^{\circ}$ C), of the two walls will be

(A) - 0.50	(B) 2.75

(C)
$$3.75$$
 (D) 4.50

SOL 1.33 Option (C) is correct.

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The equivalent resistance diagram for the given system is,

Η

condition,

$$q = \frac{T_{\infty_i} - T_{\infty_o}}{AR_{eq}} = h_i (T_{\infty_i} - T_1)$$

$$= \frac{k_1 (T_1 - T)}{L_1} = \frac{k_2 (T - T_2)}{L_2} \qquad \dots (i)$$

$$q = \frac{T_{\infty i} - T_{\infty o}}{AR_{eq}} = \frac{20 - (-2)}{0.088} = 250 \text{ W/m}^2 \qquad \dots (\text{ii})$$

$$q = \frac{T_{\infty_i} - T_1}{\frac{1}{h_i}} = \frac{20 - T_1}{\frac{1}{20}}$$
 From equation(i)

$$250 = 20(20 - T_1)$$

12.5 = 20 - T₁ \Rightarrow T₁ = 20 - 12.5 = 7.5° C

Again from equation(i),

$$q = \frac{k_1(T_1 - T)}{L_1}$$

250 = $\frac{20}{0.3}(7.5 - T)$
3.75 = 7.5 - T \Rightarrow T = 3.75° C

Alternate :

Brought to you by: Nodia and Company PUBLISHING FOR GATE Under steady state conditions,

Heat flow from I to interface wall = Heat flow from interface wall to O

$$\frac{(T_{\infty,i} - T)}{\frac{1}{h_i A} + \frac{L_1}{k_1 A}} = \frac{(T - T_{\infty,o})}{\frac{L_2}{k_2 A} + \frac{1}{h_0 A}}$$
$$\frac{T_{\infty,i} - T}{\frac{1}{h_i} + \frac{L_1}{k_1}} = \frac{T - T_{\infty,o}}{\frac{L_2}{k_2} + \frac{1}{h_o}}$$
$$\frac{(20 - T)}{\frac{1}{20} + \frac{0.3}{20}} = \frac{T - (-2)}{\frac{0.15}{50} + \frac{1}{50}}$$
$$\frac{(20 - T)}{\frac{1.3}{20}} = \frac{T + 2}{\frac{1.15}{50}}$$
$$(20 - T) = 2.826 (T + 2) = 2.826 T + 5.652$$
$$T = \frac{14.348}{3.826} = 3.75^{\circ} C$$

MCQ 1.34 GATE ME 2009 TWO MARK

$$u(r) = -\frac{R^2}{4\mu} \left(\frac{dp}{dx}\right) \left(1 - \frac{r^2}{R^2}\right)$$

shown in the figure, is given by the expression

Where $\frac{dp}{dx}$ is a constant. The average velocity of fluid in the pipe is

The velocity profile of a fully developed laminar flow in a straight circular pipe, as



SOL 1.34

Option (A) is correct.



$$u(r) = -\frac{R^2}{4\mu} \left(\frac{dp}{dx}\right) \left(1 - \frac{r^2}{R^2}\right)$$

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Therefore, the velocity profile in fully developed laminar flow in a pipe is parabolic with a maximum at the center line and minimum at the pipe wall.

The average velocity is determined from its definition,

$$\begin{split} V_{avg} &= \int_{0}^{R} u(r) \, r dr \\ &= -\frac{2}{R^{2}} \int_{0}^{R} \frac{R^{2}}{4\mu} \left(\frac{dp}{dx}\right) \left(1 - \frac{r^{2}}{R^{2}}\right) r dr \\ &= -\frac{1}{2\mu} \left(\frac{dp}{dx}\right) \int_{0}^{R} \left(r - \frac{r^{3}}{R^{2}}\right) dr \\ &= -\frac{1}{2\mu} \left(\frac{dp}{dx}\right) \left[\frac{r^{2}}{2} - \frac{r^{4}}{4R^{2}}\right]_{0}^{R} = -\frac{1}{2\mu} \left(\frac{dp}{dx}\right) \left[\frac{R^{2}}{2} - \frac{R^{4}}{4R^{2}}\right] \\ &= -\frac{1}{2\mu} \left(\frac{dp}{dx}\right) \times \frac{R^{2}}{4} = -\frac{R^{2}}{8\mu} \left(\frac{dp}{dx}\right) \end{split}$$

Alternate Method

Now we consider a small element (ring) of pipe with thickness dr & radius r. We find the flow rate through this elementry ring.

$$dQ = (2\pi r) \times dr \times u(r)$$
 Put the value of $u(r)$
$$dQ = (2\pi r) \times dr \times \left(-\frac{R^2}{4\mu}\right) \left(\frac{dp}{dx}\right) \left(1 - \frac{r^2}{R^2}\right)$$

Now for total discharge integrate both the rides within limit. $Q \Rightarrow 0$ to Q and $R \Rightarrow 0$ to R

 So

$$\int_{0}^{Q} dQ = -2\pi \frac{R^{2}}{4\mu} \left(\frac{dp}{dx}\right) \int_{0}^{R} r \left(1 - \frac{r^{2}}{R^{2}}\right) dr$$
$$[Q]_{0}^{Q} = -2\pi \frac{R^{2}}{4\mu} \left(\frac{dp}{dx}\right) \left[\frac{r^{2}}{2} - \frac{r^{4}}{4R^{2}}\right]_{0}^{R}$$

Now put the limits

Then

$$Q = -2\pi \frac{R^2}{4\mu} \left(\frac{dp}{dx}\right) \left[\frac{R^2}{2} - \frac{R^4}{4R^2}\right]$$
$$Q = -2\pi \frac{R^2}{4\mu} \left(\frac{dp}{dx}\right) \left[\frac{R^2}{2} - \frac{R^2}{4}\right]$$
$$Q = -2\pi \left(\frac{R^2}{4\mu}\right) \left(\frac{dp}{dx}\right) \left[\frac{R^2}{4}\right]$$
$$Q = -\frac{\pi R^4}{8\mu} \left(\frac{dp}{dx}\right)$$

Now

$$egin{aligned} Q &= ext{Area} imes ext{Average velocity} \ &= A imes V_{avg.} \ V_{avg.} &= rac{Q}{A} = rac{-\pi R^4}{8\mu} \Big(rac{dp}{dx}\Big) imes rac{1}{\pi R^2} \end{aligned}$$

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$$V_{avg.} = -rac{R^2}{8\mu} \Big(rac{dp}{dx}\Big)$$



First, the shaft is divided in two parts (1) & (2) and gives a twisting moment T_1 (in counter-clockwise direction) & T_2 (in clock wise direction) respectively.

By the nature of these twisting moments, we can say that shafts are in parallel combination.

So,	$T_0=T_1\!+T_2$	(i)
From the torsi	ional equation,	
	$\frac{T}{J} = \frac{\tau}{r} = \frac{G\theta}{l} \Rightarrow T = \frac{GJ\theta}{l}$	
But, here	$G_1 = G_2$	
	$ heta_1= heta_2$	For parallel connection
	$J_1 = J_2$	Diameter is same
So,	$T_1 l_1 = T_2 l_2$	
2	$T_1 imes rac{L}{4} = T_2 imes rac{3L}{4}$	
Now, From eq	$T_1 = 3 T_2$ uation (i), $T_0 = 3 T_2 + T_2 = 4 T_2$	
	$T_2=rac{T_0}{4}$	

And

 $T_1 = \frac{3T_0}{4}$

 $T_1 > T_2$

Here

So, maximum shear stress is developed due to T_1 ,

$$rac{T_1}{J} = rac{ au_{ ext{max}}}{r} \Rightarrow au_{ ext{max}} = rac{T_1}{J} imes r$$

Substitute the values, we get

$$au_{
m max} = rac{\left(rac{3\,T_0}{4}
ight)}{rac{\pi}{32}\,d^4} imes rac{d}{2} = rac{32 imes 3\,T_0}{8\pi imes d^3} = rac{12\,T_0}{\pi d^3}$$

MCQ 1.36 GATE ME 2009 TWO MARK An epicyclic gear train in shown schematically in the given figure. The run gear 2 on the input shaft is a 20 teeth external gear. The planet gear 3 is a 40 teeth external gear. The ring gear 5 is a 100 teeth internal gear. The ring gear 5 is fixed and the gear 2 is rotating at 60 rpm CCW (CCW=counter-clockwise and CW=clockwise).



The arm 4 attached to the output shaft will rotate at

(A) 10 rpm CCW	(B) 10 rpm CW
(C) 12 rpm CW	(D) 12 rpm CCW





Given $Z_2 = 20$ Teeth, $Z_3 = 40$ Teeth, $Z_5 = 100$ Teeth, $N_5 = 0$, $N_2 = 60$ rpm (CCW) If gear 2 rotates in the CCW direction, then gear 3 rotates in the clockwise direction. Let, Arm 4 will rotate at N_4 rpm. The table of motions is given below

Take CCW = +ve, CW = -ve

S.	Condition of Motion	Revolution of elements			5
No.		Sun Gear 2	Planet Gear 3	Arm 4	Ring Gear 5
		N_2	N_3	N_4	N_5
1.	Arm fixed and sun gear 2 rotates $+1 \text{ rpm}$ (CCW)	+1	$-rac{Z_2}{Z_3}$	0	$-rac{Z_2}{Z_3} imesrac{Z_3}{Z_5}$
2.	Give $+x$ rpm to gear 2 (CCW)	+x	$-\frac{Z_2}{Z_3}x$	0	$-x\frac{Z_2}{Z_5}$
3.	Add $+y$ revolutions to all elements	+y	+y	+y	+y
4.	Total motion.	y + x	$y - x \frac{Z_2}{Z_3}$	+y	$y - x \frac{Z_2}{Z_5}$

Note : Speed ratio = $\frac{\text{Speed of driver}}{\text{Speed of driven}} = \frac{\text{No. of teeth on dirven}}{\text{No. of teeth on driver}}$

Ring gear 5 is fixed. So,

$$y - x \frac{Z_2}{Z_5} = 0$$
 Gate

$$y = \frac{Z_2}{Z_5} x = \frac{20}{100} x \frac{125}{5}$$
 From the table

$$\dots (i)$$

$$N_2 = 60 \text{ rpm (CCW)}$$

Given,

From table

 $x = 10 \times 5 = 50 \,\mathrm{rpm}$

And from equation (i),

$$y = \frac{50}{5} = 10 \operatorname{rpm}(\operatorname{CCW})$$

From the table the arm will rotate at $N_4 = y = 10 \text{ rpm} (\text{CCW})$

y + x = 60

 $\frac{x}{5} + x = 60$

MCQ 1.37 GATE ME 2009 TWO MARK A forged steel link with uniform diameter of 30 mm at the centre is subjected to an axial force that varies from 40 kN in compression to 160 kN in tension. The tensile (S_u) , yield (S_y) and corrected endurance (S_e) strengths of the steel material are 600 MPa, 420 MPa and 240 MPa respectively. The factor of safety against fatigue endurance as per Soderberg's criterion is

(A) 1.26	(B) 1.37
(C) 1.45	(D) 2.00

SOL 1.37 Option (A) is correct. Given : S_u or $\sigma_u = 600$ MPa, S_y or $\sigma_y = 420$ MPa, S_e or $\sigma_e = 240$ MPa, d = 30 mm $F_{\text{max}} = 160$ kN (Tension), $F_{\text{min}} = -40$ kN (Compression) Maximum stress, $\sigma_{\text{max}} = \frac{F_{\text{max}}}{A} = \frac{160 \times 10^3}{\frac{\pi}{4}(30)^2} = 226.47$ MPa

Minimum stress,
$$\sigma_{\min} = \frac{F_{\min}}{A} = -\frac{40 \times 10^3}{\frac{\pi}{4} \times (30)^2} = -56.62 \text{ MPa}$$

Mean stress, $\sigma_m = \frac{\sigma_{\max} + \sigma_{\min}}{2} = \frac{226.47 - 56.62}{2} = 84.925 \text{ MPa}$
Variable stress, $\sigma_v = \frac{\sigma_{\max} - \sigma_{\min}}{2} = \frac{226.47 - (-56.62)}{2} = 141.545$

le stress,
$$\sigma_v = \frac{\sigma_{\text{max}} - \sigma_{\text{min}}}{2} = \frac{220.47 - (-50.02)}{2} = 141.545 \,\text{MPa}$$

From the Soderberg's criterion,

$$\frac{1}{F.S.} = \frac{\sigma_m}{\sigma_y} + \frac{\sigma_v}{\sigma_e}$$
$$\frac{1}{F.S.} = \frac{84.925}{420} + \frac{141.545}{240} = 0.202 + 0.589 = 0.791$$
$$F.S. = \frac{1}{0.791} = 1.26$$

So,

MCQ 1.38 GATE ME 2009 TWO MARK
An automotive engine weighing 240 kg is supported on four springs with linear characteristics. Each of the front two springs have a stiffness of 16 MN/m while the stiffness of each rear spring is 32 MN/m. The engine speed (in rpm), at which resonance is likely to occur, is (A) 6040
(B) 3020

(A) 6040	(B) 3020
(C) 1424	(D) 955

SOL 1.38 Option (A) is correct.



Given $k_1 = k_2 = 16 \text{ MN/m}$, $k_3 = k_4 = 32 \text{ MN/m}$, m = 240 kgHere, $k_1 \& k_2$ are the front two springs or k_3 and k_4 are the rear two springs. These 4 springs are parallel, So equivalent stiffness

 $k_{eq} = k_1 + k_2 + k_3 + k_4 = 16 + 16 + 32 + 32 = 96 \text{ MN/m}^2$

We know at resonance

$$\begin{split} \omega &= \omega_n = \sqrt{\frac{k}{m}} \\ \frac{2\pi N}{60} &= \sqrt{\frac{k_{eq}}{m}} \\ N &= \text{Engine speed in rpm} \\ N &= \frac{60}{2\pi} \sqrt{\frac{k_{eq}}{m}} = \frac{60}{2\pi} \sqrt{\frac{96 \times 10^6}{240}} \\ &= \frac{60}{2\pi} \times 10^2 \times \sqrt{40} = 6042.03 \simeq 6040 \text{ rpm} \end{split}$$
MCQ 1.39
A vehicle suspension system consists of a spring and a damper. The stiffness of the spring is 3.6 kN/m and the damping constant of the damper is 400 Ns/m. If the mass is 50 kg, then the damping factor (d) and damped natural frequency (f_n) , respectively, are

- (C) 0.666 and 1.35 Hz (D) 0.666 and 8.50 Hz
- **SOL 1.39** Option (A) is correct. Given k = 3.6 kN/m, c = 400 Ns/m, m = 50 kgWe know that, Natural Frequency $\omega_n = \sqrt{\frac{k}{2}} = \sqrt{\frac{3.6 \times 1000}{200}} = 8.485 \text{ rad/sec}$

$$\omega_n = \sqrt{\frac{n}{m}} = \sqrt{\frac{3.0 \times 1000}{50}} = 8.485 \text{ rad/sec} \qquad \dots(i)$$
And damping factor is given by,
$$d \text{ or } c = \frac{c}{c} \qquad c \qquad 400$$

d or
$$\varepsilon = \frac{c}{c_c} = \frac{c}{2\sqrt{km}} = \frac{100}{2 \times \sqrt{3.6 \times 1000 \times 50}}$$
$$= \frac{400}{2 \times 424.26} = 0.471$$

Damping Natural frequency,

$$\begin{split} \omega_d &= \sqrt{1 - \varepsilon^2} \, \omega_n \\ 2\pi f_d &= \sqrt{1 - \varepsilon^2} \, \omega_n \\ f_d &= \frac{\omega_n}{2\pi} \times \sqrt{1 - \varepsilon^2} \\ &= \frac{8.485}{2 \times 3.14} \times \sqrt{1 - (0.471)^2} = 1.19 \, \text{Hz} \end{split}$$

MCQ 1.40A frame of two arms of equal length L is shown in the adjacent figure. The flexuralGATE ME 2009
TWO MARKrigidity of each arm of the frame is EI. The vertical deflection at the point of
application of load P is



X

x

SOL 1.40

Y - - -

We have to take sections XX and YY along the arm BC and AB respectively and find the total strain energy.

So, Strain energy in arm BC is,

LX

y

В

$$U_{BC} = \int_{0}^{L} \frac{M_x^2}{2EI} dx = \int_{0}^{L} \frac{(Px)^2}{2EI} dx \qquad \qquad M_x = P \times x$$

Integrating the equation and putting the limits, we get

$$U_{BC} = \frac{P^2}{2EI} \left[\frac{x^3}{3}\right]_0^L = \frac{P^2 L^3}{6EI}$$

C

Similarly for arm AB, we have

$$U_{AB} = \int_{0}^{L} \frac{M_{y}^{2}}{2EI} dy = \int_{0}^{L} \frac{P^{2}L^{2}}{2EI} dy \qquad \qquad M_{y} = P \times L$$

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Integrating the above equation and putting the limit, we get

$$U_{AB} = \frac{P^2 L^3}{2EI}$$

So, total strain energy stored in both the arms is,

$$U = U_{AB} + U_{BC}$$

= $\frac{P^2 L^3}{2EI} + \frac{P^2 L^3}{6EI} = \frac{2P^2 L^3}{3EI}$

From the Castigliano's theorem, vertical deflection at point A is,

$$\delta_A = \frac{\delta U}{\delta P}$$
$$\delta_A = \frac{\delta}{\delta P} \left(\frac{2P^2 L^3}{3EI}\right) = \frac{4PL^3}{3EI}$$

MCQ 1.41 A uniform rigid rod of mass M and length L is hinged at one end as shown in the adjacent figure. A force P is applied at a distance of 2L/3 from the hinge so that the rod swings to the right. The reaction at the hinge is



SOL 1.41 Option (B) is correct.



When rod swings to the right, linear acceleration a and angular acceleration α comes in action.

Centre of gravity (G) acting at the mid-point of the rod. Let R be the reaction at the hinge.

Linear acceleration

$$a = r.\alpha = \frac{L}{2} \times \alpha$$
$$\alpha = \frac{2a}{L} \qquad \dots (i)$$

And about point G, for rotational motion

$$\sum M_{G} = I_{G} \times \alpha$$

$$R\left(\frac{L}{2}\right) + P\left(\frac{L}{6}\right) = \frac{ML^{2}}{12}\left(\frac{2a}{L}\right)$$
From equation (i)
$$R + \frac{P}{3} = \frac{Ma}{3}$$

$$a = \frac{3R}{M} + \frac{P}{M}$$
...(ii)

By equilibrium of forces in normal direction to the rod

$$\sum F_m = 0$$

$$P - R = Ma = M \left(\frac{3R}{M} + \frac{P}{M} \right)$$
From equation (ii)
$$P - R = 3R + P$$

$$R = 0$$

 \Rightarrow

So, reaction at the hinge is zero.

MCQ 1.42Match the approaches given below to perform stated kinematics/dynamics analysisGATE ME 2009
TWO MARKof machine.

Analysis

Approach

- **P.** Continuous relative rotation
- **Q.** Velocity and acceleration
- **R.** Mobility

- **1.** D' Alembert's principle
- **2.** Grubler's criterion
- **3.** Grashoff's law

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	 S. Dynamic-static analysis (A) P-1, Q-2, R-3, S-4 (C) P-2, Q-3, R-4, S-1 	 4. Kennedy's theorem (B) P-3, Q-4, R-2, S-1 (D) P-4, Q-2, R-1, S-3 	m
SOL 1.42	Option (B) is correct.		
	Analysis	Approach	
	P. Continuous relative rotation	3. Grashoff law	
	Q. Velocity and Acceleration	4. Kennedy's Theo	orem

- **2.** Grubler's Criterion
- **1.** D'Alembert's Principle
- So, correct pairs are P-3, Q-4, R-2, S-1

Dynamic-static Analysis

MCQ 1.43 A company uses 2555 units of an item annually. Delivery lead time is 8 days. The reorder point (in number of units) to achieve optimum inventory is



In figure,

R.

S.

Mobility

ROP = Reorder pointLT = Lead Time = 8 daysTT = Total Time = 365 daysq = stock level = 2555 units

Let the reorder quantity be xNow from the similar triangles $\triangle ABC \& \triangle BDE$

$$\frac{q}{TT} = \frac{x}{LT}$$
\Rightarrow

$$\frac{2555}{365} = \frac{x}{8}$$
$$x = \frac{2555}{365} \times 8 = 56$$
 Units

Alternate method

Given,

Demand in a year D = 2555 Units Lead time T = 8 days Now, Number of orders to be placed in a year $N = \frac{\text{Number. of days in a year}}{\text{Lead Time}}$ $= \frac{365}{8}$ orders

Now, quantity ordered each time or reorder point.

$$Q = \frac{\text{Demand in a years}}{\text{Number of orders}}$$
$$= \frac{2555}{\underline{365}} = 56 \text{ Units}$$

MCQ 1.44Consider the following Linear Programming Problem (LPP):GATE ME 2009
TWO MARKMaximize
Subject to
 $x_1 \leq 4$
 $x_2 \leq 6$
 $3x_1 + 2x_2 \leq 18$
 $x_1 \geq 0, x_2 \geq 0$

(A) The LPP has a unique optimal solution

- (B) The LPP is infeasible.
- (C) The LPP is unbounded.
- (D) The LPP has multiple optimal solutions.
- **SOL 1.44** Option (D) is correct. Given Objective function

 $Z_{\rm max} = 3x_1 + 2x_2$

and constraints are

 $x_1 \le 4$...(i) $x_2 \le 6$...(ii)

$$3x_1 + 2x_2 \le 18 \qquad \dots (iii)$$
$$x_1 \ge 0$$
$$x_2 \ge 0$$

Plot the graph from the given constraints and find the common area.

(E is the intersection point of equation. (ii) & (iii))



Now, we find the point of intersection E & F. $3x_1 + 2x_2 = 18$ For E,

 $x_2 = 6$

 $x_1 = 2$

 $x_1 = 4$

 $3x_1 + 12 = 18$

 $3x_1 + 2x_2 = 18$

So,

For F,

 $3 \times 4 + 2x_2 = 18$ So, Hence, E(2,6) or F(4,3)Now at point E(2,6) $Z = 3 \times 2 + 2$ = 18At point F(4,3)

 $Z = 3 \times 4 + 2 \times 3$ = 18

The objective function and the constraint (represent by equation (iii)) are equal. Hence, the objective function will have the multiple solutions as at point E & F, the value of objective function $(Z = 3x_1 + 2x_2)$ is same.

Six jobs arrived in a sequence as given below:

GATE ME 2009	
TWO MARK	

Jobs	Processing Time (days)
Ι	4
II	9
III	5
IV	10
V	6
VI	8

Average flow time (in days) for the above jobs using Shortest Processing time rule is

(A) 20.83	(B) 23.16
(C) 125.00	(D) 139.00

SOL 1.45 Option (A) is correct.

> In shortest processing time rule, we have to arrange the jobs in the increasing order of their processing time and find total flow time. So, job sequencing are I - III - V - VI - II - IV

Jobs	Processing Time (days)	Flow time (days)
Ι	4	4
III	5	4 + 5 = 9
V	6	9 + 6 = 15
VI	8	15 + 8 = 23
II	9	23 + 9 = 32
IV	10	32 + 10 = 42

Now Total flow time
$$T = 4 + 9 + 15 + 23 + 32 + 42$$

= 125
Average flow time = $\frac{\text{Total flow time}}{\text{Number of jobs}}$
 $T_{average} = \frac{125}{6}$

 $= 20.83 \,\mathrm{days}$

Minimum shear strain in orthogonal turning with a cutting tool of zero rake angle **MCQ 1.46** GATE ME 2009 is TWO MARK

(A) 0.0	(B) 0.5
(C) 1.0	(D) 2.0

SOL 1.46 Option (D) is correct. Given : $\alpha = 0^{\circ}$

We know that, shear strain

$$s = \cot \phi + \tan \left(\phi - \alpha \right) \qquad \qquad \alpha = 0^{\circ}$$

So. $s = \cot \phi + \tan \phi$

For minimum value of shear strain differentiate equation (i) w.r.t. ϕ

$$\frac{ds}{d\phi} = \frac{d}{d\phi}(\cot\phi + \tan\phi) = -\csc^2\phi + \sec^2\phi \qquad \dots (ii)$$

Again differentiate w.r.t. to ϕ ,

$$\frac{d^2s}{d\phi^2} = -2\operatorname{cosec}\phi \times (-\operatorname{cosec}\phi\cot\phi) + 2\operatorname{sec}\phi \times (\operatorname{sec}\phi\tan\phi) \\ = +2\operatorname{cosec}^2\phi\cot\phi + 2\operatorname{sec}^2\phi\tan\phi \qquad \dots \dots (\text{iii})$$

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...(i)

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Using the principle of minima - maxima and put $\frac{ds}{d\phi}=0$ in equation(ii) $-\csc^2 + \sec^2 \phi = 0$ $-\frac{1}{\sin^2\phi} + \frac{1}{\cos^2\phi} = 0$ $\frac{\cos^2\phi-\sin^2\phi}{\sin^2\phi\times\cos^2\phi}=0$ $\cos^2\phi - \sin^2\phi = 0$

$$\cos 2\phi = 0$$

$$2\phi = \cos^{-1}(0) = \frac{\pi}{2}$$

$$\phi = \frac{\pi}{4}$$

From equation (iii), at $\phi = \frac{\pi}{4}$

$$\begin{pmatrix} \frac{d^2s}{d\phi^2} \\ \phi = \frac{\pi}{4} \end{pmatrix}_{\phi = \frac{\pi}{4}} = 2 \operatorname{cosec}^2 \frac{\pi}{4} \times \cot \frac{\pi}{4} + 2 \operatorname{sec}^2 \frac{\pi}{4} \tan \frac{\pi}{4} \\ \left(\frac{d^2s}{d\phi^2} \right)_{\phi = \frac{\pi}{4}} = 2 \times 2 \times 1 + 2 \times 2 \times 1 = 8 \\ \left(\frac{d^2s}{d\phi^2} \right)_{\phi = \frac{\pi}{4}} > 0 \quad \mathbf{1} \quad \mathbf{e}$$

Electrochemical machining is performed to remove material from an iron surface of

Therefore it is minimum at $\phi = \frac{\pi}{4}$, so from equation (i),

$$(s)_{\min} = \cot\frac{\pi}{4} + \tan\frac{\pi}{4} = 1 + 1 = 2$$

MCQ 1.47 GATE ME 2009

20 mm \times 20 mm under the following conditions : TWO MARK Inter electrode gap = 0.2 mmSupply voltage (DC) = 12 VSpecific resistance of electrolyte = 2Ω cm Atomic weight of Iron = 55.85Valency of Iron = 2Faraday's constant = 96540 Coulombs The material removal rate (in g/s) is (A) 0.3471 (B) 3.471 (C) 34.71 (D) 347.1 SOL 1.47 Option (A) is correct. Given : L = 0.2 mm, $A = 20 \text{ mm} \times 20 \text{ mm} = 400 \text{ mm}^2$, V = 12 Volt $\rho = 2 \Omega \text{cm} = 2 \times 10 \Omega \text{ mm}, Z = 55.85, v = 2, F = 96540$ Coulombs We know that Resistance is given by the relation

$$R = \frac{\rho L}{A} = \frac{2 \times 10 \times 0.2}{20 \times 20} = 0.01 \,\Omega$$

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		$I = \frac{V}{R} = \frac{12}{0.01} = 1200 \text{ A}$			
	Rate of mass removal	$\dot{m} = rac{I}{F} imes rac{Z}{v}$			
	So,	$\dot{m} = \frac{1200}{96540} \times \frac{55.85}{2} = 0.3471 \mathrm{g/sec}$			
MCQ 1.48	Match the following:				
GATE ME 2009 TWO MARK	NC code	Definition			
1 II O Dimiti	P. M05	1. Absolute coordinate system			
	Q. G01	2. Dwell			
	R. G04	3. Spindle stop			
	S. G09	4. Linear interpolation			
	(A) P-2, Q-3, R-4, S-1				
	(B) P-3, Q-4, R-1, S-2				
	(C) P-3, Q-4, R-2, S-1				
	(D) P-4, Q-3, R-2, S-1				
SOL 1.48	Option (C) is correct.	late			
	NC code	Definition			
	P. M05	3. Spindle stop			
	Q. G01	4. Linear interpolation			
	R. G04	2. Dwell			
	S. G09	1. Absolute coordinate system			
	So, correct pairs are, P-3, O	Q-4, R-2, S-1			
MCQ 1.49	What are the upper and lo	wer limits of the shaft represented by 60 f_8 ?			
GATE ME 2009	Use the following data :				
TWO MARK	Diameter 60 lies in the diam	-			
		t, <i>i</i> in $\mu m = 0.45 D^{1/3} + 0.001 D$			
	Where D is the representate Tolerance value for $IT8 =$				
	Fundamental deviation for				
	(A) Lower limit = 59.924 r	nm, Upper limit = 59.970 mm			
	(B) Lower limit = 59.954 mm, Upper limit = 60.000 mm				
	(C) Lower limit $= 59.970$ r	nm, Upper limit = 60.016 mm			
	(D) Lower limit = 60.000 r	nm, Upper limit = 60.046 mm			
SOL 1.49	Option (A) is correct.				
	Since diameter 60 lies in th	the diameter step of $50 - 80 \text{ mm}$, therefore the geometric			

mean diameter.

$$D = \sqrt{50 \times 80} = 63.246 \,\mathrm{mm}$$



Fundamental tolerance unit.

$$\begin{split} i &= 0.45 D^{1/3} + 0.001 D \\ &= 0.45 (63.246)^{1/3} + 0.001 \times 63.246 \\ &= 1.856 \,\mu\text{m} = 0.00186 \,\text{mm} \\ \end{split}$$
 Standard tolerance for the hole of grades 8 (IT8) $&= 25i = 25 \times 0.00186 = 0.0465 \,\text{mm} \\ \texttt{Fundamental deviation for `f' shaft} \\ e_f &= -5.5 D^{0.41} = -5.5 (63.246)^{0.41} \\ &= -30.115 \,\mu\text{m} = -0.030115 \,\text{mm} \\ \texttt{Upper limit of shaft} = \texttt{Basic size} + \texttt{Fundamental deviation} \\ &= 60 - 0.030115 = 59.970 \,\text{mm} \\ \texttt{Lower limit of shaft} = \texttt{Upper limit} - \texttt{Tolerance} = 59.970 - 0.0465 \\ &= 59.924 \end{split}$

MCQ 1.50 Match the items in Column I and Column II.

GATE ME 2009 TWO MARK	P.	Column I Metallic Chills	1.	Column II Support for the core
	Q.	Metallic Chaplets	2.	Reservoir of the molten metal
	R.	Riser	3.	Control cooling of critical sections
	s.	Exothermic Padding	4.	Progressive solidification
	(A)	P-1, Q-3, R-2, S-4		
	(B)	P-1, Q-4, R-2, S-3		
	(C)	P-3, Q-4, R-2, S-1		
	(D)	P-4, Q-1, R-2, S-3		
SOL 1.50	Opt	ion (D) is correct.		
		Column I		Column II
	Р.	Metallic Chills	4.	Progressive solidification
	Q .	Metallic Chaplets	1.	Support for the core
	R.	Riser	2.	Reservoir of the molten metal

- **S.** Exothermic Padding
- 3. Control cooling of critical sections

So, correct pairs are P-4, Q-1, R-2, S-3

Common Data for Question 51 and 52:

The inlet and the outlet conditions of steam for an adiabatic steam turbine are as indicated in the figure. The notations are as usually followed.



MCQ 1.51 If mass rate of steam through the turbine is 20 kg/s, the power output of the turbine (in MW) is (A) 12 157

INK	(A) 12.157	J (B) 12.941
	(C) 168.001	D (D) 1 68.785
		пстр

SOL 1.51 Option (A) is correct. Given : $h_1 = 3200 \text{ kJ/kg}$, $V_1 = 160 \text{ m/sec}$, $z_1 = 10 \text{ m}$

$$p_1 = 3 \text{ mpA}, \ \dot{m} = -\frac{dM}{dt} = 20 \text{ kg/sec}$$

It is a adiabatic process, So dQ = 0

Apply steady flow energy equation [S.F.E.E.] at the inlet and outlet section of steam turbine,

$$h_{1} + \frac{V_{1}^{2}}{2} + z_{1}g + \frac{dQ}{dm} = h_{2} + \frac{V_{2}^{2}}{2} + z_{2}g + \frac{dW}{dm}$$

$$dQ = 0$$
So $\frac{dQ}{dm} = 0$
And $h_{1} + \frac{V_{1}^{2}}{2} + z_{1}g = h_{2} + \frac{V_{2}^{2}}{2} + z_{2}g + \frac{dW}{dm}$

$$\frac{dW}{dm} = (h_{1} - h_{2}) + \left(\frac{V_{1}^{2} - V_{2}^{2}}{2}\right) + (z_{1} - z_{2})g$$

$$= (3200 - 2600) \times 10^{3} + \left[\frac{(160)^{2} - (100)^{2}}{2}\right] + (10 - 6)9.8$$

$$= 600000 + 7800 + 39.20$$
$$\frac{dW}{dm} = 607839.2 \text{ J/kg} = 607.84 \text{ kJ/kg}$$

Power output of turbine

$$P = \text{Mass flow rate} \times \frac{dW}{dm}$$
$$= 20 \times 607.84 \times 10^{3} \qquad \dot{m} = 20 \text{ kg/sec}$$
$$P = 12.157 \text{ MJ/sec} = 12.157 \text{ MW}$$

Assume the above turbine to be part of a simple Rankine cycle. The density of **MCQ 1.52** water at the inlet to the pump is 1000 kg/m^3 . Ignoring kinetic and potential energy GATE ME 2009 TWO MARK effects, the specific work (in kJ/kg) supplied to the pump is

() *****	(_)
(C) 2.930	(D) 3.510

Option (C) is correct. SOL 1.52

(A) 0.293

Given : $ho = 1000 \, \text{kg/m}^3$

Here given that ignoring kinetic & potential energy effects, So in the steady flow energy equation the terms $V^2/2, Z_1g$ are equal to zero and dQ is also zero for adiabatic process.

(B) 0.351

S.F.E.E. is reduces to, $h_4 = h_3 + \frac{dW_p}{dm}$ Here, W_p represents the pump work

where $h_3 =$ Enthalpy at the inlet of pump and $h_4 =$ Enthalpy at the outlet of the pump.

$$\frac{dW_p}{dm} = h_4 - h_3 = dh \qquad \dots (i)$$

For reversible adiabatic compression,

$$dQ = dh - \nu dp \qquad (dQ = 0)$$

$$dh = \nu dp$$
 ...(ii)

From equation (i) and (ii), we get

$$\begin{aligned} \frac{dW_p}{dm} &= \nu dp \\ \frac{dW_p}{dm} &= \frac{1}{\rho} (p_1 - p_2) \\ \frac{dW_p}{dm} &= \frac{(3000 - 70) \,\text{kPa}}{1000} \\ &= \frac{2930}{1000} \,\text{kPa} = 2.930 \,\text{kPa} \end{aligned}$$

Common Data for Questions 53 and 54 :

Radiative heat transfer is intended between the inner surfaces of two very large

GATE ME 2009 TWO MARK isothermal parallel metal plates. While the upper plate (designated as plate 1) is a black surface and is the warmer one being maintained at 727°C, the lower plate (plate 2) is a diffuse and gray surface with an emissivity of 0.7 and is kept at 227°C. Assume that the surfaces are sufficiently large to form a two-surface enclosure and steady-state conditions to exits. Stefan-Boltzmann constant is given as $5.67 \times 10^{-8} \,\mathrm{W/m^2 \, K^4}$

MCQ 1.53	The irradiation	(in	kW/m^2)	for	the plate	e (plate 1	1) is

19	(A) 2.5	(B) 3.6
	(C) 17.0	(D) 19.5

SOL 1.53 Option (D) is correct.



 $E_2 \rightarrow$ The radiant energy of gray surface

Now, Plate 1 emits radiant energy E_1 which strikes the plate 2. From it a part αE_1 absorbed by the plate 2 & the remainder $(E_1 - \alpha E_1)$ is reflected back to the plate 1. On reaching plate 1, all the part of this energy is absorbed by the plate 1, because the absorptivity of plate 1 is equal to one (it is a black surface).

Irradiation denotes the total radiant energy incident upon a surface per unit time per unit area.

Energy leaving from the plate 2 is,

$$E = E_2 + (1 - \alpha) E_1$$
 ...(i)

Hence, E_2 is the energy emitted by plate 2.

$$E_{2} = \varepsilon \sigma_{b} T_{2}^{4} = 0.7 \times 5.67 \times 10^{-8} \times (500)^{4} \qquad E = \varepsilon \sigma_{b} T^{4}$$

= 0.7 × 5.67 × 10⁻⁸ × 625 × 10⁸ = 2480.625 W/m²

And fraction of energy reflected from surface 2 is,

$$= (1 - \alpha) E_1 = (1 - \alpha) \sigma T_1^4$$

= 5.67 × 10⁻⁸(1 - 0.7) × (1000)⁴ = 17010 W/m²

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Now, Total energy incident upon plate 1 is,

$$E = E_2 + (1 - \alpha) E_1 = 2480.625 + 17010$$

= 19490.625 W/m² = 19.49 kW/m² \approx 19.5 kW/m²

MCQ 1.54 If plate 1 is also diffuse and gray surface with an emissivity value of 0.8, the net radiation heat exchange (in kW/m^2) between plate 1 and plate 2 is (A) 17.0

(A) 17.0	(B) 19.5
(C) 23.0	(D) 31.7

SOL 1.54 Option (D) is correct.

Given : $\varepsilon_2 = 0.8$, $\varepsilon_1 = 0.7$

As both the plates are gray, the net heat flow from plate 1 to plate 2 per unit time is given by,

$$Q_{12} = \frac{\varepsilon_1 \varepsilon_2}{\varepsilon_1 + \varepsilon_2 - \varepsilon_1 \varepsilon_2} \sigma_b (T_1^4 - T_2^4) = \frac{1}{\frac{1}{\varepsilon_2} + \frac{1}{\varepsilon_1} - 1} \sigma_b (T_1^4 - T_2^4)$$
$$= \frac{1}{\frac{1}{0.8} + \frac{1}{0.7} - 1} \times 5.67 \times 10^{-8} [(1000)^4 - (500)^4]$$
$$= \frac{1}{1.68} \times 5.67 \times 9375 = 31640.625 \text{ W/m}^2 \simeq 31.7 \text{ kW/m}^2$$

Common Data for Questions 55 and 56:

Consider the following PERT network:



The optimistic time, most likely time and pessimistic time of all the activities are given in the table below:

Activity	Optimistic time (days)	Most likely time (days)	Pessimistic time (days)
1 - 2	1	2	3
1 - 3	5	6	7
1 - 4	3	5	7
2 - 5	5	7	9
3 - 5	2	4	6
5 - 6	4	5	6
4 - 7	4	6	8
6 - 7	2	3	4

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MCQ 1.55	The critical path durat	ion of the network (in days) is
GATE ME 2009 TWO MARK	(A) 11	(B) 14
I WO MARK	(C) 17	(D) 18

SOL 1.55 Option (D) is correct.

Make the table and calculate the excepted time and variance for each activity

Activity	$\begin{array}{c} \mathbf{Optimistic} \\ \mathbf{time} \ (\mathbf{days}) \\ t_o \end{array}$	$\begin{array}{l} \textbf{Most likely} \\ \textbf{time} \\ \textbf{(days)} \\ t_m \end{array}$	$\begin{array}{c} \mathbf{Pessimistic} \\ \mathbf{time} \ (\mathbf{days}) \\ t_p \end{array}$	$egin{aligned} \mathbf{Expected} & \mathbf{Time} \ \mathbf{(days)} \ t_e = rac{t_o+4t_m+t_p}{6} \end{aligned}$	Variance $\sigma^2 = \left(rac{t_p - t_o}{6} ight)^2$
1 - 2	1	2	3	$\frac{1+8+3}{6} = 2$	$\left(\frac{3-1}{6}\right)^2 = \frac{1}{9}$
1 - 3	5	6	7	$\frac{5+24+7}{6} = 6$	$\left(\frac{7-5}{6}\right)^2 = \frac{1}{9}$
1 - 4	3	5	7	$\frac{3+20+7}{6} = 5$	$\left(\frac{7-3}{6}\right)^2 = \frac{4}{9}$
2 - 5	5	7	9	$\frac{5+28+9}{6} = 7$	$\left(\frac{9-5}{6}\right)^2 = \frac{4}{9}$
3 - 5	2	4	6	$\frac{2+16+6}{6} = 4$	$\left(\frac{6-2}{6}\right)^2 = \frac{4}{9}$
5 - 6	4	5	hein	$\frac{4+20+6}{6} = 5$	$\left(\frac{6-4}{6}\right)^2 = \frac{1}{9}$
4 - 7	4	6	8	$\frac{4+24+8}{6} = 6$	$\left(\frac{8-4}{6}\right)^2 = \frac{4}{9}$
6 - 7	2	3	4	$\frac{2+12+4}{6} = 3$	$\left(\frac{4-2}{6}\right)^2 = \frac{1}{9}$



Now, the paths of the network & their durations are given below in tables.

	Paths	Expected Time duration (in days)
i	Path 1-3-5-6-7	T = 6 + 4 + 5 + 3 = 18
ii	Path 1-2-5-6-7	T = 2 + 7 + 5 + 3 = 17
iii	Path 1-4-7	T = 5 + 6 = 11

Since path 1-3-5-6-7 has the longest duration, it is the critical path of the network and shown by dotted line.

Hence, The expected duration of the critical path is 18 days.

MCQ 1.56	The standard deviation of the critical	path is
GATE ME 2009 TWO MARK	(A) 0.33	(B) 0.55
I WO MARK	(C) 0.77	(D) 1.66

SOL 1.56 Option (C) is correct. The critical path is 1-3-5-6-7

Variance along this critical path is,

$$\sigma^{2} = \sigma_{1-3}^{2} + \sigma_{3-5}^{2} + \sigma_{5-6}^{2} + \sigma_{6-7}^{2}$$
$$= \frac{1}{9} + \frac{4}{9} + \frac{1}{9} + \frac{1}{9}$$
$$= \frac{7}{9}$$

We know,

Standard deviation =
$$\sqrt{\text{Variance}(\sigma^2)}$$

= $\sqrt{\frac{7}{9}} = 0.88$

The most appropriate answer is 0.77.

Statement for Linked Answer Questions 57 and 58 :

In a machining experiment, tool life was found to vary with the cutting speed in the following manner :

Cutting speed (m/min)	Tool life (minutes)
60	81
90	36

The exponent (n) and constant (K) of the Taylor's tool life equation are MCQ 1.57 (A) n = 0.5 and K = 540GATE ME 2009 (B) n = 1 and K = 4860TWO MARK (C) n = -1 and K = 0.74(D) n = -0.5 and K = 1.155 **SOL 1.57** Option (A) is correct. Given : $V_1 = 60 \text{ m/min}$, $T_1 = 81 \text{ min}$, $V_2 = 90 \text{ m/min}$, $T_2 = 36 \text{ min}$. From the Taylor's tool life Equation $VT^n = \text{Constant}(\mathbf{K})$ $V_1 T_1^n = \mathbf{K}$ For case (I), $60 \times (81)^n = K$...(i) $V_2 T_2^n = \mathbf{K}$ For case (II), $90 \times (36)^n = K$...(ii) By dividing equation (i) by equation (ii),

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	$\frac{60 \times (81)^n}{90 \times (36)^n} = \frac{K}{K} = 1$	$rac{60 imes (81)^n}{90 imes (36)^n} = rac{\mathrm{K}}{\mathrm{K}} = 1$
	$\left(\frac{81}{36}\right)^n = \frac{90}{60}$	
	$\left(rac{9}{4} ight)^n=\left(rac{3}{2} ight)$	$\left(\frac{1}{4}\right) = \left(\frac{1}{2}\right)$
	Taking (log) both the sides, (2)	
	$n\log\left(\frac{9}{4}\right) = \log\left(\frac{3}{2}\right)$	$n\log\left(\frac{3}{4}\right) = \log\left(\frac{3}{2}\right)$
	$n \times 0.3522 = 0.1760$	
	n = 0.5 Substitute $n = 0.5$ in equation (i), we get	
	$K = 60 \times (81)^{0.5} = 540$	
	So, $n = 0.5 \text{ and } K = 540$	n = 0.5 and K = 540
MCQ 1.58	What is the percentage increase in tool life when the cutting speed is halved ?	
GATE ME 2009 TWO MARK	(A) 50% (C) 300% (B) 200% (D) 400%	(B) 200% (D) 400%
SOL 1.58	Option (C) is correct. Take, $n = 0.5$ C {from previous part	is correct. $n = 0.5$ 1 C {from previous part}
	From Taylor's tool life equation $VT^n = C$ $VT^{0.5} = C$	$VT^n = C$
	$V = \frac{1}{\sqrt{T}} \qquad \dots ($	$V = \frac{1}{\sqrt{T}} \qquad \dots (i)$
	Given that cutting speed is halved $V = 1$	
	$V_2 = \frac{1}{2} V_1 \Rightarrow \frac{V_2}{V_1} = \frac{1}{2}$	$V_2 = \frac{1}{2} V_1 \Rightarrow \frac{V_2}{V_1} = \frac{1}{2}$
	Now, from equation (i),	
	$rac{V_2}{V_1}=\sqrt{rac{T_1}{T_2}}$	$rac{V_2}{V_1}=\sqrt{rac{T_1}{T_2}}$
	$rac{1}{2}=\sqrt{rac{T_1}{T_2}}$	$rac{1}{2}=\sqrt{rac{T_1}{T_2}}$
	$\frac{1}{4} = \frac{T_1}{T_2}$	$\frac{1}{4} = \frac{T_1}{T_2}$
	$rac{T_2}{T_1}=4 \ \Rightarrow T_2=4 \ T_1$	$rac{T_2}{T_1}=4 \ \Rightarrow T_2=4T_1$
	Now, percentage increase in tool life is given by $= \frac{T_2 - T_1}{T_1} \times 100 = \frac{4T_1 - T_1}{T_1} \times 100$	
	$=rac{3T_1}{T_1} imes 100=300\%$	$=\frac{3T_1}{T_1} \times 100 = 300\%$

Statement for Linked Answer Questions 59 and 60

A 20° full depth involute spur pinion of 4 mm module and 21 teeth is to transmit 15 kW at 960 rpm. Its face width is 25 mm.

MCQ 1.59	The tangential force transmitted (in N) is			
GATE ME 2009	(A) 3552	(B) 2611		
TWO MARK	(C) 1776	(D) 1305		
SOL 1.59	N = 960 rpm, b = 25 mm	$D = mZ = 4 \times 21 = 84 \text{ mm}$		
		$F_T = \frac{T}{r}$	(i)	
	Power transmitted,	$P = \frac{2\pi NT}{60} \Rightarrow T = \frac{60P}{2\pi N}$ $F_T = \frac{60P}{2\pi N} \times \frac{1}{r}$		
	Then	$F_T=rac{60P}{2\pi N} imesrac{1}{r}$	r = Pitch circle radius	
		$= \frac{60 \times 15 \times 10^{3}}{2 \times 3.14 \times 960} \times \frac{1}{42 \times 1}$ = 3554.36 N \approx 3552 N		
MCQ 1.60	Given that the tooth g	eometry factor is 0.32 and the co	ombined effect of dynamic	
GATE ME 2009	load and allied factors	intensifying the stress is 1.5; the	minimum allowable stress	
TWO MARK	(in MPa) for the gear n			
	(A) 242.0	(B) 166.5		
	(C) 121.0	(D) 74.0		
SOL 1.60	Option (B) is correct. From Lewis equation			
	$\sigma_b =$	$\frac{F_T p_d}{h u} = \frac{F_T}{h \times u \times m}$	$p_d = \frac{\pi}{n} = \frac{\pi}{\pi m} = \frac{1}{m}$	

$$\sigma_b = rac{by \quad b imes y imes m}{25 imes 10^{-3} imes 0.32 imes 4 imes 10^{-3}}$$

 p_d p_c πm \overline{m}

 $\sigma_b = 111 \,\mathrm{MPa}$ Minimum allowable (working stress)

$$\sigma_W = \sigma_b \times C_v$$

= 111 × 1.5
 $\sigma_W = 166.5 \text{ MPa}$

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Answer Sheet									
1.	(A)	13.	(B)	25.	(A)	37.	(A)	49.	(A)
2.	(C)	14.	(C)	26.	(A)	38.	(A)	50.	(D)
3.	(C)	15.	(B)	27.	(B)	39.	(A)	51.	(A)
4.	(D)	16.	(D)	28.	(B)	40.	(D)	52.	(C)
5.	(A)	17.	(A)	29.	(D)	41.	(B)	53.	(D)
6.	(B)	18.	(A)	30.	(C)	42.	(B)	54.	(D)
7.	(A)	19.	(C)	31.	(D)	43.	(C)	55.	(D)
8.	(A)	20.	(D)	32.	(A)	44.	(D)	56.	(C)
9.	(B)	21.	(C)	33.	(C)	45.	(A)	57.	(A)
10.	(C)	22.	(A)	34.	(A)	46.	(D)	58.	(C)
11.	(C)	23.	(B)	35.	(B)	47.	(A)	59.	(A)
12.	(D)	24.	(A)	36.	(A)	48.	(C)	60.	(B)

<u>g a t e</u> help

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