W	$\frac{1}{WANDOOD CANITHAM RDIDCE MATEDIAL CLASS Y 2021 22}$					
•••						
	NUMI	<u>BERS</u>				
	Natural numbers	1,2,3,4,5,6,				
	Even numbers	2,4,6,8,10,12,				
	Odd numbers	1,3,5,7,9,11,				
<u>Pri</u>	me numbers					
Nu	mbers (other than 1) which are not divis	ible by the numbers other than 1 and the				
nu	mber itself are called prime numbers					
Exa	mple: 2,3,5,7,11,13,17,19,23	, 29 , 31 , 37 , . , . , .				
		6				
Fractions						
Fractions are the number of parts .						
Exa	Example: $\frac{1}{2}$, $\frac{3}{5}$, $\frac{5}{4}$, $\frac{10}{7}$,					
<u>Ne</u>	gative numbers					
Nu	mbers written with a minus sign are called	negative numbers .				
Positive numbers						
Numbers which are not negative are called positive numbers .						
NOTE : 0 is neither positive nor negative .						
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NUMBERS AND ALGEBRA				
Algebra				
Mathematical shorthand of writing number related facts using letters is called <i>algebra</i> .				
<u>Concept 1</u>				
Multiplying two numbers by a number separately and adding give the same result as				
multiplying their sum by the number .				
That is , $x + y = (x + y) z$, for all numbers x, y, z				
<u>Activity</u>				
Try these problems				
a) $36 \times 28 + 64 \times 28$ b) $125 \times 436 + 875 \times 436$				
<u>Answer</u>				
a) $36 \times 28 + 64 \times 28 = (36 + 64)28 = 100 \times 28 = 2800$				
b) $125 \times 436 + 875 \times 436 = (125 + 875)436 = 1000 \times 436 = 436000$				
More activity				
Try these problems				
a) $36 \times 18 + 14 \times 18$ b) $185 \times 122 + 215 \times 122$				
<u>Concept 2</u>				
Multiplying two numbers by a number separately and subtracting give the same result as				
multiplying their difference by the number .				
That is, $x z - y z = (x - y) z$, for all numbers x, y, z				
<u>Activity</u>				
Try these problems				
a) $58 \times 76 - 48 \times 76$ b) $239 \times 397 - 139 \times 397$				
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Answer_
a) $58 \times 76 - 48 \times 76 = (58 - 48)76 = 10 \times 76 = 760$
b) $239 \times 397 - 139 \times 397 = (239 - 139)397 = 100 \times 397 = 39700$
More activity
Try these problems
a) $96 \times 39 - 76 \times 39$ b) $316 \times 125 - 116 \times 125$
<u>Concept 3</u>
Algebraic expressions
General form indicating arithmetical operations using letters are called
algebraic expressions .
NOTE :
When we use algebra to state general properties of numbers, we should also specify the
when we use algebra to state general properties of numbers, we should also specify the
type of numbers indicated by the letter .
In algebra , natural numbers are usually denoted by n . (any letter can be used)
Activity
Adding 10 repeatedly to 1 .
a) Find the numbers .
b) Find the algebraic expression of such numbers .
Answer
a) 11 , 21 , 31 , 41 , 51 ,
b) Algebraic expression = $1 + 10n$
<u>More activity</u>
a) Find the algebraic expression for the numbers got by adding 5 repeatedly to 1 .

b) Find the algebraic expression for the numbers got by adding 5 repeatedly to 4 .

c) Add the numbers in the same position of the first two patterns . Why do we get only

multiples of 5 ?

Agebraic forms

1) Numbers of the form 2 n are even .

2) Numbers of the form 2 n - 1 are odd .

3) Numbers of the form 5 n are the multiples of 5.

4) Numbers of the form 10 n +1 are the numbers got by adding 1 to the multiples of 10.

4) Numbers of the form 3 n - 2 are the numbers which give a remainder 1 when divided

by 3

That is ,

- 1) Algebraic form of even numbers = 2 n
- 2) Algebraic form of odd numbers = 2 n- 1
- 3) Algebraic form of multiples of 5 = 5 n
- 4) Algebraic form of the numbers got

by adding 1 to the multiples of 10 = 10 n+1

5) Algebraic form of the numbers which

give a remainder 1 when divided by 3 = 3 n - 2

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NEGATIVE NUMBERS – OPERATIONS

Concept 1

For positive numbers , the larger subtracted from the smaller is the negative of the smaller subtracted from the larger .

For any positive numbers x, y if x < y then x - y = -(y - x)Activity Try these problems **a)** 4 – 5 **b)** 12 - 20 521 - 743 C) Answer **a)** 4 - 5 = -1**b)** 12 - 20 = -8c) 521 - 743 = -222More activity Try these problems . **b)** 37 – 95 **c)** 135 – 627 a) 7 - 9 <u>Concept 2</u> Adding to the negative of a positive number, a second positive number means subtracting the first number from the second number. For any two positive numbers x and y-x + y = y - xSARATH A S, GHS ANCHACHAVADI, MALAPPURAM

<u>Activity</u>

6

Try these problems .

a) -2 + 8

b) -95 + 20 **c)** −675 **+** 520 <u>Answer</u>

a) -2 + 8 = 6

b) -95 + 20 = -75

c) -675 + 520 = -155

More activity

Try these problems .

a) -9 + 6

b) -45 + 80

-326 + 792

Concept 3

Subtracting a positive number from the negative of a positive number, we get the negative of the sum of these positive numbers .

For any positive numbers x and y

-x - y = -(x + y)

<u>Activity</u>

Try these problems .

a) -8 - 5 **c)** -372 - 251 **b)** -62 - 38

Answer

- a) -8 5 = -13
- **b)** -62 38 = -100
- c) -372 251 = -623

Mo	7 <u>re activity</u>				
Try	these problems .				
a)	-7 - 9 b) -18 - 73 c) -267 - 679				
<u>Co</u>	ncept_4				
	Adding the negative of a positive number means subtracting that positive number				
<u>Ac</u>	ivity				
Try	these problems .				
a)	5 + (-3) b) -15 + (-32) c) 715 + (-936)				
An	swer				
a)	5 + (-3) = 5 - 3 = 2				
b)	-15 + (-32) = -15 - 32 = -47				
c)	715 + (-936) = 715 - 936 = -221				
M	ore activity				
Try	these problems .				
a)	4 + (-9) b) -75 + (-19) c) 621 + (-384)				
<u>Co</u>	ncept 5				
	Subtracting the negative of a positive number means adding that positive number				
<u>Act</u>	<u>Activity</u>				
Try these problems .					
a)	b) $-63 - (-15)$ c) $-531 - (-856)$				
An	swer_				
a)	8 - (-6) = 8 + 6 = 14				
b)	-63 - (-15) = -63 + 15 = -48				
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c) -531 - (-856) = -531 + 856 = 325

More activity

Try these problems .

a) 1 - (-9) b) -78 - (-56) c) -267 - (-598)

<u>Concept 6</u>

The negative of the negative of a number is that number itself

That is, -(-x) = x, for any number x

Concept 7

The product of a positive number and the negative of a positive number means,

the negative of the product of these positive numbers .

For any positive numbers x and y

-(x) y = x (-y) = -x y

<u>Activity</u>

Try these problems . a) $7 \times (-5)$ b) -15×12 c) $125 \times (-426)$ Answer a) $7 \times (-5) = -35$ b) $-15 \times 12 = -180$ c) $125 \times (-426) = -53250$ More activity Try these problems . a) $(-8) \times 9$ b) $25 \times (-46)$ c) $235 \times (-124)$ SARATH A S , GHS ANCHACHAVADI , MALAPPURAM

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Concept 8

The product of the negatives of two positive numbers means the product of these positive

numbers.

For any two positive numbers x , y

(-x)(-y) = xy

Activity_

Try these problems .

- **a)** $(-4) \times (-7)$
- **b)** $(-36) \times (-15)$
- $(-345) \times (-152)$ C)

Answer

- $(-4) \times (-7) = 28$ a)
- **b)** $(-36) \times (-15) = 540$
- c) $(-345) \times (-152) = 52440$

More activity

Try these problems .

- **a)** $(-6) \times (-9)$
- **b)** $(-75) \times (-28)$
- **c)** $(-495) \times (-364)$

NEGATIVE DIVISION

As in the case of positive numbers , division is the inverse of multiplication for negative

numbers .

NOTE :

In algebra , we usually write $x \div y$ as $\frac{x}{y}$. So , in the equation $z = \frac{x}{y}$

x = -6, y = 2 gives $z = \frac{-6}{2} = -3$

x = 6, y = -2 gives $z = \frac{6}{-2} = -3$

x = -6, y = -2 gives $z = \frac{-6}{-2} = 3$

More activity

In the equation $z = \frac{x}{y}$, take x as the x, y as the numbers given below and

calculate the number z .

- **a)** x = -20 , y = 5
- **b)** x = 48, y = -6
- c) x = -63 , y = -9









EQUATIONS

Activity_

The length of a rectangle is 5 centimetres more than twice of its breadth and its perimeter

is 34 centimetres . Find its area .

<u>Answer</u>



More activity

In a calendar , a square of four numbers is marked . The sum of the numbers is 80 .

What are the numbers ?

16 IDENTITIES

<u>Concept 1</u>

To multiply a sum of positive numbers by a sum of positive numbers , multiply each

number in the second sum by each number in the first sum and add .

$$(x + y) (u + v) = xu + xv + yu + yv$$

for any our positive numbers x, y, u, v

<u>Activity</u>

Look at these .

1	×	4	=	(2	×	3)	_	2
2	×	5	=	(3	×	4)	_	2
3	×	6	=	(4	×	5)	_	2
4	×	7	=	(5	×	6)	_	2

a) Write the next two lines in this pattern .

b) If we take four consecutive natural numbers , what is the relation between the product of the first and the last , and the product of the middle two ?

c) Explain the general principle using algebra .

<u>Answer</u>

a)

- $5 \times 8 = (6 \times 7) 2$ $6 \times 9 = (7 \times 8) - 2$
- b) If we take four consecutive natural numbers , the product of the first and the last is 2 less than the product of the middle two.

c) If we take four consecutive natural numbers are x, x + 1, x + 2, x + 3, then

$$x(x+3) = (x+1)(x+2) - 2$$
.

 $x (x+3) = x^{2} + 3x$ (x+1)(x+2) = x×x + x×2 + 1×x + 1×2 = x² + 2x + x + 2 = x² + 3x + 2

Thus x(x+3) = (x+1)(x+2) - 2.

<u>More activity</u>

a) Mark four numbers forming a square in a calendar . Add the product of the diagonal

pair and find the difference of these products .

b) Is it same for all the squares of four numbers ?

c) Explain why this is so , using algebra .

Concept 2

The square of sum of two positive numbers is the sum of the squares of the two numbers and twice their product .

For any two positive numbers x and y , $(x \,+\, y)^2 \,=\, x^2 \,+\, y^2 \,+\, 2xy$

<u>Activity</u>

Look at these.

1	\times	3	=	2^2	_	1
2	×	4	=	3^2	_	1
3	×	5	=	4^2	_	1
4	\times	6	_	5^2	_	1

a) Write the next two lines in this pattern .

b) If we take three consecutive natural numbers ,what is the relation between the product of the first and the last , and the middle number ?

c) Explain the general principle using algebra .

Answer

a)

 $egin{array}{rcl} 7 \, imes \, 5 &=& 6^2 \, - \, 1 \ 8 \, imes \, 6 &=& 7^2 \, - \, 1 \end{array}$

b) If we take three consecutive natural numbers , the product of the first and the last is 1

less than the square of the middle number .

c) If we take the three consecutive natural numbers are x, x + 1, x + 2, then

$$x(x+2) = (x+1)^2 - 1$$

 $x (x + 2) = x^{2} + 2x$ $(x + 1)^{2} - 1 = x^{2} + 1^{2} + 2 \times x \times 1 - 1 = x^{2} + 2x + 1 - 1 = x^{2} + 2x$ Thus $x (x + 2) = (x + 1)^{2} - 1$.

More activity

Look at these.

 $egin{array}{rll} 1^2 + (4 imes 2) &=& 3^2 \ 2^2 + (4 imes 3) &=& 4^2 \ 3^2 + (4 imes 4) &=& 5^2 \ 4^2 + (4 imes 5) &=& 6^2 \end{array}$

a) Write the next two lines in this pattern .

b) Write the general principle of the above pattern ?

c) Explain the general principle using algebra .

<u>Concept 3</u>

The square of the difference of two positive numbers is twice their product subtracted

from the sum of their squares.

For all positive numbers x , y with
$$x > y$$
 ,
 $(x - y)^2 = x^2 + y^2 - 2xy$

<u>Activity</u>

Find the squares of the following numbers

a) 49 **b)** 98

<u>Answer</u>

a) $49^2 = (50-1)^2 = 50^2 + 1^2 - 2 \times 50 \times 1 = 2500 + 1 - 100 = 2401$

b) $98^2 = (100 - 2)^2 = 100^2 + 2^2 - 2 \times 100 \times 2 = 10000 + 4 - 400 = 99604$

<u>More activity</u>

Find the squares of the following numbers

a) 47 **b)** 99

Concept 4

The product of the sum and the difference of two positive numbers is the difference of their squares .

For any two positive numbers x, y with $\, {
m x} \, > \, {
m y}\,$, $(x \, + \, y) \, (x \, - \, y) \, = \, x^2 \, - \, y^2$

<u>Activity</u>

Look at these

3^2	_	1^2	=	4	\times	2
4^2	_	2^2	=	4	×	3
5^2	_	3^2	=	4	×	4
6^2	_	4^2	_	4	\times	5

a) Write the next two lines in this pattern .

b) If we take three consecutive natural numbers , what is the relation between the difference of the squares of first and the last , and the middle number ?

c) Explain the general principle using algebra .

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Answer a) $7^{2} - 5^{2} = 4 \times 6$ $8^{2} - 6^{2} = 4 \times 7$ b) If we take three consecutive natural numbers , the difference of the squares of the first and last numbers is four times the middle number . c) If we take the three natural numbers are x , x + 1 , x + 2, then $(x + 2)^{2} - x^{2} = 4 (x + 1)$ $(x + 2)^{2} - x^{2} = (x + 2 + x)(x + 2 - x) = (2x + 2)2 = 4x + 4$ 4 (x + 1) = 4x + 4Thus $(x + 2)^{2} - x^{2} = 4 (x + 1)$.

More activity

a) Mark four numbers forming a square in a calendar . Add the squares of the diagonal

pair and find the difference of these sums .

- b) Is it same for all the squares of four numbers?
- c) Explain why this is so , using algebra .

PAIRS OF EQUATIONS

<u>Concept</u>

If two informations of two measures are given , we can find them by forming a pair

of equations with two letters .

Activity_

The price of 3 pencils and 4 pens is 55 rupees . The price of 5 pencils and 2 pens is 45

rupees . What is the price of a pen ? And the price of the note book ?

<u>Answer</u>

Take, the price of a pen = x and the price of a pencil = y, then

3x + 4y =	55	(1)
-----------	----	-----

$$5x + 2y = 45$$
 (2)

(1) x 5 ==>
$$15 x + 20 y = 275$$
 (3)

$$(2) x 3 ==> 15 x + 6 y = 135$$
(4)

$$(3) - (4) = 15x + 20y = 275 - 15x + 20y = 275$$

y

$$15 x + 6 y = 135$$

0 + 14 y = 140
140

$$=\frac{140}{14} = 10$$

 $3x + 4 \times 10 = 55 = 3x + 40 = 55 = 3x = 15 = x = \frac{15}{3} = 5$

Price of a pencil = x = 5 Rs , Price of a pen = y = 10 Rs

<u>More activity</u>

4 small buckets and 7 large buckets of water make 62 litres . 6 small buckets and 5 large buckets make only 60 litres . How much water can each bucket hold ?

EQUAL TRIANGLES

<u>Concept -1</u>

If the sides of a triangle are equal to the sides of another triangle , then the angles of the

triangles are also equal.

<u>Activity</u>



C

D

5 ch

7 cm

Find the equal angles of triangles ABC and ABD.

<u>Answer</u>

In triangles ABC and ABD,

$$AC = AD$$
 , $BC = BD$

AB = AB (common side)

(If the sides of a triangle are equal to the

sides of another triangle , then the angles

of the triangles are also equal.)

$$\angle BAC = \angle BAD$$

 $\angle ABC = \angle ABD$

 $\angle ACB = \angle ADB$

More activity

In quadrilateral PSQR , PR = PS , QR = QS

 $< SPQ = 30^{\circ}$, $< PQR = 60^{\circ}$

Find the measures of all the angles of the

quadrilateral .

Concept -2

If two sides of a triangle and the angle made by them are equal to two sides of another triangle and the angle made by them , then the third sides of the triangles are also equal and the other two angles are also equal .

Activity_

```
In the figure , D is the midpoint of BC . \angle BDA = 90^{\circ}
```

a) Prove that AB = AC

b) Prove that *AD* **is the bisector of** $\angle BAC$

<u>Answer</u>

```
In triangles ADB and ADC,
```

```
BD = CD ( D is the midpoint of BC )
```

AD = AD (common side)

 $\angle ADB = \angle ADC = \angle 90^{\circ}$

a) AB = AC (If two sides of a triangle and the angle made by them are equal to two sides of another triangle and the angle made by them , then the third sides of the triangles are also equal and the other two angles are also equal .)

b) $\angle BAD = \angle CAD$

AD is the bisector of \angle BAC .





More activity

In the figure , P is the midpoint of AB

and CD .

a) Which angle has the same measure as that of \angle APC ?

b) Prove that AC = BD .

c) Prove that BD is parallel to AC .

<u>Concept -3</u>

If one side of a triangle and the angles at its ends are equal to one side of another triangle and the angles at its ends , then the third angles are also equal and the sides opposite

D

Α

24

equal angles are equal.

Activity_

In any parallelogram , opposite sides are equal

<u>Answer</u>

In the figure , ABCD is a parallelogram .

That is, side AB is parallel to the side CD,

and AD is parallel to BC .

Join AC .

In triangles ACD and ABC,

AC = AC (common side)

 $\angle CAD = \angle ACB$ (alternate angles are equal)

$$\angle ACD = \angle BAC$$

So AB = CD, AD = BC (If one side of a triangle and the angles at its ends are equal to one side of another triangle and the angles at its ends, then the third angles are also equal and the sides opposite equal angles are equal)

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C

B



ISOSCELES TRIANGLES

Concept - 4

A triangle with two sides equal , is called an isosceles triangle .

<u>Concept - 5</u>

Equilateral triangle

A triangle with all three sides equal , is called an equilateral triangle .

<u>Concept - 6</u>

In any isosceles triangle , the perpendicular from the point joining equal sides to

the opposite side bisects the angle at this point and the side opposite

A line dividing a line or an angle into two equal parts is called a bisector

NOTE : The relations between the base and the third vertex of an isosceles triangle can be put in three different ways .

1) The perpendicular from the third vertex bisects the base .

2) The line joining the third vertex and the midpoint of the base is

perpendicular to the base .

3) The third vertex is on the perpendicular bisector of the base .

POLYGONS

We can divide a polygon into triangles by drawing maximum number of diagonals from

any one of its vertices . Hence we can find the sum of the angles of this polygon .

We can draw a maximum of **n** - **3** diagonals from a vertex of an **n**- sided polygon

If we draw maximum number of diagonals from a vertex of an $\,n$ - sided polygon , we get $\,n$ - 2 triangles .

The sum of the angles of an n-sided polygon is $(n-2) \times 180^{\circ}$

Polygon	Number of sides	Sum of angles
Triangle	3	180°
Quadrilateral	4	$2 \ge 180 = 360^{\circ}$
Pentagon	5	$3 \ge 180 = 540^{\circ}$
Hexagon	6	$4 \ge 180 = 720^{\circ}$
Heptagon	7	$5 \ge 180 = 900^{\circ}$
Octagon	8	$6 \ge 180 = 1080^{\circ}$
Nonagon	9	$7 \ge 180 = 1260^{\circ}$
Decagon	10	$8 \ge 180 = 1440^{\circ}$

Activity_

What is the sum of the angles of a 12 sided polygon ?

<u>Answer</u>

Sum of angles = $10 \times 180 = 1800^{\circ}$

<u>More activity</u>

The sum of the angles of a polygon is 3600[°]. How many sides does it have ?

Angle around a point is 360°

Outer angle of a triangle

If we extend one side of a triangle , we get a new angle outside the triangle . This angle is

called an outer angle (exterior angle).



In any triangle , the outer angle at a vertex is equal to the sum of the inner angles at

the other two vertices .



The sum of inner and outer angle at a vertex of a polygon is 180°

The sum of the outer angles of any polygon is **360**⁰

<u>Activity</u>

All angles in an 18 sided polygon are equal . How much is each outer angle ?

<u>Answer</u>

Sum of the outer angles $= 360^{\circ}$

An outer angle = $\frac{360}{18}$ = 20°

<u>More activity</u>

In a polygon with all angles equal , one outer angle is 12⁰ .How many sides does it have ?

<u>Regular polygon</u>

A polygon with equal sides and angles is called a regular polygon .

<u>Activity</u>

A regular polygon has 12 sides.

a) What is the measure of each outer angle ?

b) What is the measure of each inner angle ?

<u>Answer</u>

a) Sum of the outer angles = 360°

An outer angle = $\frac{360}{12}$ = 30°

b) An inner angle = $180 - 30 = 150^{\circ}$

More activity

Each angle of a regular polygon is 170° .

a) What is the measure of each outer angle ?

b) How many sides does it have ?

QUADRILATERALS

Polygon	Features
Rectangle	Opposite sides equal
	Opposite sides parallel
	All angles right
	Diagonals equal
	Diagonals bisect each other
<u>Square</u>	All sides equal
	Opposite sides parallel
	All angles right
	Diagonals equal
	Diagonals bisect each other
	Diagonals perpendicular to each other
Parallelogram	Opposite sides equal
P	Opposite sides parallel
	Opposite angles equal
6	Diagonals bisect each other
	Sum of angles on the same side 180°
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More activity

a) Calculate the area of the parallelogram in the figure

b) What is the distance between the parallel sides of

length 4 centimetres.

Area of a Rhombus

The area of a rhombus is half the product of the diagonals .

<u>Activity</u>

The length of the diagonals of a rhombus are 6 centimetres and 8 centimetres .

a) Calculate its area .

b) What is the measure of the angle between the diagonals ?

c) Compute the length of the side .

<u>Answer</u>

a) Area of the rhombus = $\frac{1}{2}$ x product of the diagonals.

= $\frac{1}{2} \times 6 \times 8$ = 24 square centimetres

b) Angle between the diagonals = 90°

c) In right triangle APB ,

 $Base^2$ + $Altitude^2$ = $Hypotenuse^2$ ==> BP^2 + AP^2 = AB^2

 $=> 3^2 + 4^2 = AB^2 => 9 + 16 = AB^2$

==> AB^2 = 25 ==> AB = $\sqrt{25}$ = 5 cm

Side of the rhombus = 5 centimetres .



3 cm

-- 12 cm

<u>More activity</u>

The area of a rhombus is 96 square centimetres and the length of one of its diagonal is

16 centimetres .

- a) What is the length of its second diagonal ?
- b) What is the measure of the angle between the diagonals ?
- c) Compute the length of the side .
- d) Compute the distance between the parallel sides .

<u>Area of a trapezium</u>

The area of a trapezium is half the product of the parallel sides and the distance between

them.

<u>Activity</u>

The length of the parallel sides of a trapezium are 12 centimetres, 8 centimetres and the distance between them is 10 centimetres. What is its area ?

Answer

a) Area of the trapezium = $\frac{1}{2}$ x sum of parallel sides x distance between them

 $= \frac{1}{2} \times (12 + 8) \times 10 = \frac{1}{2} \times 20 \times 10 = 100 \text{ square centimetres}$

D

A

 $7 \ cm$

C

10 cm

8 cm

More activity

In the figure , ABCD is a trapezium .

 $\angle A = 90^{\circ}$, AB = 8 centimetres,

BD = 10 centimetres and , **DC** = 7 centimetres

a) What is the length of AD ?

b) Compute the area of the trapezium .



RATIO

<u>Concept 1</u>

If two quantities are in the ratio a:b, then there is a quantity x such that the first

is ax and the second is bx

<u>Activity</u>

The length and breadth of a rectangle are in the ratio 5:4 and its perimeter is 54 centimeters. Calculate the length and breath.

<u>Answer</u>

Length = 5xBreadth = 4xPerimeter = 54 ==> $2 \times 5x + 2 \times 4x = 54$

$$10x + 8x = 54$$

 $18x = 54 \implies x = \frac{54}{18} = 3$

Length = $5x = 5 \times 3 = 15 \ cm$

Breadth = $4x = 4 \times 3 = 12 cm$

More activity

In a regular polygon , the ratio of the inner and outer angle is 7 : 2 .

a) What is each inner angle ?

b) What is each outer angle ?

c) How many sides does the polygon have ?

Concept 2

If three quantities are in the ratio a : b : c, then there is a quantity x such that

the first is ax , the second bx and the third is $\,cx$.

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<u>Activity</u>

The outer angles of a triangle are in the ratio 3:4:5 .

a) What is the sum of the outer angles ?

b) What is each outer angle ?

Answer

a) Sum of outer angles = 360° b) If we take the outer angles are 3x, 4x, 5x $3x + 4x + 5x = 360 ==> 12x = 360 ==> x = \frac{360}{12} = 30$ Outer angles = 3×30 , 4×30 , 5×30 90° , 120° , 150°

More activity

The length , breadth ,and height of a rectangular block are in the ratio 5 : 3 : 6 and its volume is 2160 cubic centimetres . Calculate the length , breadth and height .
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<u>NEW NUMBERS</u>			
The square of any fraction is not 2			
The diagonal of a square of side 1 cannot be expressed as a fraction .			
Concept 1			
We can not express all the lengths using fractions			
We have to make a new kind of number to denote measures which cannot be expressed as			
fractions .			
Concept 2			
If x is a positive number , in some cases \sqrt{x} would be a natural number or fraction ,			
in some cases , we compute fractions whose squares get closer to x and write \sqrt{x} in			
decimal form .			
Concept 3			
To get fractions approximately equal to the sum (or difference) of square roots of positi -			
ve numbers which are not perfect squares , we add approximately equal fractions of each			
<u>Activity</u>			
The length of the perpendicular sides of a right triangle are $\sqrt{3}$ centimetres and			
$\sqrt{2}$ centimetres.			
a) Calculate the length of its hypotenuse .			
b) Calculate the perimeter of the triangle .			
(Hint: $\sqrt{2} = 1.41$, $\sqrt{3} = 1.73$, $\sqrt{5} = 2.23$)			
<u>Answer</u>			
a) Base ² + Altitude ² = Hypotenuse ² ==> $(\sqrt{3})^2$ + $(\sqrt{2})^2$ = Hypotenuse ²			
==> 3 + 2 = Hypotenuse ² ==> Hypotenuse ² = 5 ==> Hypotenuse = $\sqrt{5}$ cm			
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b) Perimeter = $\sqrt{3} + \sqrt{2} + \sqrt{5} = 1.73 + 1.41 + 2.23 = 5.37$ സെ. മീ		
<u>More activity</u>		
In the figure , in triangle ABC		
AB = 2 metres , $\angle A = 30^{\circ}$, $\angle B = 105^{\circ}$		
a) What is the altitude of an equilateral triangle of		
side 2 metres ?		
b) Calculate the perimeter of triangle ABC .		
(Hints : Draw a perpendicular from B to AC . $\sqrt{2} = 1.41$, $\sqrt{3} = 1.73$)		
Concept 4		
For any positive numbers x and y , $\sqrt{x} imes\sqrt{y}=\sqrt{xy}$		
Activity		
Length of a rectangle is $\sqrt{5}$ centimetres and its breadth is $\sqrt{2}$ centimetres . Find its		
area.		
<u>Answer</u>		
Area = $\sqrt{5} \times \sqrt{2} = \sqrt{10} \ sq.cm$		
More activity		
In the figure , in triangle ABC , AB = 2 centimetres . \angle A = 60 $^{\circ}$, \angle B = 75 $^{\circ}$		
a) Find the length of the perpendicular from B to AC .		
b) What is the length of AC ?		
c) Calculate the area of the triangle .		
Concept 5 A 2 cm B		
For any positive numbers x , y the product \sqrt{x} $ imes$ \sqrt{y} $=$ \sqrt{z}		
can be written as the divisions $\ \ rac{\sqrt{z}}{\sqrt{x}} = \sqrt{y} \ \ , rac{\sqrt{z}}{\sqrt{y}} = \sqrt{x}$		

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<u>Activity</u>

Try these problems .

a)
$$\frac{\sqrt{12}}{\sqrt{6}}$$
 b) $\frac{\sqrt{24}}{\sqrt{8}}$

<u>Answer</u>

a) $\frac{\sqrt{12}}{\sqrt{6}} = \sqrt{2}$ **b)** $\frac{\sqrt{24}}{\sqrt{8}} = \sqrt{3}$

More activity

Try these problems .

a) $\frac{\sqrt{42}}{\sqrt{7}}$

 $\frac{\sqrt{90}}{\sqrt{18}}$

b)

PARALLEL LINES - 2

Concept -1

All angles with the same base and area have their third vertices on a line parallel to the base .

Conversely, all triangles with the same base and the third vertex on a line parallel to the

base have the same area.



In the figure $\langle A = 90^{\circ}$. D is a point on a line through C parallel to AB.

AB = 4 centimetres , BC = 5 centimetres.

a) What is the length of AC ?

b) Find the area of triangle ABC .

c) Find the area of triangle ABD .

<u>Answer</u>

a) In right triangle ABC ,

 $Base^2$ + Altitude² = hypotenuse² ==> AB^2 + AC^2 = BC^2 ==> 4^2 + AC^2 = 5^2

==> 16 + AC^2 = 25 ==> AC^2 = 25 - 16 = 9 ==> AC = $\sqrt{9}$ = 3 cm

b) Area of triangle ABC = $\frac{1}{2} \times a$ side \times altitude to that side = $\frac{1}{2} \times AB \times AC$

=
$$\frac{1}{2} \times 4 \times 3$$
 = 6 square centimetres.

c) Area of triangle ABD = Area of triangle ABC = 6 square centimetres .

<u>More activity</u>

Draw a circle and a triangle with one vertex at the centre of the circle and the other two

on the circle .Draw another triangle of the same area with all three vertices on the circle .

Concept -2

A line from the vertex of a triangle divides the length of the opposite side and the area of

the triangle in the same ratio .

Activity_

In the figure , area of triangle ABC is 100 square centimetres BD = 3 centimetres and

DC= 7 centimetres

a) Find the ratio of the areas of the triangles ABD and

ADC.

b) Find the area of triangle ABD .

c) Find the area of triangle ADC

<u>Answer</u>

a) Ratio of the areas of triangles ABD and ADC = BD : DC = 3 : 7

b) Area of triangle ABD = $\frac{3}{10} \times 100 = 30 \ sq. cm$

c) Area of triangle ADC = $\frac{7}{10} \times 100 = 70 \ sq. cm$

<u>More activity</u>

In the figure , area of triangle PQS is 10 square -

centimetres , area of triangle PST is 40 square -











AP : PB = 2 : 3

(Draw a line 7 centimetres long. Draw a line 5 centimetres long from one end and divide it into 2 centimetres and 3 centimetres .Now join the ends of the lines and draw a line parallel to it through the point of division of the shorter lines to cut longer line in the ratio 2:3

More activity

Draw a 11 centimetres long line and divide it in the ratio 2:3:4.

<u>Concept - 5</u>

If three or more parallel lines cut a line into equal parts , they will cut any any line into equal parts .

More activity

Divide a 8 centimetres long line into three equal parts .

<u>Concept - 6</u>

In any triangle , a line drawn parallel to a side cuts the other two sides in the same ratio .

<u>Activity</u>

Prove that a line drawn through the midpoint of a side of a triangle parallel to another side

passing through the midpoint of the third side .

<u>Answer</u>

In the figure P is the midpoint of AB and PQ is

parallel to BC .

$$=> \frac{AP}{PB} = \frac{AQ}{QC}$$

$$\frac{AQ}{QC} = 1 \qquad (AP = PB)$$

$$==> AQ = QC$$

That is , Q is the midpoint of AC .

More activity

In the figure , in triangle ABC , DE is parallel to BC

AD = 2 centimetres, DB = 3 centimetres,

AE = 4 centimetres.

a) $AE : EC = \dots : \dots$

b) What is the length of EC ?



C

A

Ρ

B

<u>Concept - 7</u>

A line which divides two sides of a triangle in the same ratio is parallel to the third side .

<u>Concept - 8</u>

The length of the line joining the midpoints of two sides of a triangle is half the length of

the third side

<u>Activity</u>

In the figure, P, Q and R are the midpoints of the

sides of triangle ABC . BC = 10 centimetres .

a) What is the length of PR?

b) Prove that BQRP is a parallelogram .

c) Find two more parallelograms from the figure .

<u>Answer</u>

a) $PR = \frac{BC}{2} = \frac{10}{2} = 5$ centimetres

b) PR = BQ and PR is parallel to BQ .

So BQRP is a parallelogram . (since a pair of opposite sides are equal and parallel)

```
c) QCRP , APQR
```

More activity

Prove that the quadrilateral formed by joining the midpoints of the sides of a quadrila -

teral is a parallelogram .

<u>Concept - 9</u>

In any triangle , ll the perpendiculars from the vertices to the opposite sides passes

through a single point .





SIMILAR TRIANGLES

Concept - 1

The sides of triangles with the same angles , taken in the order of size , are in the same ratio.

<u>Activity</u>



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Concept - 2

If the sides of two triangles are scaled by the same factor , then their angles are the same

Activity_

Draw a triangle of angles the same as those of the triangle shown the figure and sides scaled by 2. Answer



<u>More activity</u>

a) Draw a triangle of sides 3, 4, 6 centimetres.

b) Draw a triangle of angles the same as those of this triangle and sides scaled by $1\frac{1}{2}$

<u>Concept - 3</u>

In triangles with two sides scaled by the same factor and the angle between them the same

, the third side are also scaled by the same factor .

<u>Activity</u>

The picture shows two circles centred at O and two triangles

formed by joining the centre to the points of intersection of the

circles with two radii of the larger circle.

Prove that the triangles OPQ and OAB are similar .

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B

Answer

Take the radius of the smaller circle is r and the radius of the larger circle is R

 $\frac{OP}{OA} = \frac{r}{R}$ $\frac{OQ}{OB} = \frac{r}{R} \implies OP OA = OQ OB$ $\angle POQ = \angle AOB \text{ (common angle)}$ $\Longrightarrow \text{ Triangles OPQ and OAB are similar .}$ More activity In the figure AB = 6 centimetres , AP = 2 centimetres , AQ = 3 centimetres , AC = 9 centimetres .

Prove that the angles of the triangles APQ and ABC are the same .

NOTE :

For two triangles to be similar , they have to be related in one of the following ways .

- Having the same angles .
- Having scaled by the same factor .
- Having two sides scaled by the same factor and the angles between them equal.







Length of Chords

In a circle , the square of half a chord is the difference of the squares of the radius and

the perpendicular from the centre to the chord.

<u>Activity</u>

In a circle , a chord 8 centimetres away from the centre is 10 centimetres long . Compute

the length of the chord .

<u>Answer</u>

In right triangle BOC ,

 $Base^2$ + Altitude² = Hypotenuse² ==> BC^2 + OC^2 = OB^2

==> BC^2 + 8^2 = 10^2 ==> BC^2 + 64 = 100==> BC^2 = 100 - 64 =36 ==> BC = $\sqrt{36}$ = 6 cm



Length of the chord = $2 \times BC$ = $2 \times 6 = 12 \ cm$

More activity

In a circle of radius 5 centimetres , two parallel chords of lengths 6 and 8 centimetres are

drawn on either side of the a diameter.

a) What is the distance between the parallel chords ?

b) If parallel chords are drawn on the same side of the diameter , what would be the

distance between them ?

POINTS AND CIRCLES

We can draw so many circles through a point

We can draw so many circles through two points

If three points are on a line , we cannot draw a circle passing through all these points

<u>Concept - 7</u>

In any triangle , the perpendicular bisectors of all three sides intersect at a single point

If three points are not on a line , we can draw only one circle through these points

Circumcircle of a triangle

A circle passing through all three vertices of a triangle is called the circumcircle of the

triangle.

The centre of the circumcircle of a triangle is the point of intersection of the perpendicul-

ar bisectors of the sides .



NOTE :

. The circumcentre of a right triangle is the midpoint of its hypotenuse .

<u>ARC</u>

Any part of a circle between two points on it is called an arc .

Central angle of an arc

The angle between two radii joining the ends of an arc to the centre of the circle

is called the central angle of the arc .



<u>Sector</u>

An arc and the radii through its ends enclose a part of the area of the circle . Such a piece

of a circle is called a sector





<u>Activity</u>

Radius of a circle is 5 centimetres.

a) Calculate its perimeter.

b) Calculate its area .

<u>Answer</u>

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a) Perimeter =
$$2\pi r = 2\pi \times 5 = 10 \pi$$
 cm
b) Area = $\pi r^2 = \pi \times 5^2 = 25 \pi$ sq.cm
More activity
A circle is drawn inside a square as shown in the figure .
Length of the side of a square is 6 centimetres .
a) Find the radius of the circle .
b) Calculate the perimeter of the circle .
b) Calculate the area of the circle .
concept 3
Length of an arc.
The length of an arc is that fraction of the perimeter of the circle as the fraction of
360° that its central angle is .
Concept 4
Area of a sector.
The area of a sector is that fraction of the area of the circle as the fraction of 360° that
its central angle is .
In a circle of radius r ,
a) the length of an arc of central angle x^0 is $2\pi r \times \frac{x}{360}$
b) the area of a sector of central angle x^0 is $\pi r^2 \times \frac{x}{360}$
b) the area of a sector of central angle x^0 is $\pi r^2 \times \frac{x}{360}$

<u>Activity</u>

In a circle of radius 6 centimetres ,

a) What is the length of an arc of central angle 120° ?

b) What is the area of a sector of central angle 120°?

<u>Answer</u>

a) Length of the arc = $2\pi \times 6 \times \frac{120}{360} = 4\pi \ cm$

b) Area of the sector = $\pi \times 6^2 \times \frac{120}{360} = \pi \times 36 \times \frac{120}{360} = 12 \pi \ sq. \ cm$

<u>More activity</u>

In a circle , the length of an arc of central angle 60° is 6π cm

a) Calculate the perimeter of the circle .

b) Calculate the radius of the circle .

c) What is the area of a sector of central angle 60° ?

PRISMS

Solids

Geometrical objects having spreads and vertical heights are called solids (Three

dimensional objects)

Prisms

Geometrical objects having two identical polygons and rectangles of the same height,

with the polygons as opposite sides are called **prisms** .

Faces of a prism

The polygons and rectangles in a prism are called its faces .

The polygons on the top and bottom are called bases and the rectangles are called lateral faces .

Depending on the shape of the bases , they are named

<u>Concept 1</u>

Volume of a prism

The volume of any prism is the product of its base area and height .

Volume = Base area x Height

<u>Activity</u>

The base of a prism is a square of side 20 centimetres and its height 30 centimetres .

a) Calculate the volume of the prism .

b) How much litres of water can be contained in this prism ?

<u>Answer</u>

a) Volume = Base area x height = $20 \times 20 \times 30 = 12000$ cubic cm

b)

 $\frac{12000}{1000}$ = 12 litres

<u>More activity</u>

The base of a prism is an equilateral triangle of perimeter 12 centimetres and its height is

9 centimetres .

a) What is the length of its base edge ?

b) Calculate the volume of the prism .

<u>Concept 2</u>

Lateral surface area

The lateral surface area of any prism is the product of the base perimeter and height

Lateral surface area = Base perimeter x Height

NOTE :

For a closed prism , the total surface area can be calculated by adding the base areas to

the lateral surface area .

<u>Activity</u>

The base of a prism is a rectangle of length 10 centimetres and breadth 8 centimetres and

its height is 15 centimetres .

a) Calculate its base perimeter .

b) Calculate its lateral surface area .

c) Calculate its total surface area .

<u>Answer</u>

a) Base perimeter = $2 \times (10 + 8) = 2 \times 18 = 36 \ cm$

- **b)** Lateral surface area = Base perimeter x Height = $36 \times 15 = 540$ sq. cm
- c) Total surface area = Lateral surface area + 2 x Base area

 $= 540 + 2 \times 10 \times 8 = 540 + 160 = 700 \, sq.cm$

<u>More activity</u>

The base area of a square prism is 100 square centimetres and its height 8 centimetres .

- a) What is the length of its base edge ?
- b) Calculate its lateral surface area .
- c) Calculate its total surface area .

CYLINDER

Solids with circles at both ends and a smoothly curving surface all around are called

cylinders.



Concept 3

Volume of a cylinder

The volume of a cylinder is the product of its base area and height .

<u>Activity</u>

The base perimeter of a cylinder is 18π centimetres and its height is 20 centimetres .

a) What is its base radius ?

b) Calculate the volume of the cylinder .

<u>Answer</u>

a) Base perimeter = 18π cm ==> $2\pi r = 18\pi$ ==> $r = \frac{18\pi}{2\pi} = 9$ cm

b) Volume = Base area x Height = $\pi \times 9^2 \times 20 = 1620 \pi$ cubic.cm

More activity

The base of a rectangular block of wood is a square of side 10 centimetres and its height is

25 centimetres . A largest cylinder is carved out of this .

a) What are the base radius and height of the cylinder ?

b) Calculate the volume of the cylinder .

<u>Concept 4</u>

Curved surface area of a cylinder

The curved surface area of a cylinder is the product of the base perimeter and height .

NOTE :

For a closed cylinder , the total surface area can be calculated by adding the base areas to

the curved surface area.

<u>Activity</u>

The base diameter of a solid cylinder is 10 centimetres and its height is 12 centimetres .

a) What is its base radius ?

b) Calculate its curved surface area .

c) Calculate its total surface area .

<u>Answer</u>

a) Base radius = $\frac{10}{2}$ = 5 cm

b) Curved surface area = Base perimeter x Height = $2\pi \times 5 \times 12 = 120\pi$ sq. cm

c) Total surface area = Curved surface area + 2 x Base area

= $120 \pi + 2 \times \pi \times 5^2$ = $120 \pi + 50 \pi$ = $170 \pi sq.cm$

<u>More activity</u>

The inner diameter of a well is 3 metres and it is 8 metres deep .

a) What is the base perimeter of the well ?

b) Calculate the curved surface area of the inside of the well ?

c) What would be the cost cementing its inside at 400rupees per square metre ?

PROPORTION

Equality of ratios is called proportion

<u>Concept 1</u>

Direct proportion

Let's take an independent quantity as x and the dependent quantity y . If y is always x

multiplied by a fixed quantity $k \,$ (which does not change with x) $\,$, then we can write

the relation between them as y = kx . Then the ratio of **x** to **y** remains unchanged as 1:k

That is , y changes proportional to x . This proportion is known as direct proportion .

Constant of proportionality

The fixed number occurring in the equation of proportional change is called the constant of proportionality .

<u>Activity</u>

- a) Prove that the perimeter of a square varies proportional as the length of a side .
- b) What is the constant of proportionality here ?

<u>Answer</u>

a) In any square ,the perimeter is 4 times the length of a side .

That is , in any square , the ratio of the length of a side to the perimeter is 1 : 4

That is , the length of a side and perimeter of a square are scaled by the same factor .

That is perimeter of a square varies proportionally as the the length of a square .

b) If the length of a side of a square is x and its perimeter is y, then y = 4x

Constant of proportionality = 4

a) Prove that the perimeter of a circle varies proportional as the radius .

b) What is the constant of proportionality here ?

<u>Concept 2</u>

Inverse proportion

Let's take an independent quantity as x and the dependent quantity y. If y is always a quotient obtained by dividing a fixed quantity k by x (k does not change with x), then we can write the relation between them as $y = \frac{k}{x}$. That is, y changes proportio - nal to the reciprocal of x. This proportion is known as inverse proportion.

<u>Activity</u>

For any regular polygon , we can draw a circle through all vertices .

a) Prove that for regular polygons , angle made by two adjacent vertices at the centre of the circle passing through all the vertices is inversely proportional to the number of sides

b) What is the the constant of proportionality here ?

<u>Answer</u>

Regular polygon	Number of sides	Angle made by two adjacent vertices
0 1 00		at the centre of the circle .
	3	$\frac{360}{120^{\circ}}$ = 120°
Equilateral triangle		3
	4	$\frac{360}{2} = 90^{\circ}$
Square		4 - 50
	5	$\frac{360}{2} = 72^{\circ}$
Regular pentagon		5 7 2
	6	$\frac{360}{2} = 60^{\circ}$
Regular hexagon		6 - 55

If the number of sides is x and the measure of the angle made by two adjacent vertices

at the centre of the circle is y, then $y = \frac{360}{x}$

That is, $y = 360 \times \frac{1}{x}$

Here y is proportional to the reciprocal of x .

b) Constant of proportionality = 360

<u>More activity</u>

An object travelling from one one point to a point 100 metres away at a steady speed along a straight line .

- a) Prove that the speed of the object is inversely proportional to the time taken to reach the destination .
- b) What is the the constant of proportionality here ?

REAL NUMBERS

The natural numbers, tractions and their negatives with zero as well are collectively

called rational numbers. All other umbers are called irrational numbers.

General form of a rational number

All rational numbers have a common form $\frac{x}{y}$ where x and y are natural numbers or

their negatives with x possibly zero also.

Real numbers

The rational and irrational numbers together are called *real numbers*.

Number line

Mark a point on a line and denote it as zero. Mark one more point on this line. Taking the distance from the first point to the second as 1 (the unit of length), we can write the distances to all other points on the right as numbers .To mark distances to all points, we need irrational numbers also . To mark the numbers to the left of the first point (0), we use the the negative of the numbers to the right. Thus, all points on this line can be marked using real numbers . On the other hand , all real numbers can be seen as the points on this line . Such a line is called *number line* or *real line* .



For any two real numbers , the position of the larger number on the number line is to the

right of the smaller number .

<u>Concept 1</u>

The distance between any two points on the number line is the smaller of the numbers

denoting them subtracted from the larger .

<u>Concept 2</u>

The midpoint of two points on the number line is that point denoted by half the sum of the

numbers denoting these points .

<u>Activity</u>

Find the distance between the two points on the number line , denoted by each pair of

numbers given below .

a) 3, -7b) -9, -1Answer a) Distance = 3 - (-7) = 3 + 7 = 10Midpoint = $\frac{3 + (-7)}{2} = \frac{-4}{2} = -2$ b) Distance = -1 - (-9) = -1 + 9 = 8Midpoint = $\frac{-9 + (-1)}{2} = \frac{-10}{2} = -5$ More activity Find the distance between the two points on the number line, denoted by each pair of numbers given below. a) -16, 4b) -11, -25

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Concept 3

On the number line , the distance between the point denoted by 0 and point denoted by

another number is the *absolute value* of that number.

$$|x| = \begin{cases} x, & \text{if } x > 0 \\ -x, & \text{if } x < 0 \\ 0, & \text{if } x = 0 \end{cases}$$

Concept 4

The distance between two points on the number line is the absolute value of the difference

of the numbers denoting these points .

The distance between two points denoted by the numbers **x** and **y** on the number line is

|x - y|

<u>Activity</u>

Find x satisfying the equation , |x-1| = |x-3|

<u>Answer</u>

$$x = \frac{1+3}{2} = \frac{4}{2} = 2$$

More activity

Find x satisfying each of the equations below .

- a) |x-2| = |x-8|
- b) |x+3| = |x+7|

POLYNOMIALS

Look at the algebraic expressions given below

 $x^2 + 5x + 6$ $x^3 + 6x^2 + 11x + 6$ 49 - 9.8x

In all these, the only mathematical operations involved are multiplying different powers of the number x by various numbers and adding or subtracting them .A definite number is also sometimes added or subtracted . An algebraic expression involving such operations is called a *polynomial*.

<u>Note :</u>

Features of polynomials

Various powers of the changing number .

All powers are natural numbers .

Powers of the changing number are multiplied by definite numbers .

Sum or difference of the products are found .

A definite number is added or subtracted .

Note :

Algebraic expressions involving the operations of taking reciprocal or square root of

the changing number are not polynomials .

 $[\]boldsymbol{x}$ is a changing number .

Degree of a polynomial

In a polynomial, we take powers of the changing numbers. The largest power used is

called the *degree* of the polynomial.

General form of a polynomial

Based on the degree , we can write the general forms of the polynomials .

Polynomial	General form
First degree polynomial	ax + b
Second degree polynomial	$ax^2 + bx + c$
Third degree polynomial	$ax^3 + bx^2 + cx + d$

Here the letters a , b , c and d denote fixed numbers (definite numbers).

They can be any sort of numbers (natural numbers, fractions, numbers which are not fractions or negative numbers). They are called *coefficients* in a polynomial.

<u>Activity</u>

Find p(0), p(1) and p(-1) in the following polynomials.

a) p(x) = 2x + 3 **b)** $p(x) = x^2 + 5x + 6$

Answer

a) p(x) = 2x + 3 $p(0) = 2 \times 0 + 3 = 0 + 3 = 3$ $p(1) = 2 \times 1 + 3 = 2 + 3 = 5$ $p(-1) = 2 \times (-1) + 3 = -2 + 3 = 1$

b)
$$p(x) = x^2 + 5x + 6$$

 $p(0) = 0^2 + 5 \times 0 + 6 = 0 + 0 + 6 = 6$
 $p(1) = 1^2 + 5 \times 1 + 6 = 1 + 5 + 6 = 12$
 $p(-1) = (-1)^2 + 5 \times (-1) + 6 = 1 - 5 + 6 = 2$

<u>More activity</u>

Find p(0) , p(1) and p(-2) in the following polynomials .

a) $p(x) = x^2 + 7x + 10$ **b)** $p(x) = x^2 - 2x - 8$
STATISTICS

Frequency table

<u>Activity</u>

The scores of 45 children in a test are given below .

8	7	6	3	8	8	7	7	6
7	9	7	6	8	7	2	6	7
10	6	7	3	9	5	4	5	4
4	4	5	8	10	8	8	9	7
7	6	8	8	7	4	5	9	8

Make a frequency table .

<u>Answer</u>

Score	Number of children (frequency)
2	1
3	2
4	5
5	4
6	6
7	11
8	10
9	4
10	2
Total	45

More activity

The number of members in 50 households of a village are listed below .

8	6	9	4	4	2	6	4	5	3
7	3	3	2	3	7	6	3	2	5
5	13	9	9	7	4	4	5	4	3
3	7	2	3	3	10	8	6	6	4
2	4	5	4	3	8	7	5	6	3

Make a frequency table .

Frequency table with classes

<u>Activity</u>

The runs that a batsman got in 50 one-day cricket matches are given below .

50	0	49	60	100	68	27	48	15	65
101	45	2	52	25	18	29	53	72	90
32	81	28	104	35	49	2	60	87	71
68	20	10	30	55	47	21	35	12	20
38	102	35	11	27	43	38	40	48	71

Make a frequency table .

<u>Answer</u>

Runs	Number of matches (frequency)
0 - 10	3
10 - 20	6
20 - 30	7
30 - 40	7
40 - 50	8
50 - 60	4
60 - 70	5
70 - 80	3
80 - 90	2
90 - 100	1
100 - 110	4

More activity

The weights of the members of the school Health club are given below .

38	39	41	59	48	48	38	58	50	55
39	40	41	49	32	43	45	53	37	44
51	52	33	46	55	36	45	47	43	33

Make a frequency table with the length of the class interval 5

(Hint : Take classes as 30 - 35 , 35 - 40 ,...)

Histogram

<u>Activity</u>

The table below gives the amount of water 28 households use . Draw a histogram .

Amount of water (litres)	Number of households
0 - 500	2
500 - 1000	5
1000 - 1500	10
1500 - 2000	8
2000 - 2500	3

<u>Answer</u>



Note :

In the figure above , the classes are marked on the horizontal line and the frequencies on the vertical line .The width of each rectangle shows the length of the class interval and its height shows the frequency .Such a picture is called a *histogram*.

More activity

Detail of rainfall in June and July are given in the table below . Draw a histogram .

Rainfall (mm)	Number of days
0 - 10	1
10 - 20	4
20 - 30	7
30 - 40	9
40 - 50	15
50 - 60	10
60 - 70	9
70 - 80	6

ARITHMETIC MEAN

The average of any set of numbers between two fixed numbers is also between these two numbers

The number got by dividing the sum by the number (which we usually call average) called *arithmetic mean* or simply *mean*.

<u>Activity</u>

The table shows the labourers in a factory sorted according to their daily wages .

Daily wage (Rs)	Number of workers
300	2
350	4
400	6
450	4
500	4

What is the average daily wage in this factory ?

<u>Answer</u>

Daily wage (Rs)	Number of workers	Total wages (Rs)
300	2	$300 \times 2 = 600$
350	4	$350 \times 4 = 1400$
400	6	$400 \times 6 = 2400$
450	4	$4500 \times 4 = 1800$
500	4	$500 \times 4 = 2000$
Total	20	8200

Average daily wage = $\frac{8200}{20}$ = 410 Rs

<u>More activity</u>

The table shows the children in a class ,sorted according to the marks they got for a maths

test .

Mark	Number of children
2	1
3	2
4	5
5	4
6	6
7	11
8	10
9	4
10	2

Calculate the average mark of the class .

<u>Activity</u>

The table shows the labourers in a factory sorted according to their daily wages .

Daily wages (Rs)	Number of workers
300 - 400	8
400 - 500	6
500 - 600	14
600 - 700	10
700 - 800	7
800 - 900	5

What is the average daily wage in this factory ?

Daily wages (Rs)	Number of workers	Mid value of the class	Total wages (Rs)
300 - 400	8	$\frac{300+400}{2} = 350$	$350 \times 8 = 2800$
400 - 500	6	$\frac{400+500}{2} = 450$	$450 \times 6 = 2700$
500 - 600	14	$\frac{500+600}{2} = 550$	$550 \times 14 = 7700$
600 - 700	10	$\frac{600+700}{2} = 650$	$650 \times 10 = 6500$
700 - 800	7	$\frac{700+800}{2} = 850$	$750 \times 7 = 5250$
800 - 900	5	$\frac{800+900}{2} = 850$	$850 \times 5 = 4250$
Total	50	C.X.	29200

Average daily wage =

 $\frac{29200}{50} = 584 \ Rs$

<u>More activity</u>

The table below shows the children in a class , sorted according to their heights .

Height (cm)	Number of children	
148 – 152	8	
152 – 156	10	
156 - 160	15	
160 - 164	10	
164 - 168	7	

What is the mean height of a child in this class ?