WANDOOR GANITHAM - S S L C MODEL QUESTION PAPER 2021

PREE4
DETAILED ANSWER KEY - QUESTION PAPER 4

| Qn no. | Key |
| :---: | :---: |
| For questions from 1 to 5 one score each . |  |
| 1 | What is the common difference of the arithmetic sequence $\mathbf{6 , 1 0 , 1 4}$ $\qquad$ ? $(6,4,2,8)$ |
|  | Answer . $4$ |
| 2 | In the figure $O$ is the centre of the circle and $\angle A O B=100{ }^{\circ}$. <br> What is the measure of $<$ ACB ? $\left(50^{\circ}, \mathbf{8 0}^{\circ}, 130^{\circ}, 200^{\circ}\right)$ |
|  | Answer . $50^{\circ}$ |
| 3 | If $\sin x^{0}=\cos x^{0}$,find the value of $\mathbf{x}$ ? $(0,30,45,60)$ |
|  | Answer . $45$ |
| 4 | A line is drawn through the point $(3,2)$ parallel to the x -axis . If $(5, k)$ is a point on this line, what is the value of $k$ ? $(0,1,2,3)$ |
|  | Answer . <br> 2 |
| 5 | Which among the following is added to $x^{2}+36$ to get a perfect square ? $(6 x, 18 x, 12 x, 36 x)$ |
|  | Answer . $12 x$ |

6 Algebraic form of an arithmetic sequence is 4n-1.
a) What is its common difference ?
b) What is its first term ?

Answer .
a) Common difference $=4$
b) First term $=4-1=3$

7 Write $x^{2}-64$ as the product of two first degree polynomials ?

Answer.
a) $x^{2}-64=x^{2}-8^{2}=(x+8)(x-8)$

8 In the figure $P Q$ is the diameter of the semicircle.
The measures of $<\mathrm{R},<\mathrm{S}$ and $<\mathrm{T}$ are in arithmetic sequence. $<\mathbf{T}=60^{\circ}$
a) What is the measure of <S ?

b) What is the measure of $<\mathbf{R}$ ?

Answer .
a) $\angle \mathrm{S}=90^{\circ}$ ( common difference $=90-60=30$ )
b) $<\mathbf{R}=\mathbf{9 0}+\mathbf{3 0 = 1 2 0}{ }^{\circ}$

9 The base radius of a cone is 12 centimetres and its slant height is 20 centimetres
a) What is its height ?
b) Compute its volume ?

Answer .
a) $r^{2}+h^{2}=l^{2}==>12^{2}+h^{2}=20^{2}==>\quad 144+h^{2}=400==>h^{2}=400-144=256==.>$

$$
h=\sqrt{256}=16 \mathrm{~cm}
$$

|  | b) Volume $=\frac{1}{3} \times \pi \times r^{2} \times h=\frac{1}{3} \times \pi \times 12^{2} \times 16=768 \pi \mathrm{~cm}^{3}$ |
| :---: | :---: |
| 10 | In the figure PQRS is a parallelogram . <br> a) What are the coordinates of $\mathbf{P}$ ? <br> b) What are the coordinates of the point of intersection of its diagonals ? |
|  | Answer . <br> a ) $(6+4-9,2+6-5)=(1,3)$ <br> b) $\left(\frac{6+4}{2}, \frac{2+6}{2}\right)=\left(\frac{10}{2}, \frac{8}{2}\right)=(5,4)$ <br> ( Diagonals of a parallelogram bisect each other ) |
| For questions from 11 to 20 carries 3 scores each . |  |
| 11 | Draw a triangle of circumradius 4 cm and two of the angles $70^{\circ}$ and $80{ }^{\circ}$. |
|  | Answer. |

12 Find the following sums .
a) $1+2+3+4+5+\ldots . \ldots \ldots+40$
b) $2+4+6+8+10+\ldots \ldots \ldots+80$
c) $1+3+5+7+9+\ldots \ldots \ldots+79$

Answer .
a) $1+2+3+4+5+\ldots \ldots \ldots+40=\frac{40 \times 41}{2}=820$
b) $2+4+6+8+\mathbf{1 0}+\ldots \ldots \ldots+80=2 \times 820=1640$
c) $1+3+5+7+9+\ldots \ldots \ldots+79=1640-40=1600$

13 Consider the polynomial $p(x)=x^{2}-5 x+4$
a) Find $p(1) \quad$ ?
b) Check whether $\quad x-4$ is a factor of $p(x)$ ?
c) Write $\quad p(x)$ as the product of two first degree polynomials ?

Answer .
a) $p(1)=1^{2}-5 \times 1+4=1-5+4=0$
b) $p(4)=4^{2}-5 \times 4+4=16-20+4=0==>\mathbf{x}-4$ is a factor $\mathbf{o f} \mathbf{p}(\mathbf{x})$
c) $(x-1)(x-4)$

14 A dice with faces numbered from 1 to 6 is rolled .
a ) What is the probability of getting an even number ?
b ) What is the probability of getting an odd number ?
c) What is the probability of getting a prime number ?

Answer .
a ) $\frac{\text { Number of favourable results }}{\text { Total number of results }}=\frac{3}{6}=\frac{1}{2}$
( Total results = 1, $2,3,4,5,6$, favourable results = $2,4,6$ )
b) $\frac{\text { Number of favourable results }}{\text { Totalnumber of results }}=\frac{3}{6}=\frac{1}{2}$
( favourable results $=1,3,5$ )
c) $\frac{\text { Number of favourable results }}{\text { Total number of results }}=\frac{3}{6}=\frac{1}{2} \quad$ ( favourable results $=2,3,5$ )

15 The number of pictures drawn by the arts club members of a school are given below.

$$
15,39,30,42,27,33,24,18,36,21
$$

a) What is the mean of the number of pictures?
b) What is the median of the number of pictures?

Answer .
a ) $\quad$ Mean $=\frac{15+39+30+42+27+33+24+18+36+21}{10}=\frac{285}{10}=28.5$
b) $15,18,21,24,27,30,33,36,39,42$

Median $=\frac{27+30}{2}=\frac{57}{2}=28.5$
16 Two children stand on either side of a flag post of height 50 meters . First child sees the top of the flag post at an elevation of $45^{\circ}$ and the second child sees it at an elevation of $3 \mathbf{0}^{\mathbf{0}}$
a) Draw a rough figure based on the given details?
b) What is the distance between the flag post and the first child ?
c) What is the distance between the flag post and the second child ?

Answer .
a)

b ) Distance between the flag post and the first child $=50 \mathrm{~m}$

c) Distance between the flag post and the second child $=50 \sqrt{3} \mathrm{~m}$

17 The base radii of two cones are in the ratio $3: 4$ and their slant heights are in the ratio 5: 6
a) If the radius of the first cone is taken as $3 r$, what will be the radius of the second cone ?
b) What is the ratio of their curved surface areas ?
c) If the curved surface area of the first cone is $300 \pi$ square centimetres, what will be the curved surface area of the second cone ?

Answer .
a) Radius of the second cone $=4 \mathrm{r}$
b) $\pi \times 3 r \times 5 l: \pi \times 4 r \times 6 l=15 \pi l: 24 \pi l=15: 24=5: 8$
c) Curved surface area of the second cone $=\frac{8}{5} \times 300 \pi=480 \pi \mathrm{~cm}^{2}$

18 Consider the line passing through the points $A$ and $B$ in the picture .
a) What is the slope of the line ?
b) Write the coordinates of another point on this line
c) If $(x, y)$ is point on this line, prove that $x+y=4$


Answer.
a ) Slope $=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}=\frac{0-4}{4-0}=\frac{-4}{4}=-1$
b) $\left(\frac{0+4}{2}, \frac{4+0}{2}\right)=\left(\frac{4}{2}, \frac{4}{2}\right)=(2,2)$ or any point $(x, y)$ with $x+y=4$
c) $\frac{y-0}{x-4}=-1==>\quad y=-1(x-4)==>\quad y=-x+4==>y+x=4$

|  | $\frac{y-4}{x-0}=-1==>\quad y-4=-x==>\quad y+x=4$ |
| :---: | :---: |
| 19 | Draw a circle of radius 3 cm and mark a point 7 cm away from its centre. Draw the tangents to the circle from this point . |
|  | Answer . |
| 20 | When each side of a square was decreased by 5 metres , the area became 225 square metres. <br> a) Write a second degree equation by taking the side of the original square as $\boldsymbol{x}$ <br> b) What was the length of a side of the original square ? |

## Answer .

a ) $(x-5)^{2}=225$
b) $x-5=\sqrt{225}=15$
$x=15+5=20$
Length of a side of the original square $=20 \mathrm{~m}$

For questions from 21 to 30 carries 4 scores each .

21 Draw a rectangle of width 7 cm and height $\mathbf{3 c m}$. Draw a square of the same area .

Answer .


22
Consider the following number patterns .

1
23

456
$\begin{array}{llll}7 & 8 & 9 & 10\end{array}$
......................................
................................................
( pattern 1)

4
$7 \quad 10$
$\begin{array}{lll}13 & 16 & 19\end{array}$
$\begin{array}{llll}22 & 25 & 28 & 31\end{array}$
.....................................
$\qquad$
( pattern 2 )

|  | pattern 1 | pattern 2 |
| :--- | :--- | :--- |
| Next line of the number patterns | a) ...................... | b)....................... |
| Last number in $10^{\text {th }}$ line | c) ....................... | d) ....................... |


|  | Answer . |
| :---: | :---: |
|  | pattern 1 pattern 2 |
|  | a) $\begin{array}{llllllllll}11 & 12 & 13 & 14 & 15 & \text { b) } 34 & 37 & 40 & 43 & 46\end{array}$ |
|  | c) $\frac{10 \times 11}{2}=55$ d) $3 \times 55+1=165+1=166$ |
| 23 | A bag contains 25 white and 35 green beads. Take one bead from this <br> a ) What is the probability of getting a green bead ? <br> b) What is the probability of getting a white bead? <br> c) How many more white beads are to be put in the box to make the probability of getting a green bead is $\frac{5}{9}$ ? <br> Answer. <br> a ) Probability of getting a green bead $=\frac{\text { Number of favourable results }}{\text { Total number of results }}=\frac{35}{60}$ <br> b ) Probability of getting a white bead $=\frac{\text { Number of favourable results }}{\text { Total number of results }}=\frac{25}{60}$ <br> c) $\frac{35}{x}=\frac{5}{9} \quad==>\quad x=63$ <br> Number of white beads more added $=63-60=3$ |
| 24 | $A$ line is drawn by joining the points $A(3,6)$ and $B(7,6)$. <br> a) What are the coordinates of the midpoint of the line ? <br> b) Write the coordinates of another two points on this line ? <br> c) What are the coordinates of the point on the $x$-axis which is equidistant from the ends of the line $A B$ ? |


|  | Answer . <br> a) $\left(\frac{3+7}{2}, \frac{6+6}{2}\right)=\left(\frac{10}{2}, \frac{12}{2}\right)=(5,6)$ <br> b) $(5,1),(5,2)$ or any two pints with $\mathbf{x}$ coordinate 5 . <br> ( Since the $y$ coordinates of $A$ and $B$ are equal, the line $A B$ is parallel to the $x$-axis . <br> So the perpendicular bisector of AB is parallel to the y -axis ) <br> c) $(5,0)$ <br> (Any point on the perpendicular bisector of a line is equidistant from its ends ) |
| :---: | :---: |
| 25 | Consider the polynomial $p(x)=x^{2}+9 x+8$ <br> a) Find $p(1)$ ? <br> b) Write a factor of $p(x)-p(1) \quad$ ? <br> c) Write $p(x)-p(1)$ as the product of two first degree polynomials ? |
|  | Answer . <br> a) $p(1)=1^{2}+9 \times 1+8=1+9+8=18$ <br> b) $x-1$ <br> c) $\quad p(x)-p(1)=x^{2}+9 x+8-18=x^{2}+9 x-10$ $x^{2}+9 x-10=(x-1)(x+10)$ |
| 26 | In triangle $P Q R, \quad<Q=90^{\circ},<R=x^{0}$ and the length of the sides $Q R, P Q, P R$ are $a, b, c$ respectively. <br> a) Which among the following is $\tan x^{0} \quad$ ? $\left(\frac{b}{c}, \frac{a}{c}, \frac{b}{a}, \frac{a}{b}\right)$ <br> b) Similarly write $\sin x^{0}$ and $\cos x^{0}$ from this triangle ? <br> c) Prove that $\frac{\sin x^{0}}{\cos x^{0}}=\tan x^{0} \quad$ ? |


|  | a) $\tan x^{0}=\frac{b}{a}$ <br> b) $\quad \sin x^{0}=\frac{b}{c} \quad, \quad \cos x^{0}=\frac{a}{c}$ <br> c) $\frac{\sin x^{0}}{\cos x^{0}}=\frac{b}{c} \div \frac{a}{c}=\frac{b}{c} \times \frac{c}{a}=\frac{b}{a}=\tan x^{0}$ |  |  |
| :---: | :---: | :---: | :---: |
| 27 | In the figure line $O A$ makes an angle $45^{\circ}$ with the x -axis . <br> a) What are the coordinates of $O$ ? <br> b)What is the slope of the line $O A$ ? <br> c) Write the coordinates of another two point this line other than the origin ? | $X^{\prime}$ $\bar{O}$ |  |
|  | Answer . <br> a) $(0,0)$ <br> b) Slope $=\tan 45^{\circ}=1$ <br> c) $(1,1),(2,2)$ or any two points | $\text { with } x=y$ |  |
| 28 | Workers in a factory are sorted according to their daily wage in the table below . |  |  |
|  | Daily wage (Rs) | Number of workers |  |
|  | 900 | 5 |  |
|  | 1000 | 7 |  |
|  | 1250 | 10 |  |
|  | 1500 | 11 |  |
|  | 1750 | 8 |  |
|  | 2000 | 6 |  |



|  | Answer . <br> a) Radius of the sector $=$ Slant height of the cone $=15 \mathrm{~cm}$ <br> b ) Base perimeter of the cone $=$ Arc length of the sector $=10 \pi \mathrm{~cm}$ <br> c) Base radius of the cone $=\frac{10 \pi}{2 \pi}=5 \mathrm{~cm}$ <br> d) $\frac{x}{360}=\frac{5}{15} \quad==>\quad x=\frac{5 \times 360}{15}=120^{\circ}$ <br> Central angle of the sector $=120^{\circ}$ |
| :---: | :---: |
| 30 | The sum of the square of a number and 8 times that number is 240 . <br> a) Write a second degree equation by taking the number as $\boldsymbol{x}$ <br> b) Find the number ? |
|  | Answer . <br> a) $x^{2}+8 x=240$ <br> b ) $x^{2}+8 x+4^{2}=240+4^{2}==>(x+4)^{2}=256$ $\begin{aligned} & x+4=\sqrt{256}=16 \quad==>\quad x=16-4=12 \\ & \text { Number }=12 \end{aligned}$ |
|  | For questions from 31 to 45 carries 5 scores each . |
| 31 | In the figure $\mathbf{O}$ is the centre of the circle. The circle touches the sides of the triangle at the points $P, Q$ and $R$ $<\mathrm{ABC}=45^{\circ}$ <br> a ) What is the measure of < POQ ? <br> b) Draw a circle of radius $\mathbf{3} \mathbf{~ c m}$. Draw a triangle of angles $45^{\circ}, 55^{\circ}, 80^{\circ}$ with all its sides touching this circle |

Answer .
a ) $<\mathbf{P O Q}=180-45=135^{0}$ ( In a circle, the angles between the radii through two points and the angle between the tangents at these points are supplementary )


32 The sum of first 9 terms of an arithmetic sequence is 189 and the sum of first 4 terms is 44 .
a) What is its fifth term ?
b) What is the sum of first 5 terms of this sequence ?
c) What is its third term ?
d) What is its common difference ?
e) What is its algebraic form ?

Answer .
a) $\quad x_{5}=\frac{189}{9}=21$
b) $S_{5}=S_{4}+x_{5}=44+21=65$
c) $x_{3}=\frac{65}{5}=13$

|  | d) common difference $=\frac{\text { Term difference }}{\text { position difference }}=\frac{21-13}{5-3}=\frac{8}{2}=4$ <br> e) $x_{1}=x_{5}-4 d=21-4 \times 4=21-16=5$ <br> Algebraic form $=d n+f-d=4 n+5-4=4 n+1$ |
| :---: | :---: |
| 33 | a) Draw the axes and mark the points $A(1,2), B(6,2), C(6,5)$ and $D(1,5)$ <br> b) Write the most suitable name for the quadrilateral ABCD ? <br> c) Find its perimeter ? |
|  | Answer . <br> a) <br> b) Rectangle <br> c) Perimeter $=2 \times 5+2 \times 3=10+6=16 \mathrm{~cm}$ |
| 34 | In the figure the circle touches the sides of the triangle at $P, Q$ and $R . A P=5 \mathrm{~cm}, B Q=4 \mathrm{~cm}, C R=3 \mathrm{~cm}$ $B Q=4 \mathrm{~cm}, C R=3 \mathrm{~cm}$. <br> a) What is the length of AR ? <br> b) What is the length of BC ? <br> c) What is the perimeter of the triangle ABC ? |



|  | Answer . <br> a) Common difference $=5$ <br> b ) Smallest number $=11$ <br> Largest number $=96$ <br> c) Algebraic form $=d n+f-d=5 n+11-5=5 n+6$ <br> d) $x_{n}=96==>5 n+6=96$ $5 n=96-6=90==>n=\frac{90}{5}=18$ |
| :---: | :---: |
| 37 | In the figure midpoints of the sides of the quadrilateral $A B C D$ are $P, Q, R$ and $S$ ? <br> a) What is the most suitable name of the quadrilateral PQRS ? <br> b) What are the coordinates of S , B , C and D <br> Answer. <br> a ) Parallelogram <br> b) Coordinates of $\mathbf{S}=(7+4-8,2+6-5)=(3,3)$ <br> c) Coordinates of $\mathbf{B}=(9,3)$ <br> Coordinates of $\mathbf{C}=(7,7)$ <br> Coordinates of $\mathbf{D}=(1,5)$ |
| 38 | The base radius and height of a solid metal cone are 5 centimetres and 12 centimetres <br> a) What is its slant height ? <br> b) What is its surface area ? <br> c) If $\mathbf{1 0 0 0 0}$ such cones are painted and cost of the painting is $\mathbf{1 0}$ rupees per square metre, what will be the total cost ? ( hint : $\quad \pi=3.14$ ) |

## Answer.

a) $r^{2}+h^{2}=l^{2}==>5^{2}+12^{2}=l^{2}==>25+144=l^{2}==>25+144=l^{2}$

$$
l^{2}=169 \quad==>\quad l=\sqrt{169}=13 \mathrm{~cm}
$$

b) Surface area of a cone $=\pi r^{2}+\pi r l=\pi \times 5^{2}+\pi \times 5 \times 13=25 \pi+65 \pi$

$$
=90 \pi \mathrm{~cm}^{2}=\frac{90 \pi}{10000} \mathrm{~m}^{2}
$$

c) Surface area of $\mathbf{1 0 0 0 0}$ cones $=\frac{90 \pi}{10000} \times 10000=90 \pi \mathrm{~m}^{2}$

$$
\text { Total cost }=90 \pi \times 10=90 \times 3.14 \times 10=\text { Rs } 2826
$$

In the figure two circle intersect at $C . P C$ is the common tangent to both the circles.

$$
\mathrm{AB}=5 \mathrm{~cm}, \mathrm{~PB}=4 \mathrm{~cm}, \mathrm{PD}=3 \mathrm{~cm}
$$

a) What is the length of PA ?
b) What is the length of the tangent PC ?
c) What is the length of DE ?


Answer.
a) $P A=4+5=9 \mathrm{~cm}$
b ) $P A \times P B=P C^{2} \quad==>\quad 9 \times 4=P C^{2}$

$$
P C=\sqrt{36}=6 \mathrm{~cm}
$$

c) $P E \times P D=P C^{2}==>P E \times 3=6^{2}==>\quad P E=\frac{36}{3}=12 \mathrm{~cm}$ $D E=P E-P D=12-3=9 \mathrm{~cm}$

| 40 | If $x^{2}-10 x+16=(x-a)(x-b)$ <br> a) Find $a+b$ ? <br> b) Find $a b$ ? <br> c) Write $x^{2}-10 x+16$ as the product of two first degree polynomials ? |
| :---: | :---: |
|  | Answer . <br> a ) $a+b=10$ <br> b) $a b=16$ <br> c) $\quad a=8, b=2$ $x^{2}-10 x+16=(x-8)(x-2)$ |
| 41 | In the figure two chords $A B$ and $C D$ intersect at $P$. <br> a) Which other angle is equal to the measure of < CAB ? <br> b) Which other angle is equal to the measure of < ABD ? <br> c) Prove that $\mathbf{P A} \times \mathbf{P B}=\mathbf{P C} \times \mathbf{P D}$ ? |
|  | Answer . <br> A ) $\angle C A B=\angle C D B \quad$ (Angles made by an arc on its alternate arc are equal ) <br> b) $\angle A B D=\angle A C D$ <br> c) $\angle A P C=\angle B P D \quad$ ( Opposite angles are equal ) <br> $\frac{P A}{P D}=\frac{P C}{P B} \quad$ ( Since the angles of the triangles APC and BPD are equal , their sides change in the same ratio ) $P A \times P B=P C \times P D$ |

42 Look at the number pattern given below.

$$
\begin{array}{rrrrr} 
& & & 1 & \\
& & & & \\
& 2 & 3 & 4 & \\
5 & 6 & 7 & 8 & 9
\end{array}
$$

a) Write down the next two more lines of this pattern?
b) What is the last number in the $9^{\text {th }}$ line ?
c) What is the first number in the $10^{\text {th }}$ line ?
d) How many numbers are there in the $10{ }^{\text {th }}$ line?

Answer.
a) $\begin{array}{lllllll}10 & 11 & 12 & 13 & 14 & 15 & 16\end{array}$
$\begin{array}{lllllllll}17 & 18 & 19 & 20 & 21 & 22 & 23 & 24 & 25\end{array}$
b) $9^{2}=81$
c) 82
d) $2 \times 10-1=19$

43 In the figure $\mathbf{O}$ is the centre of the circle . $\angle \mathrm{ABC}=130^{\circ}$
a) What is the measure of < AEC ?
b)What is the measure of <AOC ?
c) What is the measure of < ADC ?
d) What is the measure of < ACD ?
e) What is the measure of < CAD ?



45 In the figure $A C=10 \mathrm{~cm}, \angle B=45^{\circ}, \angle C=30^{\circ}$. $A D$ is perpendicular to $B C$
a) What is the measure of $<B A C$ ?
b) What is the length of $A D$ ?
c) What is the perimeter of the triangle $A B C$ ?

d) What is the ratio of the length of the sides if the ratio of angles of a triangle is 2:3:7

## Answer .

a) $\angle B A C=180-(45+30)=180-75=105^{0}$
b ) $A D=5 \mathrm{~cm}$

$$
(A D: C D: A D=1: \sqrt{3}: 2)
$$

c) $C D=5 \sqrt{3} \mathrm{~cm}$

$B D=5 \mathrm{~cm}$

$$
(A D: B D: A B=1: 1: \sqrt{2})
$$

$A B=5 \sqrt{2} \mathrm{~cm}$
Perimeter of the triangle $A B C=(5+5 \sqrt{3})+5 \sqrt{2}+10=15+5 \sqrt{3}+5 \sqrt{2} \mathrm{~cm}$
d) Ratio of the angles $=2: 3: 7==>$ Angles are $30^{\circ}, 45^{0}, 105^{0}$

$$
\begin{aligned}
& A B: A C: B C=5 \sqrt{2}: 10: 5+5 \sqrt{3}=\sqrt{2}: 2: 1+\sqrt{3} \\
& \left(\quad \frac{2}{12} \times 180=30^{0} \quad, \quad \frac{3}{12} \times 180=45^{0} \quad, \frac{7}{12} \times 180=105^{0}\right)
\end{aligned}
$$

