

In Millikan's oil drop experiment, what is the terminal speed of an uncharged drop of radius  $2.0 \times 10^{-5} m$  and density  $1.2 \times 10^3 kg m^{-3}$ . Take the viscosity of air at the temperature of the experiment to be  $1.8 \times 10^{-5} Pa s$ . How much is the viscous force on the drop at that speed? Neglect buoyancy of the drop due to air.

Ans) Terminal speed =  $5.8 cm/s$

Viscous force =  $3.9 \times 10^{-10} N$

Radius of the given uncharged drop,  $r = 2.0 \times 10^{-5} m$

Density of the uncharged drop,  
 $\rho = 1.2 \times 10^{-3} kg m^{-3}$

Viscosity of air,  
 $\eta = 1.8 \times 10^{-5} Pa s$

Density of air ( $\rho_0$ ) can be taken as zero in order to neglect buoyancy of air.

Acceleration due to gravity,  
 $g = 9.8 m/s^2$

Terminal velocity ( $v$ ) is given by the relation:

$$V = \frac{2r^2 \times (\rho - \rho_0)g}{9\eta}$$

$$\begin{aligned} &= 2 \times (2 \times 10^{-5})^2 (1.2 \times 10^3 - 0) \times 9.8 / (9 \times 1.8 \times 10^{-5}) \\ &= 5.8 \times 10^{-2} \text{ m/s} \\ &= 5.8 \text{ cm s}^{-1} \end{aligned}$$

Hence, the terminal speed of the drop is  $5.8 \text{ cm s}^{-1}$ .

The viscous force on the drop is given by:

$$F = 6\pi\eta rv$$

$$\begin{aligned} \therefore F &= 6 \times 3.14 \times 1.8 \times 10^{-5} \times 2 \times 10^{-5} \times 5.8 \times 10^{-2} \\ &= 3.9 \times 10^{-10} \text{ N} \end{aligned}$$

Hence, the viscous force on the drop is  $3.9 \times 10^{-10} \text{ N}$ .