## WANDOOR GANITHAM - S S L C MODEL QUESTION PAPER 2021

## PREE3

MATHEMATICS
Maximum score : 80
Time: $2 \frac{1}{2}$ hours

## Instructions :

■ 20 minutes is given as cool - off time. Use cool - off time to read the questions and plan your answers .

- Attempt the questions according to the instructions .

■ Keep in mind the score and the time while answering the questions .
■ The maximum score for questions 1 to 45 will be 80 .
■ Simplify using the appropriate values of $\pi, \sqrt{2}, \sqrt{3}$ only if it is asked to do in questions

## For questions from 1 to 5 one score each (Choose the correct answer from the bracket)

1) First term of an arithmetic sequence of algebraic form $\mathbf{3 n + 1}$ is $\qquad$

$$
(3,1,4,6)
$$

2) The sum of the central angles of an arc and its alternate arc is $\qquad$

$$
\left(180^{\circ}, \quad 90^{0}, 270^{\circ}, \quad 360^{\circ}\right)
$$

3) Which number is to be added to $x^{2}+12 x+20$ to get a perfect square ?

$$
(144,36,16,400)
$$

4) In the figur $<B=90^{\circ}, \angle C=60^{\circ}, A C=12 \mathrm{~cm}$. What is the length of $B C \quad$ ?

$$
(6 \sqrt{2} \mathrm{~cm}, 6 \sqrt{3} \mathrm{~cm}, 12 \mathrm{~cm}, 6 \mathrm{~cm})
$$

5) Which among the following is a point on the $y$ - axis ?

$$
(\quad(0,1),(2,0),(1,1),(2,2))
$$

6) Consider the arithmetic sequence 7, 11, 15, ......
a) What is its common difference ?
b) Find the position of the term got by adding 40 to the tenth term of this sequence ?
7) In the figure $<\mathrm{CBE}=80^{\circ}$
a) What is the measure of $<\mathrm{ABC}$ ?
b) What is the measure of < ADC ?

8) Consider the line passing through the points $(1,2)$ and $(3,7)$.
a) What is its slope ?
b) Write the coordinates of another point on this line ?
9) The slant height of a cone is 20 centimetres and it makes an angle $30^{\circ}$ with its radius .
a) What is its radius?
b) Compute its curved surface area ?
10) Write $36 x^{2}-49$ as the product of two first degree polynomials ?

## For questions from 11 to 20 carries 3 scores each .

11) The vertices of a triangle are points on a circle of radius 4 centimetres. If two angles of this triangle are $60^{\circ}$ and $80^{\circ}$, draw the triangle ?
12) $6^{\text {th }}$ term of an arithmetic sequence is 25 and its $10^{\text {th }}$ term is 41 .
a) What is its common difference ?
b) What is algebraic form ?
c) Find the position of 201 in this sequence ?
13) Numbers from 1 to 25 are written on slips of paper and put in a box. A slip is to be drawn from it .
a ) What is the probability that the number written in it is an even number ?
b ) What is the probability that the number written in it is an odd number ?
c) What is the probability that the number written in it is a perfect square ?
14) The marks of 8 students in an exam are given below .

$$
44,73,57,34,62,44,38,48
$$

a) What is the mean mark ?
b) What is the median mark ?
15) In the figure $\angle A B C=120^{\circ}, \angle D=90^{\circ}, A B=14 \mathrm{~cm}, B C=10 \mathrm{~cm}$
a) What is the measure of $\angle A B D \quad$ ?
b) What is the length of $A D$ ?
c) What is the area of the triangle $A B C$ ?

16) In a second degree polynomial $p(x), p(2)=0, p(3)=0$ and the coefficient of $x^{2}$ is $\mathbf{1}$.
a) Write a factor of $p(x)$ ?
b) Write $p(x)$ as the product of two first degree polynomials ?
c) What number should be subtracted from $p(x)$ to get a second degree polynomial with $x-1$ as a factor ?
17) Draw a circle of radius 3 centimetres and draw a diameter. Draw tangents through the ends of this diameter .
18) From a circular sheet of radius 12 centimetres, a sector of central angle $120^{\circ}$ is cut out and made into a cone .
a) What is the slant height of the cone ?
b) What is the base radius of the cone ?
c) What is the base radius of another cone made by rolling up the remaining portion of the circular sheet ?
19) In the figure $A B C D$ is a rectangle and its sides are parallel to the axes. The coordinates of $A$ are (1,2) and those of $C$ are $(5,4)$.

a) What are the coordinates of $B$ and $D$ ?
b) Write the coordinates of the point of intersection of the diagonals?
20) In the figure, tangents through the points $A$ and $B$ of a circle intersect at $\mathbf{P} . \mathrm{QR}$ is a tangent through C
a) Which other line has the same length as that of PA ?
b) Which other line has the same length as that of RC ?

c) Prove that the perimeter of the triangle PQR is double the length of PA ?

## For questions from 21 to 30 carries 4 scores each .

21) Draw a rectangle of width 5 cm and height $\mathbf{3} \mathbf{~ c m}$. Draw a square of the same area .
22) a) What is the common difference of the sequence $6,11,16$ $\qquad$?
b) What is the common difference of the sequence $9,14,19, \ldots . . . . .$. ?
c) What is the difference between the $15^{\text {th }}$ terms of the above sequences?
d) What is the difference between the sum of first 15 terms of the above sequences ?

23 ) A man standing away from the bottom of a tower sees its top at an elevation of $\mathbf{6 0}$. Standing back by 50 metres, he sees it an elevation of $30^{\mathbf{0}}$.
a) Draw a rough figure based on the given details ?
b) What is the height of the tower ?
24) The figure shows two parallel sides of a square extended by 6 centimetres to make a rectangle .The area of the new rectangle is 391 square centimetres .
a) Write a second degree equation by taking the side of the square as $\boldsymbol{x}$
b) Compute the length of the side of the square .

25) The base perimeters of two cones are in the ratio $2: 3$ and their heights are in the ratio 5: 4 .
a) If the height of the first cone is taken as $5 h$, what is the height of the second cone ?
b) What is the ratio of the base radii of the cones ?
c) What is the ratio of the volume of the cones ?
d) What is the volume of the second cone, if the volume of the first cone is $400 \pi$ cubic centimetres ?
26) A circle is drawn with the line joining the points $A(1,3)$ and $B(7,3)$ as diameter .
a) What are the coordinates of the centre of the circle ?
b) Compute the radius of the circle ?
c) Write the coordinates of another point on a line passing through the point (0, 3) parallel to the $\boldsymbol{x}$ - axis ?
d) Write the coordinates of a point at which the line passing through the centre of the circle perpendicular to the diameter AB meets the circle ?
27) If $p(x)=x^{2}-6 x+k$
a) Find $p(2)$ ?
b) Find the value of $k$ if $x-2$ is a factor of $p(x)$ ?
c) Write $p(x)$ as the product of two first degree polynomials by substituting the value of $\mathbf{k}$
28) 45 households in a neighbourhood are sorted according to their monthly income in the table below .

| Monthly income (Rs ) | Number of households |
| :---: | :---: |
| 10000 | 5 |
| 20000 | 7 |
| 30000 | 8 |
| 40000 | 10 |
| 50000 | 8 |
| 60000 | 7 |

a) If the households are arranged in increasing order of monthly income, what is the monthly income of the household at the $21^{\text {st }}$ position ?
b) If the households are arranged in increasing order of monthly income, the monthly income of the household at what position is taken as the median ?
c) Find the median of the monthly income ?
29) In the triangle $\mathrm{ABC}, \angle A=90^{\circ}, \angle B=55^{\circ}$.
a) What is the measure of $<C \quad$ ?
b) Which among the following is $\sin 55^{\circ} \quad$ ?

$$
\left(\frac{A B}{B C}, \frac{A C}{B C}, \frac{A C}{A B}, \frac{A B}{A C}\right)
$$


c) Similarly write $\cos 35^{\circ}$ from this triangle ?
d) What is the relation connecting $\sin x^{0}$ and $\cos (90-x)^{0}$ if an angle of a right triangle is $x^{0}$ ?
30) In the figure $P A$ is a tangent . $B D$ is a line parallel to to $\mathrm{PA} .<\mathrm{BAP}=50^{0}$
a) What is the measure of < ADB ?
b) What is the measure of < ABD ?
c) What is the measure of < DCB ?


## For questions from 31 to 45 carries 5 scores each .

31) a) In the figure the circle touches the sides of the triangle ABC at $P, Q$ and $R$. If $<C=60^{\circ}$, what is the measure of < POQ ?
b) Draw a circle of radius 2.5 cm . Draw the triangle
 with two angles $60^{\circ}$ and $80^{\circ}$ and all its as tangents to this circle.
32) Look at the number pattern given below.
a) Write the next line of this pattern ?
b) How many numbers are there in the $20^{\text {th }}$ line ?
c) What is the last number in the $19^{\text {th }}$ line ?
d) What are the first and last number in the $20^{\text {th }}$ line ?
33) a) Draw the axes and mark the points $A(5,1), B(3,4), C(0,4)$ and $D(-1,1)$
b) Write the most suitable name for the quadrilateral ABCD ?
c) Find its area ?
34) 1 added to the product of two consecutive even numbers gives 361 .
a) Write a second degree equation by taking the smaller number as $\boldsymbol{x}$.
b) Find the numbers ?
35) In the figure $\angle B A C=30^{\circ}, \angle A D B=50^{\circ}, \angle A C D=60^{\circ}$
a) What is the measure of < BDC ?
b) What is the measure of < ACB ?
c) What is the measure of <ABD ?
d) What is the central angle of the arc BCD ?

36) Consider the arithmetic sequence $5,8,11$, $\qquad$
a) What is its common difference ?
b) What is its algebraic form ?
c) What is its $20^{\text {th }}$ term ?
d) What is the sum of first 20 terms of this sequence ?
e) What is the sum of first 20 terms of the sequence $9,12,15, \ldots . .$. ?
37) $A(1,2), B(5,6)$ and $C(7,4)$ are the vertices of a triangle .
a) Compute the lengths of the sides of the triangle ?
b) Prove that ABC is a right triangle ?
c) What are the coordinates of the centre of the circumcircle of the triangle ABC ?
38) Consider the polynomial $p(x)=x^{2}-10 x+16$
a) Find $p(1) \quad$ ?
b) Write a factor of $p(x)-p(1) \quad$ ?
c) Write $p(x)-p(1)$ as the product of two first degree polynomials ?
39) A cone of maximum volume is carved out from a solid cylinder of base radius 12 centimetres and height 20 centimetres .
a) Compute the volume of the cylinder ?
b) Compute the volume of the cone ?
c) The remaining portion of the cylinder is melted and recast in to small cones of base radius $\mathbf{6}$ centimetres and height 10 centimetres. How many small cones can be made?
40) In the figure $\quad \angle Q=45^{\circ}, \angle S=90^{\circ},<R=60^{\circ}, S R=4 \mathrm{~cm}$
a) What is the length of $P S$ ?
b) What is the length of $Q S$ ?
c) What is the measure of $<Q P R \quad$ ?

d) What is the ratio of the sides of a triangle with angles $45^{0}, ~ 60^{\circ}, 75^{0}$
41) In the figure $O A B C$ is a parallelogram . $C P$ is the perpendicular from $C$ to its opposite side. Area of the parallelogram is 40 square centimetres .
a) What is the length of OA ?
b) Find the distance between the sides OA and BC ?
c) What are the coordinates of $B$ and $C$ ?

42) In the figure circle touches the sides of the triangle $D E F$ at $P, Q$ and $R$.

$$
<\mathbf{Q P R}=70^{\circ},<\mathbf{P R Q}=50^{\circ}
$$

a) What is the measure of < EQP ?
b) What is the measure of < E ?
c) What is the measure of $<\mathbf{F}$ ?
43) In the figure, chord $A B$ is extended to meet the tangent
 through $C$ at $P$.
a) If $<\mathrm{BCP}=30^{\boldsymbol{0}}$, What is the measure of <BAC ?
b) Prove that the angles of triangles APC and BPC are same?

c) Prove that $\mathrm{PA} \times \mathrm{PB}=\mathrm{PC}{ }^{2}$ ?
44) In the figure chords $A B$ and $C D$ of the circles are extended to meet at $P$. $P A=24 \mathrm{~cm}, A B=18 \mathrm{~cm}$.The length of $P C$ is 10 cm more than that of PD .
a) What is the length of PB ?

b) $\mathbf{P C} \times$ PD $=$
c) Write down a second degree equation by taking the length of PD as $x$.
d) Compute the length of CD ?
45) In rhombus $A B C D$, the diagonals intersect at $P$, $A B=8 \mathrm{~cm}$, $\angle B A P=30^{\circ}$
a) What is the measure of $\angle A P B$ ?
b) What is the length of $P B$ ?
c) Compute the lengths of the diagonals ?


