## Constructions - Circles

(Focus Area)

Construction 1: Constructing a square of same area as that of a rectangle
Q) Draw a rectangle of width 5 centimetres and height 3 centimetres and draw a square of the same area.
( Question can be asked in this way also->
Draw a rectangle having area $15 \mathrm{~cm}^{2}$ and draw a square of the same area.)
( Hint: $5 \times 3=15$ )

Ans) Steps:

1. Draw line AB of length 5 cm .
2. Draw perpendiculars at $\boldsymbol{A}$ \& $\boldsymbol{B}$, measure 3 centimetres on these lines. Complete rectangle $A B C D$.
3. Extend $A B$ to $Y$ such that $B Y=3 \mathrm{~cm}$.
4. Drauv the perpendicullar bisector of AY.
5. Mark the midpoint of AY as M
6. Now draw a semicircle below, with AY as diameter. Extend the right side CB of the rectangle to meet this semi circle at $P$.
This line BP is the side of the required square.
7. Extend line BY, measure BP on your compass, using this measurement with B as centre draw an arc on this line and mark the point $R$.
8. With the same measurement drauv ares by keeping your compass at $\boldsymbol{P} \& \boldsymbol{R}$. Let these arcs meet at $\mathbf{Q}$. Complete the square BPQR.


## Assipmment

1. Draw a rectangle of width 6 centimetres and height 4 centimetres and draw a square of the same area.
2. Draw a rectangle of area $18 \mathrm{~cm}^{2}$ and draw a square of same area.
3. Draw a rectangle of width 7 centimetres and height 3 centimetres and draw a square of the same area.
4. Draw a rectangle of area $28 \mathrm{~cm}^{2}$ and draw a square of same area.

Construction 2: Constructing a triangle when two angles and circumradius is given
Q) Draw a triangle of circumradius 3 centimetres and two of the angles $50^{\circ}$ and $60^{\circ}$.
(Question can be asked in this way also->
Draw a circle of radius 3 cm . Draw a triangle with two angles $50^{\circ}$ and $60^{\circ}$ and the vertices are on this circle.)
Ans) Steps
Step1. Draw circle of radius 3 cm
Step2. Draw radius OC
Step3. Measure $100^{\circ}$ angle at $0 \quad$ (Because double of $50^{\circ}$ is $100^{\circ}$ )
Step4. Draw OB
Step5. Measure $120^{\circ}$ angle at $O \quad$ (Because double of $60^{\circ}$ is $120^{\circ}$ )
Step6. Draw OA
Step7. Join AB, BC, AC
Step8. We get $\triangle A B C$ with $\angle A=50^{\circ}, \angle C=60^{\circ}$


## Assignment

1. Draw a triangle of circumradius 3 centimetres and two of the angles $57 \frac{1}{2}^{\circ}$ and $62 \frac{1}{2}^{\circ}$.
2. Draw a triangle of circumradius 5 centimetres and two of the angles $75^{\circ}$ and $60^{\circ}$.
3. Draw a circle of radius 5.5 cm . Draw a triangle with two angles $55^{\circ}$ and $65{ }^{\circ}$ and the vertices are on this circle.
4. Draw a circle of radius 4 cm . Draw a triangle with two angles $30^{\circ}$ and $70^{\circ}$ and the vertices are on this circle.
5. Draw a circle of radius 5 cm . Draw an equilateral triangle with the vertices are on this circle.

## Constructions - Tangents

(Focus Area)

Construction 1 : Drawing a tangent to the circle (Using ruler and compass)
Q) Draw a circle of radius 3 cm . Mark a point $P$ on the circle . Draw a tangent through $P$.
Steps :1) Draw the circle of radius 3 cm . Mark centre as 0.
2) Mark a point $P$ on this circle.
3) Draw radius OP. Extend this line to $R$.
4) Draw a semicircle with $P$ as centre to cut $O R$ at $A \& B$.
5) Draw a pair of equidistant arcs from $A \& B$. Let their point of intersection be $Q$.
6) Join QP. Extend this line. This line is the tangent to the circle at $P$.


## Assignment

1. Draw a circle of radius 4 cm . Mark a point $P$ on the circle . Draw a tangent through $P$.
2. Draw a circle of radius 5.5 cm . Mark a point $A$ on the circle . Draw a tangent through A.
3. Draw a circle of radius 4.5 cm . Mark a point $C$ on the circle . Draw a tangent through C.
4. Draw a circle of radius 3.5 cm . Mark a point $P$ on the circle . Draw a tangent through $P$.
5. Draw a circle of radius 4 cm . Draw diameter $A B$. Draw tangents at A and B.

Construction 2 : Drawing tangents to a circle from a point outside the circle.

Q ) Draw a circle of radius 2 cm . Mark a point $P 7 \mathrm{~cm}$ away from the centre. Draw tangents to the circle from that point. Ans)

## Steps

1. Draw a circle of radius 2 cm , mark centre as 0
2. Mark a point $P$ at distance 7 cm from the centre. Join OP.
3. Draw the perpendicular bisector of OP, mark midpoint as $M$.
4. Draw a circle with centre $M$ and radius MP. Mark the point of intersection of the circles as A \& B. 5. Join PA \& PB. PA \& PB are the tangents to the circle.


## Assipnment

1. Draw a circle of radius 3 cm and mark a point $P 8 \mathrm{~cm}$ away from its centre. Draw two tangents from $P$ and measure their length.
2. Draw a circle of radius 4 cm . Mark a point $P$ at a distance 7 cm from the centre. Draw the tangents from $P$ to the circle. Measure the length of the tangents.
3. Draw a circle of radius 3 cm . Mark a point 7 cm away from the centre. Draw the tangents from this point to the circle. Measure the length of the tangents.
4. Draw a circle of radius 4 cm and mark a point $A \mathbf{~ c m}$ away from its centre. Draw two tangents from $A$ and measure their length.
5. Draw a circle of radius 2 cm . Mark a point $P 8 \mathrm{~cm}$ away from the centre. Draw tangents to the circle from that point.

Construction 3 : Drawing incircle of a triangle when two angles of the triangle are given
Q) Draw a circle of radius 2.5 centimetres. Draw a triangle of angles $40^{\circ}, 60^{\circ}$ with all its sides touching the circle.
Ans) Draw a rough figure.

From the figure we can find the other required measurements.
In $\triangle \mathrm{ABC}$

$$
\begin{aligned}
& \angle C=40^{\circ}, \therefore \angle R O Q=180^{\circ}-40^{\circ}=140^{\circ} \\
& \angle A=60^{\circ}, \therefore \angle P O Q=180^{\circ}-60^{\circ}=120^{\circ}
\end{aligned}
$$



## Steps:

1) Draw a circle of radius 2.5 with centre 0.
2) Draw the radius OP
3) Measure angle of $120^{\circ}$ at $O$ and draw radius $O Q$.
4) Measure angle of $140^{\circ}$ at $O$ and draw radius $O R$.
5) Draw tangents at $P, Q \& R$ and complete the triangle $A B C$


## Assignment

1. Draw a circle of radius 3 centimetres. Draw a triangle of angles $50^{\circ}, 70^{\circ}$ with all its sides touching the circle.
2. Draw a circle of radius 3.5 centimetres. Draw a triangle of angles $60^{\circ}, 75^{\circ}$ with all its sides touching the circle.
3. Draw a circle of radius 3 centimetres. Draw a triangle of angles $30^{\circ}, 110^{\circ}$ with all its sides touching the circle.
4. Draw a triangle having angles $55^{\circ}, 70^{\circ}$ and inradius 4 cm .
5. Draw a triangle having angles $40^{\circ}, 60^{\circ}$ and inradius 3 cm .
