

1. Find the multiplicative inverse of $2 - 3i$

Ans) Let $z = 2 - 3i$.

Then, the multiplicative inverse
of z is

$$\frac{1}{z} = \frac{1}{2 - 3i} = \frac{1}{2 - 3i} \times \frac{2 + 3i}{2 + 3i}$$

$$= \frac{2 + 3i}{4 + 9} = \frac{2}{13} + \frac{3}{13}i$$

2. Express $\frac{2+i}{2-i}$ in the form $a+ib$.

Ans)

$$\begin{aligned}\frac{(2+i)}{(2-i)} &= \frac{(2+i)^2 \times (2+i)}{(2-i) \times (2+i)} = \frac{(4+4i+i^2)}{(4-i^2)} \quad [i^2 = -1] \\ &= \frac{(4+4i-1)}{(4+1)} \\ &= \frac{(3+4i)}{5} = \underline{\underline{\frac{3}{5}}} + \underline{\underline{\frac{4i}{5}}} = a+ib\end{aligned}$$