SJ Notes on Focus Area

February 3, 2021

1

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

■ The concept arithmetic sequence

- 1) Write an arithmetic sequence having first term 5 and common difference 3.
- 2) Look at the sequence of equilateral triangles. The sequence is formed by using matchsticks.



- a) Write the number of matchsticks in each term as a number sequence.
- b) Is this an arithmetic sequence.
- c) If so, what is its common diffrence?
- 3) a) Write the sequence of numbers ends with 1 or 6 in one's place.
 - b) Is this an arithmetic sequence?
 - c) If so, what is its largest two digit term?
- 4) a) Write the sequence of numbers which gives the remainder 2 on dividing by 3.
 - b) What is the smallest three digit term of this sequence?
- 5) a) Write the sequence of numbers 3 more than the multiples of 5.
 - b) Is this an arithmetic sequence?What is its common difference?
 - c) What is the largest three digit term of this sequence?
- 6) a) Write the sequence of numbers having 1 in ones place.
 - b) Describe this sequence in other words also.
 - c) Is this an arithmetic sequence?

7) $\frac{1}{7}, \frac{2}{7}, \frac{3}{7} \cdots$ is a sequence.

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- a) The numerators are natural numbers in the order and denominator is 7. Is this an arithmetic sequence?
- b) What is the position of 1 in this sequence?What is the position of 100 in this sequence?
- c) What is the position of 100 in this sequence?
- d) Is this sequence contain all natural numbers?

8) The sequence $7, 10, \bigcirc, 16, \bigcirc, 22$ is an arithmetic sequence.

- a) What is the common difference of the sequence ?
- b) What are the missing terms in the sequence ?

9) x, y, z are in arithmetic sequence. If x - y = k(z - x) then what is k?

SJ Notes on Focus Area

February 4, 2021

2

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

Term and position in an arithmetic sequence

- 1) Fourth term of an arithmetic sequence is 12, common difference 5.
 - a) What is the third term?
 - b) What is the first term ?
 - c) Find the tenth term.

2) Tenth term of an arithmetic sequence is 74, common difference 4.

- a) What should be added to its 10 th term to get 15 th term? What is the 15 th term?
- b) Find the fifth term of this sequence .
- c) Find the first term .
- d) Write the sequence .
- e) What is the remainder when the terms are divided by its common difference.
- 3) a) What is the common difference of the arithmetic sequence $1, 7, 13, 19 \cdots$
 - b) What is the remainder when the terms are divided by its common difference?
 - c) Is 100 a term of this sequence ?
 - d) Which is the first two digit term of this sequence?
 - e) What is the first three digit term of this sequence ?
- 4) The difference between third term and seventh term of an arithmetic sequence is 20.
 - a) What is the common difference of this sequence?
 - b) What is the difference between 10 th term and 18 th term.
 - c) What should be added to the $18\ {\rm th}\ {\rm term}\ {\rm to}\ {\rm get}\ 24\ {\rm th}\ {\rm term}.$
- 5) First term of an arithmetic sequence is 4 and tenth term $40. \label{eq:40}$
 - a) What is the common difference of the sequence .
 - b) What is the fifth term of the sequence ?
 - c) What should be added to the fifth term to get fifteenth term?
 - d) What is the difference between second term and eighth term?
- 6) The difference between $4\ {\rm th}\ {\rm term}\ {\rm and}\ 7{\rm th}\ {\rm term}\ {\rm os}\ 12$
 - a) What is the difference between seventh term and thirteenth term .
 - b) What should be added to the 10 th term to get 20 th term?
 - c) Can the difference between any two terms of this sequenec 36. How can you realize this ?

- 7) a) Write the sequence of numbers obtained by adding 4 to the multiples of 3.
 - b) Is 43 a term of this sequence ?
 - c) Can the difference between any two terms of this sequence $81\,$
 - d) What should be added to the $10\ {\rm th}\ {\rm term}\ {\rm to}\ {\rm get}\ 21\ {\rm st}\ {\rm term}.$
- 8) Seventh term of an arithmetic sequence is 16 and nineth term is $24\,$
 - a) What is the common difference ?

- b) What is the $20\ {\rm th}\ {\rm term}\ {\rm of}\ {\rm the}\ {\rm sequence}\ {\rm ?}$
- c) What is the first term of the sequence?
- d) Can the sum of some terms of this sequence $110? \ {\rm How} \ {\rm can} \ {\rm you} \ {\rm realize} \ {\rm this} \ ?$

SJ Notes on Focus Area

February 6, 2021

3

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

Algebra of arithmetic sequence

1) Observe the arithmetic sequence given below.

$$3, 5, 7, 9 \cdots$$

A pattern can be seen below $3=2\times 1+1$

 $5 = 2 \times 1 + 1$ $5 = 2 \times 2 + 1$ $7 = 2 \times 3 + 1$

- a) Write the term 9 as shown in the pattern.
- b) Which is the smallest two digit term of this sequence?
- c) Find the $20\ {\rm th}\ {\rm term}\ {\rm of}\ {\rm this}\ {\rm sequence}$
- d) Write the algebraic form or n th term of this sequence.
- 2) $5, 8, 11 \cdots$ is an arithmetic sequence
 - a) Write the algebraic form of this sequence
 - b) Using the algebraic form find its 10 th term.
 - c) Find the 25 th term of this sequence .
 - d) Is 152 a term of this sequence?

3) There is a shortcut fo write the algebraic form of an arithmetic sequence. If f stands for the first term, d for common difference then the n th term is $x_n = dn + (f - d)$. Consider the sequence $7, 10, 13, 16, 19 \cdots$

- a) Write the algebraic form of the sequence.
- b) What is the 10 th term of the sequence?
- c) Which is the largest two digit term of this sequence?
- 4) Algebraic form of an arithmetic sequence is 3n+4
 - a) What is the common difference and first term of this sequence
 - b) Can the difference between any two terms of this sequence 144?
 - c) Is $144~\mathrm{a}$ term of this sequence?
 - d) If 144 is not a term then write the term of the sequence just above 144?

5) First term of an arithmetic sequence is $\frac{1}{2}$ and common difference is $\frac{1}{6}$.

- a) Write the algebraic form of this sequence?
- b) At what position a natural number appear first time in the sequence?
- c) Is this sequence contains all natural numbers as terms? What are the positions of natural numbers.
- d) At what position 5 appear in this sequence?
- 6) The picture shown below is a pattern of squares made by using matchsticks .



- a) Write the number of matchsticks in each line as a sequence.
- b) Write the algebraic form of this sequence?
- c) How many matchsticks are nedded to make $20 {\rm th}$ line of this pattern.
- d) Is any line contains 100 matchsticks ? If so, what is the position of this line?

7) Consider the arithmetic sequence $125, 120, 115\cdots$

- a) What is the common difference of this sequence?
- b) Write the algebraic form of this sequence
- c) How many positive terms are there in this sequence?
- d) At what position the first negative term appears in this sequence?
- 8) In the arithmetic sequence $10, 17, 24 \cdots 178$
 - a) What is the common difference of this sequence ?
 - b) Write the algebraic form of this sequence?
 - c) How many terms are there in this sequence?
 - d) Which number comes as the middle term of this sequence?

SJ Notes on Focus Area

February 6, 2021

4

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

Sum of counting numbers

1) As we discussed earlier the summation of counting numbers from the beginning in an order is performed by pairing the numbers from both ends.

It is illustrated below

- 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 can be paired as (1, 10), (2, 9), (3, 8), (4, 7), (5, 6)
- Pair sum is 11. The sum of numbers is $11 \times 5 = (1+10) \times \frac{10}{2}$ So the sum of first n counting numbers is $\frac{n(n+1)}{2}$
- So the sum of first n counting furthers is $\frac{2}{2}$
 - a) What is the sum of first $10\ {\rm counting\ numbers?}$
 - b) Calculate the sum $1+2+3+4+\cdots 100$
 - c) Find the sum of first $25\ \mathrm{natural}\ \mathrm{numbers.}$

2) Look at the pattern given below

$$1 = 1$$

$$1 + 3 = 4 = 2^{2}$$

$$1 + 3 + 5 = 9 = 3^{2}$$

$$1 + 3 + 5 + 7 = 16 = 4^{2}$$

The sum of first n odd numbers is n^2 .

- a) What is the sum of first $10 \ \mathrm{odd} \ \mathrm{numbers?}$
- b) How many odd numbers from 1 in an orded makes the sum $400 \ref{eq:starses}$
- c) How many odd numbers are there below $100?\ {\rm What}$ is its sum?
- d) Sum of the odd numbers from 1 in an order makes the sum in between 900 and 1000. How many odd numbers make this sum? Which number is largest among them.
- 3) Consider the sequence of even numbers $2, 4, 6, 8, 10 \cdots$

Look at the pattern formed from this sequence

 $2 + 4 = 6 = 2 \times 3 = 2(2 + 1)$

$$2 + 4 + 6 = 12 = 3 \times 4 = 3(3 + 1)$$

$$2 + 4 + 6 + 8 = 20 = 4 \times 5 = 4(4 + 1)$$

- a) What is the sum of first 5 even numbers?
- b) Find the sum $2+4+6+8+10+\cdots 50$
- c) What is the sum of first 20 even numbers? Using this find the sum of first 20 counting numbers.

4) The sum of first n even numbers is n(n + 1) using this formula calculate the following

- a) What is the sum of first 10 even numbers?
- b) What is the sum of all even numbers below $100 \ensuremath{?}$

c) How much the sum of first 50 even numbers is greater than the sum of first 50 odd numbers.

5) Look at the pattern given below



- a) Write the sequence of numbers at the right end of each line in the pattern.
- b) Which number comes in the right end of 20 th line?
- c) In which line the number $850 \ \mbox{appears}$?
- d) How many natural numbers are needed to make 50 lines?
- e) Find the sum of all counting numbers to make $50\ {\rm lines}$ in the pattern.
- 6) a) What is the sum of first 9 counting numbers?
 - b) Calculate the sum of first $20\ {\rm counting}\ {\rm numbers.}$
 - c) What is the sum of counting numbers from $10 \mbox{ to } 20$

7) Look at the pattern given below

1



- a) Write the number of numbers in each line as a sequence.
- b) How many numbers are there in 20 th line?
- c) Which number comes at the right end of 20 th line?
- d) What is the sum of all numbers needed to make $20 \ \mbox{lines}?$

SJ Notes on Focus Area

February 7, 2021

5

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

■ Sum of the terms of an arithmetic sequence (Excluding the algebraic form of the sum)

1) There is an important property to an arithmetic sequence If the sequence contains even number of terms we can make the terms pairs taking equidistant from

both ends .Sum of the terms in each pair are equal.

That means sum of the terms equidistant from both ends are equal.

Consider the arithmetic sequence 7, 10, 13, 16, 19, 22, 25, 28, 31, 34.

- a) Make pairs taking the terms equidistant from both ends of the sequence. What is the sum of the terms in each pair?
- b) Calculate the sum of the terms of this sequence.
- c) If x_1 stands for the first term and x_n the last term then establish a formula to calculate the sum of the terms.
- d) If the sequence is 7, 10, 13, 16, 19, 22, 25, 28, 31 can you apply this formula to calculate the sum of the terms. verify!
- 2) Algebraic form of an arithmetic sequence is 3n+5
 - a) What is the first term of this sequence?
 - b) Find the 25 th term of this sequence?
 - c) Calcualte the sum of the first 25 terms of this sequence.
 - d) Which term comes in the middle of this sequence?
- 3) 21 st term of an arithmetic sequence is 100.
 - a) What is the sum of the 20th term and 22 nd term?
 - b) what is the sum of first term and 41 st term.
 - c) Calculate the sum of first 41 terms of this sequence?
- 4) The angles of a pentagon are in an arithmetic sequence.
 - a) Which angle measure is constant?
 - b) If the smallest angle is 40° then what is the measure of the largest angle?
 - c) What is the difference between two adjacent angles if the smallest angle is 40°
 - d) Can the smallest angle is 36° . Explain
- 5) The sum of the first 39 terms of an arithmetic sequence is 2379.
 - a) What is the 20 th term of this sequence?
 - b) What is the sum of first and 39 th term of this sequence?

- c) If the first term is 4 what is its 39 th term?
- d) What is the sum of $15\ {\rm th}\ {\rm term}\ {\rm and}\ 25\ {\rm th}\ {\rm term}?$
- 6) The sum of first 9 terms of an arithmetic sequence is 45. The sum of the first 18 terms is 171
 - a) What is the sum of its 10 th to 18 th terms?
 - b) What is its $5\ {\rm th}\ {\rm term}\ ?$
 - c) What is its 14 th term?

- d) Find the sum of $5\ {\rm th}\ {\rm to}\ 14\ {\rm th}\ {\rm terms?}$
- 7) The picture shown below is a sequence of equilateral triangles made by matchsticks.



- a) Write the sequence of the number of matchsticks to make the terms .
- b) Write the algebraic form of this sequence
- c) How many matchsticks are needed to make $20\ {\rm th}\ {\rm term?}$
- d) Calculate the total number of matchsticks to make 20 terms of this sequence?

SJ Notes on Focus Area

February 8, 2021

6

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

Angle in the semicircle.

1) In the figure $\triangle ACB$, $\triangle ADB$ and $\triangle AEB$ have the same base AB. If $\angle ADB = 90^{\circ}$ then



- a) What is the position of D based on the circle with diametre AB?
- b) What is the position of E based on the circle with diametre AB?
- c) What is the position of C based on the circle with diametre AB?
- 2) Draw a circle of diametre 5 cm. Construct a rectangle with diagonal 5 cm and one of its sides 3 cm Write the principle of construction.
- 3) Sides of a triangle are $\sqrt{2}$ cm , $\sqrt{3}$ cm and $\sqrt{5}$ cm.
 - a) What is the position of the vertex based on the circle with opposite side $\sqrt{5}$ cm as the diametre?
 - b) What is the position of the vertex based on the circle with opposite side $\sqrt{2}$ cm as the diametre?
 - c) What is the position of the vertex based on the circle with opposite side $\sqrt{3}$ cm as the diametre?
- 4) a) Draw a square of diagonal 6cm such that the vertices are on a circle.
 - b) What is the length of its side ?
 - c) What is the area of the square?
- 5) Sides of triangle ABC are AB = 5 cm, AC = 12 cm , BC = 13 cm
 - a) What kind of triangle is this ?
 - b) What is the position of A based on the circle with diametre BC?
 - c) What is the position of C based on the circle with diametre AB?
 - d) What is the position of B based on the circle with diametre $AC{\ensuremath{\mathcal R}}$

6) In the figure AB is the diametre of a semicircle. Three angles x, y, z are marked outside, on the semicircle and inside the semicircle.



a) What is the value of *y*?

1

- b) If x, y, z are in an arithmetic sequence, then what is x + z?
- c) If the common difference of the sequence is $50\ {\rm then}\ {\rm find}\ x$ and z
- 7) ABC is an equilateral triangle. A semicircle is drawn with diametre AB. Semicircle intersect the sides at P and Q.



- a) What is the measure of angle BQC?(Draw angle in the figure)
- b) What are the measures of $\angle CBQ$, $\angle BCQ$?
- c) Prove that the semicircle bisects the side AB and AC

SJ Notes on Focus Area

February 9, 2021

7

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

Central angle of an arc and angle in the complementary arc.

1) $\triangle ABC$ is a right angled triangle with hypotenuse AC. The line OB joins the vertex B and mid point of the hypotenuse.



- a) If $\angle BOC = 40^{\circ}$ then what is the measure of $\angle A$?
- b) What is the measure of $\angle C$?
- c) If the perpendicular sides are a and b then what is the length OB?
- 2) ABCD is a square. The diagonals meet at O.



- a) What is the measure of $\angle AOB$?
- b) What is the measure of $\angle APB$?
- c) What is the measure of $\angle AQB$?

3) Triangle ABC is an equilateral triangle.



- a) What is the measure of $\angle BAC$?
- b) What is the measure of $\angle BOC$?
- c) What is the measure of $\angle BDC$?
- d) If BD = CD then suggest a suitable name to OBDC
- 4) Two angles of a triangle are $70^\circ, 30^\circ$. The vertices are on a circle of radius 3 cm
 - a) Draw the triangle.
 - b) Mention the geometric principle of this construction.
- 5) Draw a circle of radius 3cm and mark an arc of central angle 60° .Draw a quadrilateral with the vertices are on this circle. Two opposite angles should be 30° and 150° .
- 6) In the figure triangle ABC is an equilateral triangle and triangle PBC is a right triangle.



a) What are the angles of the right triangle?

1

- b) If $PB = 10 \,\mathrm{cm}$ what is the radius of the circle?
- 7) Draw a circle of radius $3 {\rm cm}$ and draw the angles 45° and 135° on this circle.

SJ Notes on Focus Area

February 10, 2021

8

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

Cyclic Quadrilaterals.

1) The vertices of the quadrilateral ABCD are on a circle. $\angle A = x, \angle B = 2y, \angle C = 2x$ and $\angle D = 3y$



- a) Find \boldsymbol{x} and \boldsymbol{y}
- b) Write the angles of the quadrilateral
- 2) In the triangle PQR the sides PQ and PR are equal. A is the mid point of PQ and B is the mid point of PR. Also , $\angle P=40^\circ$



- a) What is the measure of $\angle Q$ and $\angle R$?
- b) Find the angles of QABR
- c) Is this a cyclic quadrilateral?

3) The vertices of ABCD are on a circle. $\angle A = x, \angle B = 3x + 15, \angle C = x + 100$ and $\angle D = x + 5$



- a) Find \boldsymbol{x}
- b) What are the angles of ABCD
- c) Is this a cyclic quadrilateral?
- 4) In the figure two circles intersect at P and Q. PBCD is a quadrilateral in which AB = CD



- a) If $\angle A = x$ then what is $\angle PQD$?
- b) What is $\angle ABC$?
- c) Is AD parallel to BC? How can you realize?
- d) Prove that ABCD is a cyclic quadrilateral .
- 5) In the triangle ABC, P is a point on AB such that CA = CP. The line through B parallel to PC and the line through C parallel to AB intersect at Q. $\angle A = 40^{\circ}$



- a) What is the measure of $\angle APC$?
- b) What is the measure of $\angle BQC$?
- c) is ABQC a cyclic quadrilateral?
- d) Suggest a suitable name to $ABQC \label{eq:absolution}$
- 6) The vertices of ABCD are on a circle with diametre AB. $\angle BAC = 20^{\circ}, AD = CD$



- a) What is the measure of angle $B\ensuremath{\mathbf{?}}$
- b) What is the measure of $\angle D$?
- c) Find other two angles of ABCD?
- 7) In the figure $\triangle ABC$ is an equilateral triangle. The measure of $\angle BCD$ is two times the measure of $\angle CBD$.



- a) What is the measure of $\angle BDC$
- b) Find $\angle CBD$ and $\angle BCD$

c) What is the measure of $\angle ABD$ and $\angle ACD$

SJ Notes on Focus Area

February 11, 2021

9

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

If chords of a circle AB and CD intersect at P then $PA \times PB = PC \times PD$

1) Chords AB and CD intersect at $P.{\rm lf}\ AB=5{\rm cm}$, $PB=3{\rm cm}$ and $PD=4{\rm cm}.$



a) What is the length PA?

b) Find ${\cal PC}$ and ${\cal CD}$

2) Chords AB and CD intersect at P outside the circle.lf AB = 5 cm, PB = 3 cm, PD = 4 cm.



- a) Write the relation between PA, PB, PC and PD
- b) Find the length ${\cal CD}$

- 3) AB and CD are two chords intersecting at a point P inside the circle such that AP = CP
 - a) What is the relation between PB and PD?
 - b) If the length of the chord AB is $10 \,\mathrm{cm}$ then what is the length of CD
- 4) In the figure AE and CB are perpendicular chords of a circle intersect at D inside the circle.If AB = 5, BD = 4, AE = 15 then



- a) Find the length AD
- b) Find the length $D {\cal E}$
- c) Find the length CE
- 5) The chords of a circle AB and CD intersect at P outside the circle.If PA=PC then prove that AB=CD



- 6) In the figure AB and CD are two chords of a circle which when produced meet at a point P
 - a) Draw AC and BD, complete the quadrilateral ABDC
 - b) Establish the similarity of the triangles PAC and PDB
 - c) Establish the relation $PA \times PB = PC \times PD$
- 7) The chords AB and CD intersect at P outside the circle.



- a) What is the relation between PA, PB, PC and PD?
- b) If AB = 5 cm, PB = 3 cm, PD = 2 cm then what is the length CD?

8) In the trapezium ABCD, AD = BC and AB is parallel to CD. The diagonals AC and BD intersect at P.



- a) What is the relation between $\angle ADB$ and $\angle ACB$? How can we realize this relation?
- b) If $\angle DAC = 30^{\circ}$ then what is the measure of $\angle DBC$?

1

c) What is the relation between the segments made by P on the diagonals?

SJ Notes on Focus Area

February 12, 2021

10

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

If chords of a circle AB and CD intersect at P then $PA \times PB = PC \times PD$

1) AB is the diametre of a circle . CD is a chord perpendiculat to AB intersect at P.If PA = 12, PB = 3 then



- a) What is the length PC?
- b) What is the length of the chord CD?
- c) What is the area of the square drawn on CD as the side?

2) AB is the diametre of a semicircle, P is a point on AB and PC is perpendicular to AB



- a) Prove that $PA \times PB = PC^2$
- b) If PA = 9 cm , PB = 4 cm then what is the length PC?
- c) What is the area of the square with side PC?
- 3) AB is the diametre of a semicircle, P is a point on AB and PC is perpendicular to AB



- a) If PC = 6 cm,and PB = 3 cm then what is the length of PA
- b) What is the radius of the circle ?
- c) What is the area of the square drawn with side PC?
- 4) In the figure AB is the diametre of the semicircle, PC is perpendicular to AB. $AC = 5\sqrt{29}$ cm and PA = 25cm.



- a) What is the length of PC?
- b) What is the lenght PB?
- c) What is the radius of the circle?
- 5) Draw a semicircle of suitable diametre .Construct a line of length $\sqrt{12}$ cm perpendicular to the diametre whose one end is on the diameter and other end is on the semicircle.Explain the principle of construction.
- 6) In the figure AB is the diametre of the circle and PC is perpendicular to the diametre. PA : PB = 2:1 and PC = 6 cm.



- a) Write the relation between PA, PB and PC?
- b) Find the lengths PA and PB
- c) What is the radius of the circle?
- 7) a) Draw an equilateral triangle of altitude 3 cm
 - b) What is the lenght of one side ?
 - c) What is the radius of its incircle?
- 8) Draw a rectangle of sides 5 cm and 3 cm. Construct a square whose area is same as the area of the rectangle
- 9) a) Draw a semicircle of suitable diametre .Draw a line of length $\sqrt{12}$ cm whose one end on AB and other end on the semicircle.
 - b) Draw a chord of length $\sqrt{48}$ cm by make the semicircle as the circle

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SJ Notes on Focus Area

February 12, 2021

11

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

Calculation of probability as a number.

- 1) A vessel contains 3 black beads and 2 white beads. One is taken from the vessel without looking into the vessel.
 - a) What is the probability of getting black bead?
 - b) What is the probability of getting white bead?
- 2) A box contains 10 cards on which one of the numbers $1, 2, 3 \cdots 10$ is written in each card.One card is taken from the box at random.
 - a) What is the probability of getting a an even numbered card
 - b) What is the probability of getting an odd numbered card?
 - c) What is the probability of getting a card on which a prime number is written?
 - d) What is the probability of getting a perfect square on the card.
- 3) Each of the numbers from 1 to 100 are written on small paper pieces .One is taken from the card at random.
 - a) How many perfect squared cards are there in the box?
 - b) What is the probability of getting a perfect squared card?
 - c) What is the probability of getting an even numbered card?കിട്ടുന്നത് ഇരട്ടസംഖ്യയായ പൂർണ്ണവർഗ്ഗം ആകാനുള്ള സാധ്യത എത്ര?
 - d) What is the probability of getting an odd numbered card?
 - e) What is the probability of not getting a perfect numbered card?
- 4) A die in which the numbers $1 \mbox{ to } 6 \mbox{are written on the faces is thrown}$
 - a) What is the probability of falling an even numbered face?
 - b) What is the probability of getting an odd numbered face ?
 - c) What is the probability of getting a prime numbered face?
- 5) Two digit numbers are written in small paper pieces and placed in a box. One is taken from the box at random
 - a) How many multiples of 5 are there in the box?
 - b) What is the probability of getting a multiple of 5?
 - c) What is the probability of not getting a multiple of 5?

- 6) Numbers $1, 2, 3 \cdots 17$ are written in small paper cards and placed in a box. One card is taken from the box at random.
 - a) What is the probability of getting odd numbered card?
 - b) What is the probability of getting prime numbered card?
 - c) What is the probability of getting a multiple of 3?
 - d) What is the probability of getting a multiple of 2 and 3?
- 7) A die numbered 1 to 6 are thrown.
 - a) What is the probability of falling a number less than 4?
 - b) What is the probability of getting a multiple of 2?
 - c) What is the probability of falling a multiple of both $2 \mbox{ and } 3$
 - d) What is the probability of not falling a prime number?
- 8) Integers from -4 to 4 are written in small paper pieces and placed in a box. One is drawn from the box at random .If the outcome is denoted by x,
 - a) What is the probability of getting a number satisfying the condition |x| < 2?
 - b) What is the probability of getting a number satisfying the condition $|x| \leq 2$?
 - c) What is the probability of getting a number satisfying the condition $|x| \ge 3$?
 - d) What is the probability of getting a number satisfying the condition $|x| \leq 3$?
- 9) Two dice numbered 1 to 6 are thrown at together.
 - a) Write the outcomes as pairs

- b) What is the probability of the occurence of equal numbers?
- c) What is the probability of the occurence of perfect squares ?
- d) What is the probability of the occurrence of multiple of 2 in one die and multiple of 3 in other die ?

10) What is the probability of getting 5 Sundays in the month December?

SJ Notes on Focus Area

February 14, 2021

12

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

Area and Probability.

1) ACP is drawn in the square ABCD and shaded P is the mid point of the side of the square



- a) If the side of the square is a then what is the altitude to the side PC of the shaded triangle.
- b) If the side of the square is a then what is the area of the shaded triangle ?
- c) If a fine dot is placed into the figure then what is the probability of falling the dot in the shaded triangle ?
- 2) A square is drawn by joining the mid points of the sides of another square. The inner square is shaded blue.



- a) Divide the triangle into eight equal triangles by drawing two lines
- b) A fine dot is placed into the figure. What is the probability of falling the dot in the inner square?

3) Triangle PQR is drawn by joining the mid points of the sides of triangle ABC.



- a) How many equal triangles are there in the figure?
- b) A fine dot is placed into the figure. What is the probability of falling the dot in triangle PQR?
- c) How many parallelograms are there in the picture?
- d) A fine dot is placed into the figure. What is the probability of falling the dot in the parallelogram PQRC?
- 4) A triangle is drawn by joining the alternate vertices of a regular hexagon.



- a) Divide the figure into $6 \ \mbox{equal triangles}$
- b) If a fine dot is placed into the figure , what is the probability of falling the dot in the shaded triangle?
- 5) A square is drawn in a circle. The vertices of the square are on the circle. A fine dot is placed into the figure at random. What is the probability of falling the dot in the shaded square.



6) There are two squares in the figure. The perimetre of the outer square is 28 cm, the perimetre of the inner square is 20 cm



- a) What is the area of the outer square?
- b) What is the area of inner square?
- c) What is the area of the shaded triangle ?
- d) If a fine dot is placed into the figure then what is the probability of falling the dot in the shaded triangle?
- 7) The mid points of the two sides and one vertex of a square are joined in such a way as to get a triangle which is coloured in the picture.



- a) If the side of the square is a, what is are of unshaded triangles ?
- b) What is the area of the shaded triangle?

c) If a fine dot is placed into the figure then what is the probability of falling the dot in the coloured traingle?

SJ Notes on Focus Area

February 15, 2021

13

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

How to develop a second degree equation in a suitable situation?

- 1) Form the equations in the following cases.
 - a) The sum of a number and its square is $12\,$
 - b) When a number is subtracted from its square results $20\,$
 - c) The sum of the square of a number and two times that number is $63\,$
 - d) Product of two consecutive odd numbers is $63. \label{eq:consecutive}$
 - e) The sum of a number and its reciprocal is $\frac{10}{3}$.
- 2) The square of a number is 16.
 - a) What are the numbers ?
 - b) Take the number as \boldsymbol{x} and form an equation
 - c) Can the square of a real number -16? Explain.
- 3) The sum of a number and its square is 30.
 - a) If the number is x, form an equation.
 - b) What is the positive number xm?
 - c) Can more than one number satisfying this condition?
- 4) x is an odd number greater than 1.
 - a) What are the odd numbers nearer to x
 - b) If the product of those numbers is 45, form an equation.
 - c) Find the numbers.
- 5) If the sides of a square are reduced by 1 , the area becomes $100. \label{eq:10}$
 - a) If the side of the first square before reducing is x, form an equation.
 - b) Find the side of the square.
 - c) What will be the perimetre of the new square.
- 6) Consider two adjacent even numbers
 - a) If one of them is x then what is the other?
 - b) If the product is 120 then write a second degree equation.
 - c) Convert this equation as a completed square by suitable changes
 - d) Find the numbers .

- 7) Length of a rectangle is 8 more then its breadth.
 - a) If the breadth is x then what is its length?
 - b) If the area is $240\,\,{\rm sq.cm}$ form a second degree equation.
 - c) Calculate the lenght and breadth
- 8) In the figure AB is the diametre of the semicircle. AB is perpendicular to PC. Also, AP = BP + 5, PC = 6.



- a) Write the relation between the lenghts PA, PB and PC
- b) If PB = x then write an equation connecting the lenghts PA, PB and PC
- c) What is the length of PB?
- d) What is the radius of this circle.
- 9) Consider the sequence of even numbers $2, 4, 6, 8 \cdots$.
 - a) What is its algebraic form?

b) How many terms from the beginning in the order makes the sum 210?

SJ Notes on Focus Area

February 16, 2021

14

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

Problems related to squares and rectangles

- 1) One side of a rectangle is $3 \ {\rm more}$ than the other side.Area is calculated $108 \ {\rm sq.cm}$
 - a) If one side is x then what is the other side?
 - b) Form a second degree equation using the given conditions.
 - b) Find the sides of the rectangle.
 - c) What is the length of the diagonal?
- 2) A rectangular stip of small side $2~{\rm cm}$ is removed from a square sheet . Removed rectangle is shaded in the figure. Area of the remaining part which is a rectangle in shape is $80~{\rm sq.cm}$



- a) If one side of the square is x then what is the small side of the unshaded rectangle?
- b) Find x by solving a second degree equation obtained from the given conditions.
- c) What is the area of the shaded rectangular strip?
- 3) The perimetre of a rectangle is 64 cm. Area 240 sq.cm
 - a) What is the sum of its length and breadth?
 - b) Form a second degree equation by taking one side as \boldsymbol{x}
 - c) Calculate the sides of the rectangle.
- 4) Sum of the area of two squares is 41 sq.cm , the difference of the sides is 1
 - a) If the side of the small square is x then what is the side of the big square?
 - b) Form a second degree equation using the given conditions.
 - c) Find the side of each square.
- 5) Sides of three squares are consecutive natural numbers. Sum of the area of these squares is 194
 - a) The side of the small square is x what is the side of other two squares?
 - b) Form a second degree equation using the given conditions.
 - c) Calculate the side of these squares.

- 6) Is it possible to draw a rectangle of area $5\,\,{\rm sq.unit}$ and perimetre $8\,\,{\rm unit.}\,$ Justify your answer .
- 7) Breadth, length and diagonal of a rectangle are in an arithmetic sequence with common difference 2. Area of the rectangle is 48 sq.cm
 - a) If the breadth is \boldsymbol{x} what is length and diagonal
 - b) Form a second degree equation and find its breadth and length
 - c) Calculate the perimetre of the rectangle.

SJ Notes on Focus Area

February 17, 2021

15

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

 $\blacksquare 30^\circ - 45^\circ - 90^\circ$ ത്രികോണവും $45^\circ - 45^\circ - 90^\circ$ ത്രികോണവും

- 1) Consider a square of perimetre $40 \mbox{cm}$
 - a) What is the length of its side?
 - b) What is the length of its diagonal
 - c) What is the area of the square drawn on its diagonal?
- 2) The area and perimetre of a square are equal in number.
 - a) What is the length of its side?
 - b) What is the length of its diagonal?
 - c) What is the area of the square drawn on its diagonal?
- 3) A bridge of length $600{\rm m}$ is built across a river making 45° angle with the direction of flow.
 - a) Draw a rough diagram.
 - b) What is the width of the river?
- 4) In traingle ABC , $\angle A = 30^{\circ}$, BC = 10 cm



a) What is the length AB?

- b) What is the length of the side AC?
- c) What is the length of the diagonal of the square drawn on AC?
- d) What is the perimetre of the square?

5) Consider an equilateral triangle of side $10\,{\rm cm}$

- a) What is its altitude?
- b) Draw a rough diagram of the square drawn on the altitude
- c) What is the area of this square.
- d) What is the length of its diagonal?

6) In the parallelogram ABCD , $\angle A = 60^{\circ}$, AB = 12 cm , AD = 10 cm



- a) What is the perpendicular distance from D to AB.
- b) Find the area of the parallelogram

7) In the rhombus $ABCD, \angle D = 150^{\circ}$



- a) What is the measure of $\angle A$?
- b) What is the diatance between AB and CD
- c) Find the area of the rhombus.

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SJ Notes on Focus Area

February 18, 2021

16

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

🔳 sine, cosineഎന്നീ കോണളവുകൾ

1) If $\sin A = \frac{3}{5}$ then what is $\cos A$?

(a) $\frac{4}{5}$ (b) $\frac{3}{4}$ (c) $\frac{1}{4}$ (d) $\frac{2}{5}$

2) In the figure given below $AB=8\ {\rm cm.lf}\ BC$ is perpendicular to AC then



a) What is the length AC?

b) What is the length BC?

3) Perimetre of an equilateral triangle is $30 \, \mathrm{cm}$

- a) What is the length a side?
- b) What is the altitude of this equilateral triangle?
- 4) In the figure O is the centre of the circle. $\angle ACB = 30^\circ$



- a) What is the measure of $\angle AOB$?
- b) What kind of triangle is OAB?
- c) If the radius of the circle is $12 {\rm cm}$ then what is the altitude of triangle OAB?
- d) What is the area of triangle OAB?

5) The diagonal of the rectangle ABC is $12 {\rm cm}$, $\angle BAC = 30^\circ$



- a) What is the length of the side AB?
- b) What is the length of the side BC?
- c) Calculate the area of the rectangle
- 6) ABCD is a quadrilateral $AC = CD = AD, \angle BAD = 120^{\circ}, \angle B = 90^{\circ}$, The perpendicular distance from D to the diagonal AC is 12 cm.



- a) What is the length of AC?
- b) What are the angles of triangle ABC ?
- c) What are the length AB and BC
- d) Find the area of triangle ABC.
- e) Find the area of triangle ADC.
- f) Find the area of the quadrilateral ABCD
- 7) There is a regular octagon of side $4\,\mathrm{cm}$. A quadrilateral is shaded .



- a) What is the measure of $\angle C$?
- b) What is the length rectangle ABCF
- c) Calculate the area of the coloured region.

SJ Notes on Focus Area

February 19, 2021

17

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

Heights and distances

- 1) Ramp makes an inclination 30° with the ground to the height 2 metre
 - a) Draw a rough diagram
 - b) What is the length of the ramp.
- 2) When the Sun appears the angle of elevation 45° the length of the shadow of a tree is found to be 17 metre.
 - a) Draw a rough diagram.
 - b) What is the height of the tree.
- 3) H_1, H_2 are the heights of two towers. When observed the tops from a point , which is the mid way of the line joining the towers are 60° and 30° . If $H_1 > H_2$ then
 - a) Draw a rough diagram.
 - b) Find $H_1: H_2$
 - c) If the tall tower has height 84 metre then what is the height of short tower.
 - d) If the height of the toll tower is 84 metre then what is the seperation between the towers .
- 4) when obeserved fro the top of a 50metre building the top and bottom of as tree some diatance away at the angle of depression 30° and 45° .
 - a) Draw a rough diagram
 - b) What is the distance from the foot of the building to the tree.
 - c) Calculate the height of the tree.
- 5) Observing from the top of a hill two points A and B are viwed at the angle of depression 30° , 45° . If the distance from A to B is 1 km
 - a) Draw a rough diagarm
 - b) what is the distance from the foot of the hill to the point ${\cal B}$
 - c) Calculate the height of the hill
- 6) A boat moves away from a light house of height 100 meter observes the angle of depression 60° from the top of the light house. After2minutes the angle becomes 45° .
 - a) Draw a rough diagarm
 - b) what is the distance between the points of obeservation?
 - c) What is the speed of the boat?
- 7) The top of building is observed from a point at the diatance a and b from the foot of a the building on either side .The angle of elevation are 30° , 60° .
 - a) Draw a rough diagram.

b) If h is the height of the building , prove that $h=\sqrt{ab}$

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SJ Notes on Focus Area

February 20, 2021

18

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

Concept of coordinate axes and coordinates of a point

How to locate the position of a point using coordinates

- 1) Draw coordinate axes and mark the points A(1,1), B(-3,2), C(-2,-3), (3,-2)
- 2) Draw coordinate axes and mark A(-2,-2)
 - a) Write the coordinates of B which is 4 unit away parallel to y axis in the upward direction.
 - b) Write the coordinates of C which is 6 unit in the right of B parallel to x axis
 - c) Write the coordinates of D which is 4 unit above C on the line parallel to y axis
 - d) What is the distance between A and D?
- 3) A(1,1), B(-3,1), C(-3,-4), D(1,-4) are the oordintes of the vertices of a rectangle.
 - a) What is the length of the side AB?
 - b) What is the length of the side AD?
 - c) Calcualte the perimetre and area of the rectangle.
- 4) There is a circle with centre at the origin . The circle passes through (5,0)
 - a) What is the radius of the circle?
 - b) What are the coordinates of the points where the circle cut the axes?
 - c) Is (3,4) a point on the circle? How can we realize it?
- 5) The line passing through (0, 4) parallel to x axis and the line passing through (4, 0) and parallel to y axis meet at a point.
 - a) Write the coordinates of the intersecting point.
 - b) What is the diatance from origin to the intersecting point.
 - c) A circle is drawn with the origin as the centre and distance from origin to the intersecting point as radius. What are the points where the circle cut the axes.
- 6) The vertices of a right triangle are A(1,1), B(4,1), C(1,5).
 - a) Name the vertex at which 90° angle is taken
 - b) What is the length of perpendicular sides?
 - c) What is the length of its hypotenuse?
 - d) What is the radius of its circumcircle?

- 7) riangle ABC is an equilateral triangle. Side AB coincides x axi. If A(-1,0), B(5,0) then
 - a) What is the length of AB?
 - b) What is the altitude of the triangle?
 - c) What are the coordinate pairs of C?
- 8) Three vertices of ABCD are A(0,0), B(8,0)C(8,4)
 - a) Write the coordiantes of ${\cal D}$
 - b) Find the perimetre of the rectangle.
 - c) Calculate the area of the rectangle.
- 9) A(4,0), B(0,4), C(-4,0), D(0,-4) are the vertices of a quadrilateral
 - a) Suggest a suitable name to ABCD
 - b) Find the length of a side?
 - c) Calcualte the area and perimetre
- 10) In triangle ABC, A(1,2), B(7,2) are two vertices.
 - a) What is the length of the side AB
 - b) In triangle ABC, $\angle A = 90^{\circ}$. Write a pair of coordinates of C
 - c) What is the length of side AC?
 - d) Calculate the area of the triangle.

SJ Notes on Focus Area

February 21, 2021

19

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

📕 വശങ്ങൾ സൂചകാക്ഷങ്ങൾക്ക് സമാന്തരമായ ചതുരങ്ങൾ , സമചതുരങ്ങൾ ,ചില ജ്യാമിതീയരൂപങ്ങൾ

1) P(3,4) is a point on a circle with centre at the origin



- a) What is the radius of the circle?
- b) PQRS is a rectangle with its vertices are on this circle, sides are parallel to the axes . Write the coordinates of its vertices.
- c) What are the points where the circle cut axes
- d) Calculate perimetre and area of the rectangle.
- 2) OABC is a parallelogram O(0,0), A(4,0), B(6,5)



- a) Write the coordinates of C
- b) Write the length of OA and BC

- c) What is the diatance between the parallel sides OA and BC
- d) Calculate area and perimetre of the parallelogram
- 3) P is a point on the circle with centre at the origin and radius 5.If OP makes an angle 30° with the centre,



- a) What are the points where the circle cut axes?
- b) Write the coordinates of ${\cal P}$
- c) The vertices of the rectangle PQRS, with the sides parallel to the axes are on the circle.Write the coordinates of the vertices.
- 4) ABCD is a rectangle ,sides are parallel to the axes .If $A(3,2),\,AB\,=\,6,\,BC\,=\,5{\rm then}$



- a) Write the coordinates of B, C, D
- b) Find the perimetre of the rectangle.
- c) Calculate the area of the rectangle.
- 5) The perpendicular sides of the right triangle coincides the axes,right angle is at the origin . The mid point of the hypotenuse is (6,8). If the sum of the perpendicular sides is 28
 - a) What is the radius of the circumcircle.
 - b) What is the length of its hypotenuse?
 - c) Find the area of the triangle.

6) P(3,4) is a point in a circle with centre at the origin. Q(x,y) is another point on this circle , $\angle AOQ = 30^{\circ}$ then



- a) What is the radius of this circle?
- b) What are the opoints where the circle cut the axes ?
- c) Write the coordinates of ${\boldsymbol{Q}}$
- d) Write the coordinates of three more points on this circle.

7) ABCD is an isosceles trapezium.A(1,1), B(8,1), AB is parallel to CD.If $AD = 4, \angle A = 30^{\circ}$ then



- a) What is the length AB?
- b) Write the coordinates of D
- c) Write the coordinates of ${\boldsymbol C}$
- d) Calculate the area of the trapezium.

8) ABC is an equilateral triangle. If A(1,1), B(7,1) then



- a) What is the length of one side?
- b) What is the altitude of this triangle?
- c) Write two pair of the coordinates of C
- d) Calculate the area of the triangle.

9) $\left(2,1
ight)$ is a point on the circle with centre at the origin.



a) What is the radius of the circle?

- b) What are the points where the circle cut the axes?
- c) Write the coordinates of $7\ \mathrm{more}\ \mathrm{points}\ \mathrm{on}\ \mathrm{this}\ \mathrm{circle.}$

10) In the figure ABCD is a square. $OD = 10, \angle AOD = 30^{\circ}$.



a) Write the coordinates of \boldsymbol{A}

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- b) What is the length of one side of the square?
- c) Write the coordinates of the vertices of the square.

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SJ Notes on Focus Area

February 22, 2021

20

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

- 1) Complete the following activities
 - a) Draw coordinate axes and mark the points $P(x_1, y_1), Q(x_2, y_2)$
 - b) Draw a line through P parallel to $x {\rm axes},$ a line passing through $Q {\rm parallel}$ to $y {\rm axis}$
 - c) Mark the intersecting point as R
 - d) Calcualte the length PR and QR
 - e) Prove that $PQ = \sqrt{(x_2 x_1)^2 + (y_2 y_1)^2}$
- 2) Using the diatance formula calculate the following.
 - a) The distance between P(-6,7) and Q(-1,-5)
 - b) What is the distance from origin to (-5, 12)
 - c) Find the distance between P(-7,-3) and , Q(-5,-11)
- 3) The distance between A(2, y) and B(-4, 3) is 10 unit
 - a) Form an equation using the diatance formula
 - b) What are the real numbers suitable for y?
 - c) Write the coordinates of these points .
- 4) Consider the points A(1, -1), B(5, 2), C(9, 5)
 - a) Find the distance AB ,BC and AC
 - b) Prove that these points are on a line.
 - c) What is the mid point of AC?
- 5) P(x,y) is equidistant from A(5,1) and B(1,5)
 - a) What is the relation between x and y
 - b) How many triangles are there with AB as the base and satisfying this condition.
 - c) What is the altitude if ABP is an equilateral triangle.

- 6) The distance from a point P on x axis to ${\cal A}(7,6)$ and ${\cal B}(-3,4)$ are equal
 - a) What is the y coordinate of P
 - b) Form an equation using the distance formula.
 - c) Write the coordinates of ${\cal P}$
 - d) Find the sides of $\triangle ABP$.
- 7) Consider the points A(4,2), B(7,5), C(9,7)
 - a) Find the distances AB, BC and AC
 - b) Can we construct $\triangle ABC$? why?
 - c) Write the property of these points.
- 8) The distance from x axis to (7, -4) is $2\sqrt{5}$.
 - a) Take a point on x axis and form an equation.
 - b) How many points are there on x axis satisfying this condition.
 - c) What is the distance between these points.
- 9) Consider the points A(0, 1), B(1, 4), C(4, 3), D(3, 0)
 - a) Find the sides of ABCD
 - b) Find the length of diagonals.
 - c) Suggest a suitable name to this quadrilateral.
- 10) Consider the points A(2, -2), B(14, 10), C(11, 13), D(-1, 1)
 - a) Find the sides of ABCD

- b) Find the length of the diagonals.
- c) Suggest a suitable name to this quadrilateral.

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SJ Notes on Focus Area

February 23, 2021

20

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

- 1) Construct a tangent to a circle by the steps given below
 - a) Draw a circle of radius 3 cm and mark a point P on the circle.
 - b) Mark ${\cal O}$ as the centre of the circle and draw the radius ${\cal OP}$
 - c) Draw the tangent to the circle at P
 - d) Draw another tangent to this circle parallel to the first tangent.
- 2) Draw suitable figure and find the lengths asked in the quaestion.
 - a) A tangent of length 12cm is drawn to a circle from a point outside the circle. If the radius of the circle is 5cm find the distance from centre to the exterior point from which the tangent is drawn.
 - b) What is the length of tangent drawn from a point at the distance $10\ {\rm cm}$ away from centre of a circle of radius $6{\rm cm}$
 - c) A tangent is drawn from a point at the distance 26 cm away from the centre of a circle. If the length of the tangent is 24 cm find the radius of the circle.
- 3) In the figure O is the center of the circle, $\angle OPA = 30^{\circ}, OP = 16$ then
 - a) Draw a rough diagram
 - b) What are the angles of $\triangle OAP$
 - c) What is the radius of the circle?
 - d) What is the length of the tangent?
- 4) In the figure O is the centre of the circle. A tangent PA is drawn from P outside the circle at the diatance 12cm from the centre. If the length of the tangent and radius are equal then
 - a) Draw a rough diagram
 - b) What are the angles of $\triangle OAP$?
 - c) What is the length of tangent and radius?
- 5) O is the centre of a circle. A tangent PA is drawn from the outer point P to the circle at A
 - a) Draw a rough diagram.
 - b) If $\angle POA = 60^{\circ}$ then what are the other angles of $\triangle OAP$
 - c) If $\angle POA = 60^{\circ}$, and the radius of the circle is 10 cm find the length of tangent.
 - d) What is the length of the line ${\cal OP}$
- 6) In the figure $\angle OPA = 40^{\circ}$, OP = 18cm then



- a) What is the measure of $\angle AOP$?
- b) What is the radius of the circle?
- c) What is the length of the tangent? $[\sin 40 = 0.6428, \cos 40^\circ = 0.7660, \tan 40 = 0.8391]$
- 7) In the figure $\angle POB = 120^{\circ}, OP = 24 {\rm cm}$, AB is the diametre of the circle.



- a) What are the angles of $\triangle POA$?
- b) What is the diametre of the circle?
- c) What is the length of the tangent from ${\cal P}$
- 8) The length of tangent drawn from a point at a distance 8 cm from the centre to a circle is 4 cm. Construct the tangent. Measure the radius of the circle and write aside.
- 9) In the figure the length of tangent PA is 12cm and PB = 7cm . what is the radius of the circle?



10) In the figure O is the centre of the circle and PA is a tangent. If the area of the triangle is OPA is $6~{\rm sq.cm}$ and $OP=5{\rm cm}$



- a) What is the radius of the circle?
- b) What is the length of tangent?

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SJ Notes on Focus Area

February 24, 2021

22

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

1) In the figure PA, PB are tangents . O is the centre of the circle.



- a) What are the measures of $\angle OAP, \angle OBP$?
- b) If $\angle APB = 40^\circ$ then what is the measure of $\angle AOB$
- c) The lines AB and CD intersect at C .What is the relation between the length of lines CO, CP, CA and CB?
- 2) In the figure PA and PB are tangents O is the centre of the circle , $\angle AQB = 50^{\circ}$ then



- a) What is the measure of $\angle AOB$?
- b) What is the measure of angle $\angle ARB, \angle APB$?
- 3) In the figure $O{\rm is}$ the centre of the circle, PA,PB are tangents . If $\angle OAB=20^{\circ}{\rm then}$



a) What is the measure of $\angle AOB$ and , $\angle AQB?$

- b) What is the measure of $\angle ARB$?
- c) What is the measure of $\angle APB$?

4) Draw two tangents from an outer point of a circle of radius 3cm such that the angle between the tangents is 60°

- a) What is the distance from centre to the outer point?
- b) What is the length of tangents തൊടുവരയുടെ (തൊടുവരകളടെ)നീളം എത്ര?
- 5) Two angles of a trinagle are $40^\circ, 60^\circ.$ The sides of the triangle touches a circle of radius $3~{
 m cm}$
- 6) The sides of an equilateral triangle touches the a circle of radius 3 cm .Construct the triangle.
- 7) In the figure PA and PB are the tangents to the circle . $\angle ACB = \frac{1}{3} \times \angle APB$
 - a) If $\angle APB = x$ then find $\angle ACB, \angle AOB, \angle ADB$
 - b) Find x
 - c) Find the measure of $\angle ACB, \angle AOB, \angle ADB$

8) One angle of a rhombus is 60° . The sides touches a circle of diametre 5cm . Construct the rhombus.

9) In the figure O is the centre of the circle. PA and PB are the tangents. If $\angle ADB = 110^{\circ}$ then



- a) Find the measure of $\angle ACB$
- b) Find the measure of $\angle AOB$
- c) Find the measure of $\angle APB$

10) Two angles of a triangle are $120^\circ, 40^\circ$. The sides touches a circle of radius 3 cm . Construct the triangle.

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SJ Notes on Focus Area

February 25, 2021

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(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

- 1) A sectoral sheet of central angle 120° is cut off from a circular sheet of radius 12cm. It is rolled in such a way as to get a cone.
 - a) What is the slant height of the cone?
 - b) What is the radius of the cone ?
 - c) Find the curved surface area of the cone.
- 2) A cone is made by rolling a semicircular metal sheet of radius $10 \mbox{cm}$
 - a) What is the slant height of the cone.
 - b) What is the radius of the cone.
 - c) Find the curved surface area of the cone.
 - d) Base is made by a suitable circular sheet. What is its total surface area ?
- 3) A circular sheet of card board of radius 12 cm .lt is cut off into two sectors of central angle 120° and 240° .Both of them are rolled into cones.
 - a) Name the measure coomon to both comes
 - b) What is the radius of small cone?
 - c) What is the radius of the big cone.
 - d) How radii of the cones are related to the radius of the circular sheet.
- 4) A sector of central angle 90° is cut off from a circular sheet of radius 16 cm .lt is rolled in such a way as to get a cone.
 - a) What is the lateral surface are of the cone?
 - b) What is the radius of the cone?
 - c) The remaining part of the circular sheet is also rolled to get a cone . What is its base radius?
 - d) Which cone has more height ? Explain
- 5) A cone is made by a sectoral sheet taken from a circular sheet. The slant height of the cone is two times its radius.
 - a) What is the relation between lateral surface area and base area?
 - b) If the base perimetre is 20π cm then what will be its lateral surface area ?
 - c) What is the central angle of this sector?
 - d) The remaining part is also rolled to get a cone. What is the ratio of the heights of cones so formed

- 6) A cone of radius r_1 is made by using a sector of a circular sheet of radius R. The remaining part of the sheet is rolled in such a way as to get another cone of radius r_2
 - a) Which measure is common in both cones?
 - b) Write the relation between the radius , slant height and central angle of the sector in the case of first cone.
 - c) Write the relation between the radius , slant height and central angle of the sector in the case of second cone.
 - d) prove that $R = r_1 + r_2$
- 7) A cone is made by taking a sector from a circular sheet. The slant height of the cone is $25 {\rm cm}$ and its radius $110 {\rm cm}$
 - a) What is the radius of the circular sheet?
 - b) What is the central angle of the sector?
 - c) What is the central angle of the remaining part?
 - d) What is the radius of the cone made by rolling the remaining part?
- 8) The base perimetre of a cone is 20π cm, slant height 18 cm . It is rolled to get a cone.
 - a) What is the radius of the sector?
 - b) What is the radius of the cone?
 - c) What is the central angle of the sector?
 - d) Find the lateral surface area of the cone?
- 9) A sector of central angle 288° and radius 25 cm is taken from a circulat sheet .
 - a) What is the radius of the cone?
 - b) What is the height of the cone?
 - c) Find the lateral surface area of the cone?
 - d) What is the radius of the cone made by rolling the remaining part?
- 10) A cone of maximum size is carved from a square prism of base edge 10 cm and height 12 cm.
 - a) What is the radius of the cone?

- b) What is the slant height of the cone?
- c) What is the lateral surface area of the cone?
- d) Find the total surface area of the cone?

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SJ Notes on Focus Area

February 26, 2021

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(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

1) ABCD is a parallelogram . If A(1,1), B(4,2), C(6,7) then



- a) Write the difference between x coordinates of A and B
- b) Write the difference between \boldsymbol{y} coordinates of \boldsymbol{A} and \boldsymbol{B}
- c) Write the coordinates of D.

2) In the figure PQRS is a parallelogram .If $P(0,3), PS=4, Q(5.4) {\rm then}$



- a) Write the coordinates of ${\boldsymbol S}$
- b) Write the coordinates of ${\cal R}$
- c) Find the length of the sides.

- 3) P(1,4) the mid point of the side AB ,Q(2,3) is the mid point of side BC , R(5,6) is the mid point of side AC
 - a) Draw a suitable diagram representing the position of points
 - b) Write the coordinates of ${\cal B}$
 - c) Write the coordinates of C
 - d) Write the coordinates of ${\boldsymbol A}$
- 4) In triangle ABC, A(-3, 2), B(1, 5), C(3, -4) then
 - a) Find the coordinates of the mid point of AB
 - b) Find the coordiantes of the mid point of BC
 - c) Find the coordinates of the mid point of $A\!C$
- 5) Draw x axis and y axis (rough diagram), mark the points ${\cal A}(4,3)$ and ${\cal B}(12,7)$
 - a) What is the slope of this line?
 - b) Write the coordinates of another point on this line?
 - c) How many lines are there having the same slop?
- 6) Consider the points A(2,3), B(3,4), C(4,5)
 - a) Find the slope of the line passing through A(2,3) and B(3,4)
 - b) Find the slope of the line passing through B(3,4) and C(4,5)
 - c) Are these points on a line? How can we realize it.
 - d) Write the coordinates of one more point on the line?
- 7) Consider the points A(2,0), B(-6,-2), C(-4,-4), D(4,-2)
 - a) Find the slope pf the lines AB and CD
 - b) Find the slope of the line AD and BC
 - c) Is ABCD a parallelogram ?Explain

8) Consider the points A(2, -3), B(-5, 1), C(7, -1), D(0, 3)

- a) Find the slope of the line AB
- b) Find the slope of the line CD
- c) Are these points the vertices of a parallelogram?
- 9) A(1,-2), B(x,4) are the points on a line of slope x.
 - a) Find \boldsymbol{x}
 - b) Write the coordinates of another point on this line
 - c) Find the point at which the line $\operatorname{cut} x$ axis
 - d) Find the point at which the line $\operatorname{cut} y$ axis
- 10) A(-4,2), B(2,6), C(8,5), D(9,-7) are the vertices of a quadrilateral
 - a) Find the coordinates of the mid point of the sides.
 - b) Prove that the quadrilateral formed by the mid points is a parallelogram
 - c) Find the coordinaters of the point where the diagonals intersect.
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SJ Notes on Focus Area

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(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

- 1) The sides of a rectangle are (x 3) and (x + 1)
 - a) Find the area a(x)
 - b) If x = 4 then what is its area ?
 - c) If x = 0 is it possible to get a rectangle ? Why?
 - d) What is the condition for x to get a rectangle?
- 2) Consider the polynomial $p(x) = x^3 4x^2 + 2x + k$
 - a) If x is a factor then find x.
 - b) x 1 is a first degree factor of p(x) then what is k?
 - c) Use k for becoming x-1 a factor and write the polynomial
 - d) Is (x + 1 a factor of this polynomial .

3) If $p(x) = x^3 - 4x^2 + 6x - k$ then

- a) Find k such that x 1 a factor of p(x)
- b) Write the polynomial . Is (x + 1) a factor of p(x)
- c) What is the speciality of the coefficients of p(x) having x 1 a factor
- d) Write three polynomials having x-1 a factor

4) Consider the polynomials $p(x) = x^3 + 1$, $q(x) = x^3 + x^2 + x + 1$

- a) Find p(-1) and q(-1)
- b) What is the factor common to both the polynomials
- c) Find r(x) = p(x) + q(x)
- d) what is the first degree factor of r(x)

5) $x^2 - 1$ is the factor of $p(x) = a^3 + bx^2 + cx + d$

- a) Find p(1), p(-1)
- b) Show that a = -c, b = -d
- c) Write a polynomial having $x^2 1$ a factor

6) If $p(x) = x^3 - 8$ then

- a) Check whether x-2 a factor of p(x)
- b) Write a first degree factor of $x^3 27$
- c) What is the second degree factor of $x^3 27$
- 7) Consider the polynomial $p(x) = 3x^2 + 4x + 1$
 - a) Write p(x) as the product of two first degree factors
 - b) Find the solution of the equation p(x) = 0

- 8) Consider the equation $p(x) = x^3 + 4x^2 + x 7$
 - a) Check whether x-1 a factor of this polynomial or not
 - b) If not what should be subtracted from p(x) to get another polynomial q(x) in which x-1 is a factor
 - c) Write q(x) as the product of three first degree factors
 - d) Write the solution of the equation q(x) = 0.
- 9) Consider the polynomial $p(x) = ax^2 2bx + c$

- a) If x 1 is a factor of p(x) prove that a, b, c are in an arithmetic sequence.
- b) Write twp polynomials in the form $ax^2 2bx + c$ such that a, b, c are in an arithmetic sequence .
- c) If $x^2 1$ is a factor of p(x) then what is a + b ?

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SJ Notes on Focus Area

February 28, 2021

<mark>26</mark>

(This is a simplified special package based on focus area mathematics X in the year 2021 SSLC Examination)

1) Atmospheric tempereature of seven days in a week are given below .

 $26^{\circ}C, 28^{\circ}C, 25^{\circ}C, 30^{\circ}C, 27^{\circ}C, 26^{\circ}C, 25^{\circ}C$

- a) Write the numbers in the ascending order.
- b) Calculate the mean of the temperatures.
- c) What is the median temperature?
- d) How many days are having temperature less than median temperature?
- e) How many temperatures are there below median temperature?
- 2) Consider th counting numbers from 1 to 100.
 - a) How many multiples of 7 are there below 100?
 - b) Calculate the mean of the multiples of 7 below 100.
 - c) What is the median of the multiples of 7 belw 100?
 - d) How many multiples are there more are median in this collection ?
- 3) The marks obtained in ten class tests are given below

14, 17, 11, 19, 15, 17, 13, 10, 14, 18

- a) Calculate the mean of the marks .
- b) What are the marks comes in the middle if the marks are arranged in the increasing order?
- c) What is the median mark ?
- d) How many class tests are there scoring mark above median mark?
- 4) Consider the arithmetic sequence $7, 10, 13 \cdots$
 - a) How many terms are there below 100?
 - b) Which term comes in the middle?
 - c) Calculate the mean of the numbers in the sequence below 100
 - d) CXalculate the median of numbers in the sequence below100
 - e) What is the relation between mean and median?

- 5) The algebraic form of an arithmetic sequence is 3n+2
 - a) Write the sequence
 - b) Calculate the mean of first $20\ {\rm terms.}$
 - c) Calculate the median of the first 20 numbers of this sequence number of this sequence .
 - d) What is the relation between mean and median.
- 6) Consider a group of numbers in an arithmetic sequence
 - a) What is the general form of its algebra?
 - b) Calculate the mean of these numbers
 - c) Find the median.
 - d) Are mean and median equal?Write a statement about the result.
- 7) The scores of $40\ {\rm students}$ in a quiz are given below

Score	4	6	9	10	15
Number of Children	5	10	10	7	8

- a) Calculate the total score in the class
- b) Calculate mean score
- c) Find the median of the scores
- d) How many students are there above median score ?
- 8) The weights of 12 members of a team are given below

Weight	67	70	72	73	75
Number of members	4	3	2	2	1

- a) Prepare a table for calculating the median
- b) What is the median of the weights ?
- c) How many members are having medsian weight and below?
- d) How many members are there above median weight?
- 9) The daily wages of 200 workers in a factory are given below .

Wages	350	400	450	500	550	600
No. Workers	14	50	30	40	36	30

- a) Prepare the table for calculating the median.
- b) Find the median wage.
- c) How many workers are getting median wage and below ?
- d) How many workers are getting median wage and above ?

10) Answer the following questions.

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- a) Find the mean of $100 \ \mathrm{odd} \ \mathrm{numbers}$.
- b) Find the median of first $100 \mathrm{odd}$ numbers
- c) What is the mean of first \boldsymbol{n} even numbers ?
- d) What is the median of first \boldsymbol{n} even numbers ?

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