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WEFI -**SSF** SSLC - EXCELLENCY TEST - 2021

MATHEMATICS (ENGLISH)

Total Score : 80

Time : $2\frac{1}{2}$ Hours

Instructions :

- First 20 minutes is the cool off time. You may use the time to read the questions and plan your answers.
- Attempt the questions according to the instructions.
- Keep in mind the score and the time while answering the questions.
- The Maximum score for questions from 1 45 will be 80.
- Simplify using the approximate values of π , $\sqrt{2}$, $\sqrt{3}$ only if it is asked to do in questions

Questions from 1 to 5 carry one mark each. (Choose correct answer from the bracket)

- 1. The fifth term of the arithmetic sequence4, 11, 18, is _______ (25, 24, 31, 32)
- 2. In the figure 'O' is the centre of circle and A, B, C, D are on it. If $\angle BAD = 70^{\circ}$ then $\angle BCD =$ _____

(140°, 110°, 20°, 70°)



C 45° A 6 cm B

3. In the figure $\angle A = 90^\circ$, $\angle B = \angle C = 45^\circ$ and AB = 6 cm. What is the length of BC?

 $(6 \text{ cm}, 6\sqrt{2}\text{ cm}, 6\sqrt{3} \text{ cm}, 12 \text{ cm})$

- 4. Which of the following point is on the X axis? ((3,2), (-3, 2), (0, 5), (5, 0))
- 5. If $P(x) = x^2 + 3x + 1$, then P(0) =_____ (0, 1, 2, -1)

Questions from 6 to 10 Carry two score each.

- 6. Find the mean of the following scores. *12, 8, 13, 15, 9, 16, 11*
- 7. Algebraic form of an arithmetic sequence is 5n+2a) Find the common difference of this sequence?
 - *b*) Find its 10^{th} term.
- 8. When each side of a square was increased by 3 cm, the area became 324 sq. cms.
 - *a)* Let *x* be the length of side of the original square. What is the length of side of new square?
 - b) What is the length of side of the original square?
- 9. In the figure, ABCD is a rectangle with sides parallel to the axes. Co-ordinates of A and C are (1, 3) and (7, 7) respectively. Find co-ordinates of B and D.



10. In the figure, 'O' is the centre of the circle, PA an PB are tangents.



Questions from 11 to 20 Carry three score each.

- 11. Draw a circle of radius 3cm. Then mark a point which is 7cm away from the centre of the circle, and draw Tangents from this point to the circle.
- 12. In the figure, PA = 15cm, PB = 8cm and the length of PD is 2cm more than the length of PC.
 - *a)* How much is PC x PD ?
 - *b)* Let *x* as the length of PC, form a second degree equation.
 - *c)* Find length of PC?



- 13. The 4^{th} term of an arithmetic sequence is 64, and its 14^{th} term is 104.
 - a) Find its common difference?
 - b) Find its 13^{th} term?
 - c) Find the sum of first 25 term of this sequence.
- 14. Construct a triangle and its circumcircle with angles 70°, 80° and with circumradius 4cm.
- 15. A bag contains 12 white balls and 8 black balls. If a ball is taken from the bag without looking into it.
 - a) What is the chance of being that ball is a white one?
 - b) What is the chance of being that ball is a black one?
 - c) How many white balls should be added to the bag to make the probability of drawing a black ball is $\frac{1}{3}$?
- 16. In the figure ABCD is a parallelogram. $AB = 12 \text{ cm}, AD = 8 \text{ cm}, \angle B = 120^{\circ}$.
 - *a*) Find $\angle A$?
 - *b)* Find the length of perpendicular from D to AB



- c) Find the area of parallelogram ABCD?
- 17. Base radius of a cone is 12 cm, and its height is 16 cm.
 - a) Find the slant height of the cone.
 - b) Find the radius and central angle of the sector needed to make this cone.
- 18. If (5, 2) is a point on the line parallel to Y axis
 - a) Find the coordinates of the point where this line meets the X axis.
 - b) Find the distance between these two points?
 - c) Find the distance between this line and Y axis?

- 19. If $P(x) = x^2 7x + 12$
 - *a) Find P*(*3*)
 - b) Check whether (x-4) is a factor of P(x), or not?.
 - c) Write P(x) as the product of two first degree polynomials.
- 20. In the figure, P(4,2),Q(5,4) and R(3,3) are mid-points of the sides of triangle ABC.Find co-ordinates of A,B and C



Questions from 21 to 30 carry four score each.

21. The table below shows marks of the students of a class. Find the median mark.

| Mark | No; of students | | | | |
|------|-----------------|--|--|--|--|
| 12 | 4 | | | | |
| 15 | 5 | | | | |
| 18 | 8 | | | | |
| 21 | 4 | | | | |
| 24 | 6 | | | | |
| 27 | 2 | | | | |

- 22. In the figure, PQ is a tangent through the point A. $\angle ADC = 110^{\circ} \text{ and } \angle DAQ = 40^{\circ}$. Find the following angles
 - a) ∠ACD
 - *b*) ∠ABD
 - c) $\angle ABC$
 - *d*) ∠PAC



- 23. Construct a rectangle of length 6 cm and breadth 4 cm, Then construct a square having area equal to that of the rectangle.
- 24. Find the following sums.
 - *a)* 1+2+3+4+.....+40 *b)* 4+8+12+16+.....+160
 - c) 6+10+14+18+....+162
 - *d*) 10+18+26+34+.....+322

- 25. Perimeter of a rectangle is 68 cm and its area is 240 square centimeters.
 - *a)* Find sum of its length and breadth?
 - b) If its breath is 17-xthen what is its length?
 - *c)* Form a second degree equation and find its length and breadth.
- 26. In the figure, AC = 20 cm. $\angle B = 45^\circ$, $\angle C = 30^\circ$ and AD perpendicular to BC.
 - *a*) Find ∠BAC
 - b) Find the length of AD.
 - c) Find the perimeter of triangle ABC.
 - d) What is the ratio of sides of a triangle, If the ratio of its angles is 2:3:7?
- 27. *a*)Draw X, Y axes and mark points A (-1, 1) and B (5, 1) *b*)If D is the mid-point of AB. Then find the coordinate of D. *c*)If ABC is an equilateral triangle. Then find the coordinate of C
- 28. A lateral face of a square pyramid is as shown below
 - *a)* Find the length of its base edge.
 - b) Find is slant height.
 - c) Find the lateral surface area of the square pyramid.
 - d) Find the height of the square pyramid.



60° 60° 30 cm

29. $P(x) = x^2 - 7x + 8$

- a) Find P(l)
- b) Write a factor of P(x) P(1).
- c) If (x-6) is a factor of x^2-7x+k , then find k.
- d) Write P(x)-P(1) as the product of two first degree polynomials.
- 30. *a)* Write an arithmetic sequence with first term 8 and common difference 3.
 - b) Check whether 100 is a term of this sequence or not?
 - c) Can the difference of any two terms of the sequence be 501?
 - d) At what position, 125 occurs in this sequence?

Questions from 31 to 45 carry five score each.

- 31. Sum of 15th and 16th terms of an arithmetic sequence is 200.
 - *a)* What is the sum of 1^{st} and 30^{th} terms?
 - *b)* Find the sum of first 30 terms If its10th term is 78.
 - *c)* Find 21^{st} term?
 - *d)* Find the common difference?
 - e) Write it's algebraic form.

- 32. Draw a circle of radius 2.5cm, Then draw a triangle with angles 50°, 60°, and 70° and with all its sides are touching the circle.
- 33. A cone of maximum size is curved from a solid wooden cylinder of base radius 18 cm and height 24cm,
 - *a)* What is the base radius of the cone?
 - b) What is the slant height of cone?
 - c) Find the total surface area of the cone.
 - *d*) Find the volume of the cone.
- 34. Consider the arithmetic sequence 81, 77, 73,
 - *a)* What is the common difference?
 - b) What is the remainder when each positive term of this sequence is divided by 4?
 - c) Which is the smallest positive number of this sequence?
 - d) Write its algebraic form.
 - e) How many positive numbers are there in this sequence?
- 35. The table below classifies workers of a company according to their wages

| Daily wages (in Rupees) | 200-300 | 300-400 | 400-500 | 500-600 | 600-700 | 700-800 |
|-------------------------|---------|---------|---------|---------|---------|---------|
| No; of workers | 5 | 7 | 10 | 6 | 4 | 3 |

- *a)* If the workers are lined up according to their daily wages, then worker in which position has the median wage?
- b) Which is the median class?
- c) What is the assumed wage of worker in 13^{th} position?
- *d*) Find median daily wage.
- 36. A man standing in the foot of a building sees the top of a tower which is 50 meter away from the building, at an angle of elevation 60°. And from the top off the building he sees the same at an angle of elevation 45°.
 - *a)* Draw a rough figure based on these details.
 - b) Find the height of the tower?
 - c) Find the height of the building?
- 37. Co-ordinates of the end points of a diameter of a circle are (1,3) and (11,3)
 - *a)* Find the length of the diameter?
 - *b)* Write the co-ordinates of the centre.
 - c) Check whether (6, 8) is a point on this circle or not.
 - d) Write the co-ordinates of any other point on the same circle.

38. In the figure,

 $\angle A = 40^{\circ}, \ \angle C = 100^{\circ}, AB = 20 \text{ cm} \text{ and}, AC = 14 \text{ cm}.$ *a)* Find $\angle B$ *b)* Find the length of BC *c)* Find the perpendicular distance from C to AB. *d)* Find the perimeter of triangle ABC. *e)* Find the area of triangle ABC. *sin 40^{\circ} = 0.64 cos 40^{\circ} = 0.76*

 $Sin 40^{\circ} = 0.76 \\
Sin 50^{\circ} = 0.76 \\
cos 50^{\circ} = 0.64$

- 39. 2 is added to the product of two consecutive multiple of 7 gives 590.
 - a) If the first of these two multiples is x, then what is the second one?
 - b) Form a second degree equation and find these multiples.
- 40. Height of a solid metallic cone is double of its base diameter?
 - a) If the base radius is 'r', then what is its height?
 - b) Find the volume of the cone.
 - c) This cone is melt and recast into spheres of radius equal to half the base radius of the cone. How many such spheres can be made?
- 41. a) Find the slope of the line segment AB, where A is (6,4) and B is (10, 10)b) If the co-ordinates of C is (18, 22), Find the slope of BC.
 - c) Check whether A, B, and C are lying on a line or not? Why?
 - d) Write co-ordinates of any other point on this line.
- 42. a) Find the diameter of the circle given below.b) Find the coordinates of the centre of the circle.c) Write the equation of the circle.



- 43. In figure, CD is the diameter of the circle and PQ is the tangent through D. If $\angle ACB = 50^{\circ}$ and $\angle ABC = 70^{\circ}$, Then find the following angles.
 - a) ∠CAD
 - *b*) ∠ADC
 - c) $\angle PDC$
 - *d*) ∠BAD
 - e) ∠APQ



- 44. In the figure AB, CD are two chords perpendicular to each other. If $\angle ACD = x^{\circ}$
 - *a*) Find $\angle ABD$
 - *b*) Find \angle BDC
 - *c)* Find the sum of central angles of arc APD and arc BQC.
 - d) If the length of arc APD is 3 cm and Length of arc BQC is 7 cm then find the perimeter of the circle.



45. All two digit numbers are written in a separate paper slips and put in to a box.a) How many slips are there in the box?

A slip is taken from the box without looking into it, then

- b) What is the probability of getting a number for which both the digits are same?
- c) What is the probability of getting an even number?
- d) What is the probability of getting a perfect square?
- *e)* What is the probability of getting a number for which the sum of digits is equal to 15?