

INTEGRALS

Class-1

Integration is the inverse process of differentiation. The process of finding the original function when derivative of a function is given is called integration. After integration we have to add a constant called constant of integration.

If $\frac{d}{dx} F(x) = f(x)$ then

$$\int f(x) dx = F(x) + C$$

Results

$$1, \int x^n dx = \frac{x^{n+1}}{n+1} + C, n \neq -1$$

$$2, \int \frac{1}{x} dx = \log |x| + C$$

$$3, \int 1 \cdot dx = x + C$$

$$4, \int \frac{1}{\sqrt{x}} dx = 2\sqrt{x} + C$$

$$5, \int \frac{1}{x^2} dx = -\frac{1}{x} + C$$

$$6, \int e^x dx = e^x + C$$

$$7, \int a^x dx = \frac{a^x}{\log a} + C$$

$$8, \int \sqrt{x} dx = \frac{x^{3/2}}{3/2} + C$$

$$(9) \int \sin x dx = -\cos x + C$$

$$(10) \int \cos x dx = \sin x + C$$

$$(11) \int \sec^2 x dx = \tan x + C$$

$$(12) \int \sec x \cdot \tan x dx = \sec x + C$$

$$(13) \int \operatorname{cosec}^2 x dx = -\cot x + C$$

$$(14) \int \operatorname{cosec} x \cdot \cot x dx = -\operatorname{cosec} x + C$$

$$(15) \int \frac{1}{\sqrt{1-x^2}} dx = \sin^{-1} x + C$$

$$(16) \int \frac{-1}{\sqrt{1-x^2}} dx = \cos^{-1} x + C$$

$$(17) \int \frac{1}{1+x^2} dx = \tan^{-1} x + C$$

$$(18) \int \frac{-1}{1+x^2} dx = \cot^{-1} x + C$$

$$(19) \int \frac{1}{|x| \sqrt{x^2-1}} dx = \sec^{-1} x + C$$

$$(20) \int \frac{-1}{|x| \sqrt{x^2-1}} dx = \operatorname{cosec}^{-1} x + C$$

$$21, \int k \cdot f(x) dx = k \int f(x) dx$$

$$22, \int k \cdot dx = kx + C$$

$$23, \int [f(x) + g(x)] dx = \int f(x) dx + \int g(x) dx$$

$$24, \int [f(x) - g(x)] dx = \int f(x) dx - \int g(x) dx$$