# JGi SRI BHAGAWAN MAHAVEER JAIN COLLEGE 

Vishweshwarapuram, Bangalore.
Mock Question Paper 2 - January 2020

Subject: Statistics
Max. Marks: 100
Duration: 3.15hrs.

## SECTION-A

I. Answer any TEN of the following questions.

1. What is demography?
2. Define price relative.
3. State the relationship between Laspeyer's, Paasche's and Fisher's price index.
4. Mention a factor causing oscillatory variation.
5. Consider the following p.d.f of a normal variate X ,
$f(x)=\frac{1}{5 \sqrt{2 \pi}} e^{-1 / 2\left(\frac{x-10}{5}\right)^{2}} ;-\infty<x<\infty$. write the variance.
6. Find the variance of $t$-distribution when $n \leq 2$.
7. Define parameter.
8. For the $\chi^{2}$ test, what is the condition for excepted cell frequency?
9. If in a large sample test the test statistic value is 2 . What is your conclusion at $1 \%$ level of significance for a two tailed test?
10. Give an advantage of SQC.
11. When do you suggest for replacement of equipment which deteriorates with age?
12. What do you mean by inventory?

## SECTION-B

II. Answer any TEN of the following questions.
$10 \times 2=20$
13. Mention any 2 uses of vital statistics.
14. Why index numbers are known as economics barometers?
15. Given $\sum p_{1} q=3600$ and $\sum p_{0} q=2850$. Calculate a suitable number.
16. Diagrammatically represent 'Business cycle' with stages.
17. Write the binomial expansion for (i) 5 known terms (ii) 6 known terms.
18. If $X \sim P . D(5)$ then find $P(X=0)$.
19. If variance of a $\chi^{2}$ variate is 18 , then find its mean.
20. A lot contains $6 \%$ defective items. 45 items are chosen from it. Find S.E (p).
21. Define estimate and estimator.
22. Find the average quality level of R -chart when $\sigma^{1}=4$ and $\mathrm{n}=5$.
23. Define (i) Pure strategy (ii) Mixed strategy.
24. If $\mathrm{R}=100$ units/month, $\mathrm{C}_{3}=₹ 250 /$ cycle and $\mathrm{C}_{1}=₹ 20 /$ unit/month. Find EOQ.

## SECTION-C

III. Answer any Eight of the following questions:
$8 \times 5=40$
25. Compute STDR for town X and Y and state which town is healthier.

| Age (in <br> years) | Town X |  | TownY |  | Standard |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Population | Deaths per 1000 | Population | Deaths per 1000 | Population |
| $0-9$ | 13500 | 10 | 8700 | 12 | 35000 |
| $10-29$ | 8900 | 18 | 5500 | 20 | 15000 |
| $30-59$ | 5000 | 20 | 3700 | 24 | 20000 |
| 60 and above | 12000 | 15 | 6900 | 18 | 30000 |

26. What are the steps involved in the construction of index numbers? Explain any three.
27. Calculate weighted arithmetic mean price index number for the following data.

| Items | Expenses | $\mathbf{2 0 1 3}$ | 2015 |
| :---: | :---: | :---: | :---: |
|  |  | Price | Price |
| A | 34.74 | 5.79 | 6 |
| B | 30.00 | 5.00 | 8 |
| C | 6.00 | 6.00 | 9 |
| D | 48.00 | 8.00 | 10 |
| E | 8.00 | 2.00 | 1.50 |
| F | 20.00 | 20.00 | 15 |

28. Calculate 5 yearly moving averages from the following data regarding the number of industries in India.

| Years | 2001 | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of Industries | 25 | 28 | 30 | 34 | 22 | 14 | 14 | 12 | 11 | 15 |

29. Interpolate and extrapolate the production for the years 2010 and 2016.

| Years | 2004 | 2006 | 2008 | 2010 | 2012 | 2014 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Production (in tons) | 100 | 120 | 150 | - | 525 | 780 |

30. On an average, one house out of 500 houses in a locality has a fire during a year. If there a 1000 houses in that locality, find the probability that (i) atmost 3 houses (ii) atleast house will have five during the year.
31. State five properties of normal distribution.
32. The number of defective articles produced by 9 machines in 2 different batches are given below.

|  | Batch I | Batch II |
| :--- | :---: | :---: |
| No. of defectives | 3 | 2 |
| No. of articles | 100 | 500 |

Has the proportion of defective articles increased in the second batch? (use $\alpha=1 \%$ ).
33. A farmer surveyed 4 plots of land of 9 acre each and found the following productions of rice in quintals: X:1269, 1271, 1263, 1265. He had decided that his production should have a S.D. of 2 quintals. Test at $5 \%$ level of significance whether his data is consistent with his assumption.
34. From the past record it is known that the number of defectives in 50 samples of size 500 is 60 . Calculate control limits for d-chart.
35. A firm thinks of replacing a machine that costs $₹ 1,22,000$. The scrap value is only $₹ 2000$. The annual operating cost is ₹ 2200 for the first year, increases by ₹ 3000 in the next two year and ₹ 4000 in the subsequent years. When should the machine be replaced?
36. For the following T.P find an initial B.F.S by NWCR method. Is the solution degenerate.

| Origin | Destination | $\mathbf{D}_{\mathbf{1}}$ | $\mathbf{D}_{\mathbf{2}}$ | $\mathbf{D}_{\mathbf{3}}$ | $\mathbf{D}_{\mathbf{4}}$ | Availability |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{O}_{1}$ | 15 | 14 | 18 | 15 | 300 |
|  | $\mathrm{O}_{2}$ | 17 | 19 | 15 | 10 | 250 |
|  | $\mathrm{O}_{3}$ | 21 | 25 | 14 | 11 | 150 |
| Requirement |  | 100 | 200 | 150 | 250 | 700 |

## SECTION-D

IV. Answer any TWO of the following questions.
37. Calculate crude birth rate, general fertility rate and age-specific fertility rates for the age group.
(10-19), (20-29) (10-24) (25-59) and (30-59) from the following data.

| Age (in years) | Male <br> population | Female <br> population | No. of live <br> births |
| :---: | :---: | :---: | :---: |
| $0-9$ | 6400 | 5197 | 0 |
| $10-19$ | 5430 | 6193 | 196 |
| $20-24$ | 6300 | 7888 | 480 |
| $25-29$ | 2300 | 3444 | 780 |
| $30-39$ | 4700 | 3800 | 211 |
| $40-59$ | 5600 | 4400 | 45 |
| 60 and above | 2800 | 1119 | 0 |

38. (a) For the data given below check whether Marshall-Edgeworth's index number satisfies TRT.

| Items | 2010 |  | 2015 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Price | Value | Price | Value |
| A | 5 | 50 | 8 | 56 |
| B | 4 | 32 | 5 | 40 |
| C | 1 | 10 | 2 | 24 |
| D | 2 | 18 | 4 | 40 |

b) Calculate appropriate index number for the years 2012 and 2014 with regard to base 2010.

| Items | Quantity |  |  | Price |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{2 0 1 0}$ | $\mathbf{2 0 1 2}$ | $\mathbf{2 0 1 4}$ | $\mathbf{2 0 1 1}$ |
| A | 8 | 50 | 49 | 10 |
| B | 10 | 20 | 25 | 12 |
| C | 15 | 12 | 10 | 18 |
| D | 18 | 2 | 5 | 20 |
| E | 17 | 5 | 8 | 22 |

39. The prices of a commodity are given below. Fit a second degree equation to the data and estimate the price for the year 2011.

| Years | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Prices | 150 | 135 | 128 | 140 | 181 | 192 |

40. The table below shows the number of days in a 50 days period during which bike accidents occurred in a city. Fit a poisson distribution and test the goodness of fit.

| No. of accidents | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| No. of days | 21 | 18 | 7 | 3 | 1 |

## SECTION-E

V. Answer any TWO of the following questions.
$2 x 5=10$
41. A supermarket installs neon lamps in its premises. If the lamps have an average life of 1000 burning hours with a variance of 14400 hour $^{2}$;
i) Find the probability of lamps whose average life will be between 925 hours and 1165 hours.
ii) Show that only $10 \%$ of the lamps fail in less than 847 burning hours.
42. The mean breaking strength of cables supplied by a manufacturer is 1500 and variance 8100 . By new techniques it is claimed that the breaking strength of the cables has increased. In order to test this a sample of 64 cables are tested. It is found that the mean breaking strength is 1540 . Can we support the claim at 0.01 level of significance?
43. The following are the marks of 6 students in the preparatory and in P. U. Board examinations.

| Preparatory <br> Marks | P.U. Board <br> Marks |
| :---: | :---: |
| 74 | 86 |
| 83 | 84 |
| 56 | 64 |
| 79 | 72 |
| 30 | 35 |
| 46 | 53 |

Can we conclude that, on an average, students have performed better in Board examination than in the preparatory exam.
44. Solve the following game by maximin-minimax principle. Is the game fair?

Player-B
Player-A $\begin{array}{r}\mathrm{B}_{1} \\ \mathrm{~A}_{1} \\ \mathrm{~A}_{2}\end{array}\left[\begin{array}{cccc}5 & 4 & -7 & \mathrm{~B}_{3} \\ \mathrm{~A}_{3} \\ 6 & 6 & -4 & -2 \\ -8 & 8 & -8 & -2\end{array}\right]$

