

## CHAPTER 8

## BINOMIAL THEOREM

## IMPROVEMENT 2018

1. a) Write the expansion of  $(a+b)^n$ . (1)
- b) Find the coefficient of  $x^5 y^7$  in the expansion of  $(x-2y)^{12}$  (2)
- c) Show that  $9^{n+1} - 8n - 9$  is divisible by 64. (3)

## MARCH 2018

2. a) Which one of the following has its middle terms independent of x? (1)
  - i)  $\left(x + \frac{1}{x}\right)^{10}$
  - ii)  $\left(x + \frac{1}{x}\right)^9$
  - iii)  $\left(x^2 + \frac{1}{x}\right)^9$
  - iv)  $\left(x^2 + \frac{1}{x}\right)^{10}$
- b) Write the expansion of  $\left(x^2 + \frac{3}{x}\right)^4$  (2)
- c) Determine whether the expansion of  $\left(x^2 - \frac{2}{x}\right)^{18}$  a term containing  $x^{10}$ . (3)

## IMPROVEMENT 2017

3. a) The number of terms in the expansion of  $(x+a)^9 = \dots\dots\dots$  (1)
  - i) 9
  - ii) 8
  - b) 10
  - iv) 5
- b) Find  $(a+b)^4 - (a-b)^4$  (2)
- c) Hence evaluate  $(\sqrt{3} + \sqrt{2})^4 - (\sqrt{3} - \sqrt{2})^4$  (2)

## MARCH 2017

4. Consider the expansion of  $\left(x + \frac{1}{x}\right)^{10}$

- a) The number of terms in the expansion is ..... (4)
  - i) 10
  - ii) 9
  - iii) 11
  - iv) 12
- b) Find the term which is independent of x in the above expansion. (3)

## IMPROVEMENT 2016

5. a) Write the expansion of  $(a+b)^4$  (2)
- b) Evaluate:  $(\sqrt{5} + \sqrt{6})^4 + (\sqrt{5} - \sqrt{6})^4$  (2)

## MARCH 2016

6. a) The 8<sup>th</sup> terms is the expansion of  $(\sqrt{2} + \sqrt{3})^7$  is ..... (1)
  - i)  $27\sqrt{2}$
  - ii)  $27\sqrt{3}$
  - iii)  $72\sqrt{2}$
  - iv)  $27\sqrt{3}$
- b) Find the term independent of x in the expansion of  $\left(x + \frac{1}{2x}\right)^{18}; x > 0$  (3)

## IMPROVEMENT 2015

7. a) Number of terms in the expansion of  $\left(x + \frac{1}{x}\right)^{20}$  is ..... (1)
  - i) 19
  - ii) 20
  - iii) 21
  - iv) 22
- b) Consider the expansion of  $\left(3x^2 - \frac{1}{3x}\right)^9$ . Find the coefficient of  $x^6$  and the term independent of x. (4)

## MARCH 2015

8. a) The number of terms in the expansion of

$$\left(x - \frac{1}{x}\right)^{2n} \text{ is } \dots\dots\dots$$

- i)  $n+1$                       ii)  $n$   
 iii)  $2n+1$                 iv)  $2n+2$                       (1)

- b) Find  $a$ , if the 17th term and 18th term of the expansion of  $(2 + \alpha)^{50}$  are equal.                      (3)

**IMPROVEMENT 2014**

9. a) Write the expansion of  $(a + b)^n$ , where  $n$  is any positive integer.                      (1)  
 b) Find the value of ' $\alpha$ ' if the 17<sup>th</sup> term and 18th term in the expansion of  $(2 + a)^{50}$  are equal.                      (4)

**MARCH 2014**

10. a) Write the number of terms in the expansion of  $(a - b)^{2n}$                       (1)  
 b) Find the general term in the expansion of  $(x^2 - yx)^{12}$ ,  $x \neq 0$                       (2)  
 c) Find the coefficient of  $x^6 y^3$  in the expansion of  $(x + 2y)^9$                       (2)

**IMPROVEMENT 2013**

11. a) The number of terms in the expansion of  $\left(\frac{x}{3} + 9y\right)^{10}$  is .....                      (1)  
 b) Find the middle term in the above expansion.                      (3)

**MARCH 2013**

12. a) Find the number of terms in the expansion of  $\left(x - \frac{1}{x}\right)^{14}$                       (1)  
 b) Find the general term in the expansion of

$$\left(x - \frac{1}{x}\right)^{14} \quad (2)$$

- c) Find the term independent of  $x$  in the above expansion.                      (1)

**IMPROVEMENT 2012**

13. Find  $(x + y)^4 - (x - y)^4$ . Hence evaluate:  
 $(\sqrt{5} + \sqrt{6})^4 - (\sqrt{5} - \sqrt{6})^4$                       (4)

**MARCH 2012**

14. a) Find the general term in the expansion of  $\left(\frac{x}{2} - \frac{2}{x}\right)^{10}$                       (2)  
 b) Find the term independent of  $x$  in the above expansion.                      (2)

**IMPROVEMENT 2011**

15. Consider the expansion of  $\left(x^3 + \frac{1}{x}\right)^8$   
 a) Write the general term in the expansion.                      (2)  
 b) Find the coefficient of term containing  $x^8$ .                      (2)

**MARCH 2011**

16. Consider the expansion of  $\left(\frac{x}{9} + 9y\right)^{2n}$   
 i) The number of terms in the above expansion is .....  
 a)  $2n$                       b)  $n+1$   
 c)  $2n+1$                       d)  $2n-1$                       (1)  
 ii) What is its  $(n+1)^{\text{th}}$  term                      (1)  
 iii) If  $n = 5$ , Find its middle term.                      (2)

**IMPROVEMENT 2010**

17. Consider the expansion of  $\left(x^2 - \frac{1}{3x}\right)^9$

- a) Find the coefficient of  $x^9$ . (2)
- b) Find the term which is independent of  $x$ . (2)

**MARCH 2010**

18. i) Find the general term in the expansion of

$$\left(3x^2 - \frac{1}{3x}\right)^9$$

- ii) Find the term independent of  $x$  in the above expansion. (2)

**IMPROVEMENT 2009**

19. a) Write the general term in the expansion of

$$\left(\frac{3x^2}{2} - \frac{1}{3x}\right)^6 \quad (2)$$

- b) Find the term independent of  $x$  in the

expansion of  $\left(\frac{3x^2}{2} - \frac{1}{3x}\right)^6$  (2)

**MARCH 2009**

20. a) Write the general term in the expansion of

$$(x^2 - y)^6. \quad (2)$$

- b) Find the term independent of  $x$  in the

expansion of  $\left(\frac{3}{2}x^2 - \frac{1}{3x}\right)^6$  (2)

**MARCH 2008**

21. a) Using binomial theorem, find the expansion of

$$(1+x)^a \quad (1)$$

- b) Obtain the expansion for  $\left(x^2 + \frac{2}{x}\right)^4$ , where

$$x \neq 0. \quad (2)$$

