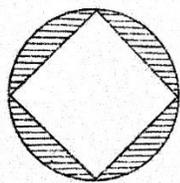


## CHAPTER 8

## APPLICATIONS OF DEFINITE INTEGRALS

## SAY 2018

1. In a circle of radius 2, a square is inscribed as shown in the figure.

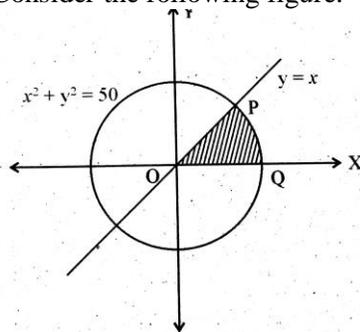


Using integration, find the area of the shaded region. (Area of a square or a triangle may be calculated using any convenient method). (6)

## MARCH 2018

2. Find the area of the region bounded by the curve  $y^2 = x$ ,  $x$  axis and the line  $x = 1$  and  $x = 4$ . (3)

3. Consider the following figure.



- a) Find the point of intersection P of the circle  $x^2 + y^2 = 50$  and the line  $y = x$ . (1)
- b) Find the area of the shaded region. (3)

## SAY 2017

4. a) Area below the curve  $y = -2x + 3$  in the first quadrant.

- a)  $1/4$                       b)  $9/8$   
c)  $2$                               d)  $8$                               (1)

- b) Draw rough sketch of the curves  $x^2 + y^2 = 4$  and  $(x - 2)^2 + y^2 = 4$ . Also find the area between these two curves. (5)

## MARCH 2017

5. a) Area bounded by the curves  $y = \cos x$ ,  $x = \frac{\pi}{2}$ ,  $x = 0$ ,  $y = 0$  is
- a)  $\frac{1}{2}$                               b)  $\frac{2}{\pi}$   
c)  $1$                                 d)  $\frac{\pi}{2}$                               (1)
- b) Find the area between the curves  $y^2 = 4ax$  and  $x^2 = 4ay$ ,  $a > 0$ . (5)

## SAY 2016

6. a) The area bounded by the curve  $y = 2 \cos x$ , the  $x$ -axis from  $x = 0$  to  $x = \frac{\pi}{2}$  is
- i)  $0$                                 ii)  $1$   
iii)  $2$                               iv)  $-1$                               (1)
- b) Find the area of the region bounded by the curves  $y^2 = 4ax$  and  $x^2 = 4ay$ ,  $a > 0$  (5)

OR

7. a) The area bounded by the curve  $y = f(x)$ , above the  $x$ -axis, between  $x = a$  and  $x = b$  is
- i)  $\int_a^b y dy$                       ii)  $\int_a^{f(b)} x dx$   
iii)  $\int_a^b x dy$                     iv)  $\int_a^b y dx$                     (1)
- b) Find the area of the circle  $x^2 + y^2 = 4$  using integration. (5)

**MARCH 2016**

8. a) The area bounded by the curve  $y = f(x)$ , above the x-axis, between  $x = a$  and  $x = b$  is

$$\begin{array}{ll} \text{i) } \int_{f(a)}^b y \, dy & \text{ii) } \int_a^{f(b)} x \, dx \\ \text{iii) } \int_a^b x \, dy & \text{iv) } \int_a^b y \, dx \end{array} \quad (1)$$

- b) Find the area of the circle  $x^2 + y^2 = 4$  using integration. (5)

**SAY 2015**

9. a) Find the area of the region enclosed by the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  (3)
- b) Find the area of the region bounded by the parabolas  $y = x^2$  and  $y^2 = x$  (3)

**MARCH 2015**

10. Consider the functions:  $f(x) = |x| - 1$  and  $g(x) = 1 - |x|$
- a) Sketch their graphs and shade the closed region between them. (2)
- b) Find the area of their shaded region. (2)

**SAY 2014**

11. Consider the ellipse  $\frac{x^2}{9} + \frac{y^2}{4} = 1$  and the

line

$$\frac{x}{3} + \frac{y}{2} = 1$$

- a) Find the points where the line intersects the ellipse? (1)

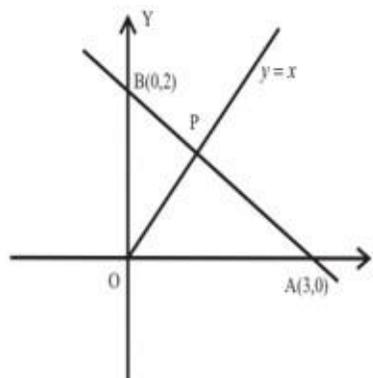
- b) Shade the smaller region bounded by the ellipse and the line. (1)
- c) Find the area of the shaded region. (4)

**MARCH 2014**

12. Consider the following figure:
- a) Find the points of intersection P, of the circle  $x^2 + y^2 = 32$  and the line  $y = x$ . (2)
- b) Express the area of the shaded portion as a sum of two definite integrals. (1)
- c) Find the area of the shaded portion. (3)

**SAY 2013**

13. Using the figure,



- a) Find the equation of AB (1)
- b) Find the point P (2)
- c) Find the area of the shaded region by integration. (3)

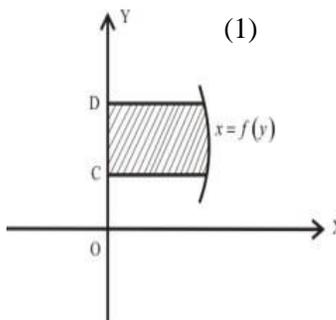
**MARCH 2013**

14. a) Find the point at which the circle  $x^2 + y^2 = 32$  intersects the positive x axis.

- (1)  
 b) Shade the region in the first quadrant enclosed by x axis, the line  $y = x$  and the circle

$$x^2 + y^2 = 32$$

- d) Find the area of the shaded region. (4)



**SAY 2012**

15. i) Area of the shaded portion in the figure is equal to

a)  $\int_d^e f(x) dx$     b)  $\int_e^d f(x) dx$

c)  $\int_d^e f(y) dy$     d)  $\int_e^d f(y) dy$     (1)

- ii) Consider the curves  $y = x^2, x = 0, y = 1, y = 4$

Draw a rough sketch and shade the region bounded by these curves. Find the area of the shaded region. (3)

Find the area of the shaded region. (2)

**MARCH 2012**

16. a) Find the area of the region bounded by the curves  $y^2 = x$  and the lines  $x = 1, y = 4$  and the x axis. (2)  
 b) Using integration, find the area of the triangle with vertices (0,1), (2,2) and (3,1) (4)

**SAY 2011**

17. a) Draw a rough sketch of the curve

$$\frac{x^2}{4} + \frac{y^2}{9} = 1 \quad (1)$$

- b) Find the area bounded by the above curve using integration. (3)

**MARCH 2011**

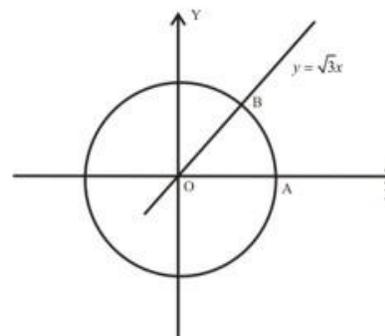
18. a) Find the area enclosed between the curve  $x^2 = 4y$  and the line  $x = 4y - 2$  (2)

- b) Find the area of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$

**SAY 2010**

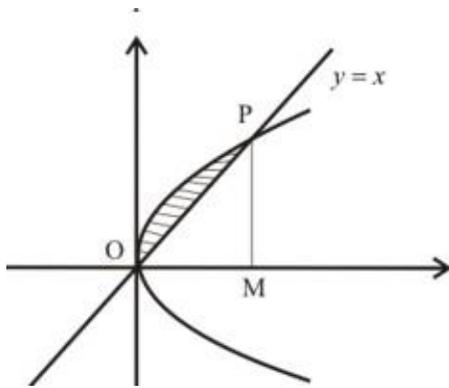
19. Consider the circle  $x^2 + y^2 = 16$  and the straight line  $y = \sqrt{3}x$  as shown in the figure.

- a) Find the point A and B as shown in figure. (1)  
 b) Find the area of the shaded region in the figure using definite integral. (3)



**MARCH 2010**

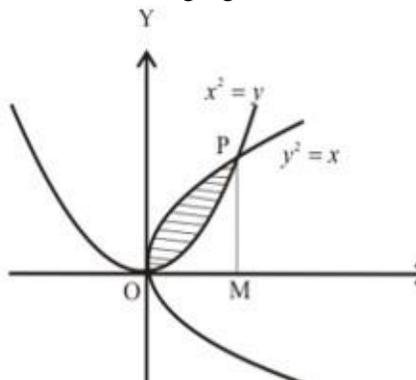
20. Consider the following figure:



- a) Find the points of intersection of the parabola  $y^2 = x$  and the line  $y = x$ . (1)
- b) Using integration, find the area enclosed between the parabola and the line. (3)

OR

Consider the following figure.



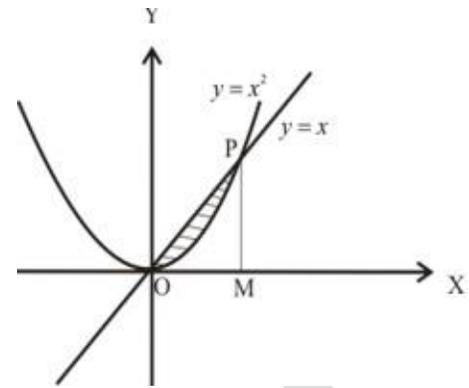
- a) Find the points of intersection of the parabola  $y^2 = x$  and  $x^2 = y$ . (1)
- b) Using integration, find the area enclosed between the parabola and the line. (3)

**SAY 2009**

21. Find the area of the region bounded by the curves  $y^2 = 8x$ ,  $x$  axis and  $x = 1$  and  $x = 3$ . (2)

**MARCH 2009**

22. Consider the figure given below:



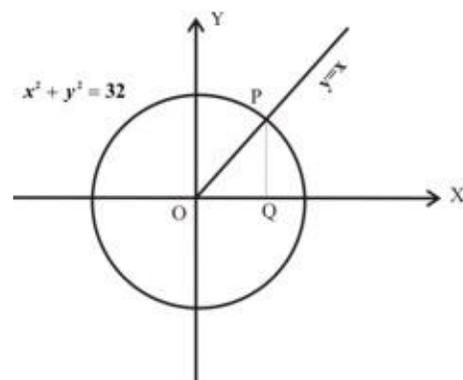
- a) Find the points of intersection P of the curve. (1)
- b) Find the area of the region bounded by the parabola  $y^2 = x$  and the line  $y = x$  in the first quadrant as shown in the figure. (3)

**MARCH 2008**

23. a) Find the points of intersection of the parabola  $y^2 = 8x$  and the line  $y = 2x$ . (1)
- b) Find, using integration, the area enclosed between the line and the parabola. (3)

**MARCH 2007**

24. Consider the following figure:



- a) Find the point of intersection P of the circle  
 $x^2 + y^2 = 32$  and the line  $y = x$  (1)

- b) Find the area of the shaded portion. (3)

OR

25. Using integration, find the area of the region bounded by the triangle whose vertices are  $(-1,1), (0,5), (3,2)$  (4)

### MARCH 2006

26. Area of the ellipse  $\frac{x^2}{4} + \frac{y^2}{9} = 1$  is

- a)  $4\pi$                       b)  $9\pi$   
 c)  $6\pi$                       d)  $36\pi$  (1)

27. Find the area bounded by the curve  $y^2 = 4ax$  and  $x^2 = 4ay$ . (5)

### MARCH 2005

28. Find the area of the region bounded by the ellipse

$$\frac{x^2}{4} + \frac{y^2}{9} = 1 \quad (3)$$

29. The area bounded by the curve  $y = \cos x$  between

$$x = \frac{\pi}{2} \text{ and } x = \frac{3\pi}{2} \text{ is}$$

- a)  $\pi$  sq.units              b) 2 sq.units  
 c) 1 sq.unit                 d)  $\frac{1}{2}$  sq.units (1)

### MARCH 2004

30. The area between  $y = e^x - 1$ , the x axis and  $x = 2$  is

- a)  $e^2 - 1$                       b)  $e^2 - 2$   
 c)  $e^2 - 3$                       d)  $e^2$  (1)

31. Find the area bounded by the curve  $y^2 = 4ax$  and  $x^2 = 4ay$ . (5)

### MARCH 2003

32. The area between the curve  $y^2 = x$  and  $x = 1$  is:

- a)  $\frac{2}{3}$                               b)  $\frac{3}{2}$   
 c) 1                                d) 0 (1)

### SAY 2002

33. The area bounded by the curve  $xy = 1, x = 1, x = 3$  and the x axis is

- a)  $\log 3$                         b) 3  
 c)  $\log 2$                         d) 2 (1)

34. Find the area under the curve  $y = \sin 2x + \cos 2x$  between  $x = 0$  and  $x = \frac{\pi}{4}$ . (2)

35. Find the area under the curve  $y = \sqrt{3x+4}$  between  $x = 0$  and  $x = 4$  (3)

36. Find the area bounded by the curve  $y^2 = 4ax$  and  $x^2 = 4ay$ . (5)

### MARCH 2002

37. Area below the curve  $y = \sqrt{x}$  between  $x = 0$  and  $x = 1$  is

- a)  $\frac{4}{9}$                               b)  $\frac{4}{3}$   
 c)  $\frac{2}{3}$                               d)  $\frac{\sqrt{2}}{3}$  (1)

38. Find the area enclosed between the curves

$$y^2 = 4x \text{ and } y = 2x \quad (5)$$

### MARCH 2001

39. Calculate the area between the curve

$$y = 4\sqrt{x-1}, 1 \leq x \leq 3, \text{ x axis and the line } x = 3. \quad (3)$$

40. Find the area bounded by the curve  $y^2 = 4ax$  and

$$x^2 = 4ay. \quad (5)$$

### MARCH 2000

41. Area of the region bounded by the curve

$$y^2 = 4x, \text{ y axis and the line } y = 3 \text{ is}$$

- a) 2 sq.units      b)  $\frac{9}{4}$  sq.units  
 c)  $6\sqrt{3}$  sq.unit      d) None of these      (1)

42. Prove that the area of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  is

$$\pi ab \text{ sq. units.} \quad (2)$$

*“Look at the sky. We are not alone. The whole universe is friendly to us and conspires only to give the best to those who dream and work”.*

**Dr. APJ**