

CBSE Class 11 PHYSICS
Revision Notes
CHAPTER 15
WAVES

1. **Transverse and longitudinal waves**
2. **Displacement relation in a progressive wave**
3. **The speed of a travelling wave**
4. **The principle of superposition of waves**
5. **Reflection of waves, Beats, Doppler effect**

Angular wave number: It is phase change per unit distance.

i.e. $k = \frac{2}{\pi}$; S.I unit of k is radian per meter.

Relation between velocity, frequency and wavelength is given as :-

Velocity of Transverse wave:-

1. In solid molecules having modulus of rigidity 'n' and density 'ρ' is

$$V = \sqrt{\frac{n}{\rho}}$$

1. In string for mass per unit length 'm' and tension 'T' is $V = \sqrt{\frac{T}{m}}$

Velocity of longitudinal wave:-

(i) in solid $V = \sqrt{\frac{Y}{\rho}}$, Y= young's modulus

(ii) in liquid $V = \sqrt{\frac{K}{\rho}}$, K=bulk modulus

(iii) in gases $V = \sqrt{\frac{K}{\rho}}$, K= bulk modulus

According to Newton's formula: When sound travels in gas then changes take in the medium are isothermal in nature.

$$V = \sqrt{\frac{P}{\rho}}$$

According to Laplace: When sound travels in gas then changes take place in medium are adiabatic in nature.

$$V = \sqrt{\frac{P\gamma}{\rho}} \text{ where } \gamma = \frac{C_p}{C_v}$$

Factors effecting velocity of sound :-

(i) Pressure – No effect

(ii) Density – $v \propto \frac{1}{\sqrt{\rho}}$ or $\frac{V_1}{V_2} = \sqrt{\frac{\rho_2}{\rho_1}}$

Temp- $V \propto \sqrt{T}$ or $\frac{V_1}{V_2} = \sqrt{\frac{T_1}{T_2}}$

(iii) Effect of humidity:- sound travels faster in moist air

(iv) Effect of wind –velocity of sound increasing along the direction

Wave equation if wave is travelling along +ve x-axis

- $Y = A \sin (ax - kt)$, Where, $K = \frac{2\pi}{\lambda}$
- $Y = A \sin 2\pi \left(\frac{t}{T} - \frac{x}{\lambda} \right)$
- $Y = A \sin \frac{2\pi}{\lambda} (vt - x)$

If wave is travelling along –ve x- axis

- $Y = A \sin (ax + kt)$, Where, $K = \frac{2\pi}{\lambda}$
- $Y = A \sin 2\pi \left(\frac{t}{T} + \frac{x}{\lambda} \right)$
- $Y = A \sin \frac{2\pi}{\lambda} (vt + x)$

Phase and phase difference

Phase is the argument of the sine or cosine function representing the wave.

$$\phi = 2\pi \left(\frac{t}{T} - \frac{x}{\lambda} \right)$$

Relation between phase difference ($\Delta\phi$) and time interval is $\Delta\phi = \frac{2\pi}{T} \Delta t$

Relation between phase difference ($\Delta\phi$) and path difference (Δx) is $\Delta\phi = \frac{2\pi}{\lambda} \Delta x$

Equation of stationary wave:-

$$Y_1 = a \sin 2\pi \left(\frac{t}{T} - \frac{x}{\lambda} \right) \text{ (incident wave)}$$

$$Y_1 = \pm a \sin 2\pi \left(\frac{t}{T} + \frac{x}{\lambda} \right) \text{ (reflected wave)}$$

(1) Stationary wave formed

$$Y = Y_1 + Y_2 = \pm 2a \cos \frac{2\pi x}{\lambda} \sin \frac{2\pi t}{T}$$

(2) For (+ve) sign antinodes are at $x = 0, \frac{\lambda}{2}, \lambda, \frac{3\lambda}{2}$

And nodes at $x = \frac{\lambda}{4}, \frac{3\lambda}{4}, \frac{5\lambda}{4}, \dots$

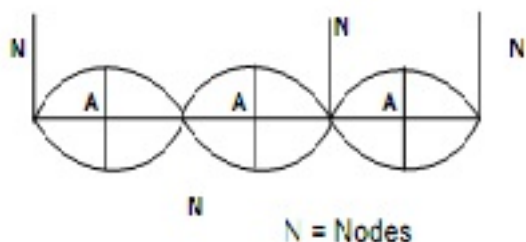
(3) For (-ve) sign antinodes are at $x = \frac{\lambda}{4}, \frac{3\lambda}{4}, \frac{5\lambda}{4}, \dots$

Nodes at $x = 0, \frac{\lambda}{2}, \lambda, \frac{3\lambda}{2}$

(4) Distance between two successive nodes or antinodes are $\frac{\lambda}{2}$ and that between nodes and nearest antinodes is $\frac{\lambda}{4}$

(5) Nodes- point of zero displacement-

Antinodes- point of maximum displacement-



A = Antinodes

Mode of vibration of strings:-

$$1. v = \frac{p}{2L} \sqrt{\frac{T}{m}} \text{ where, } T = \text{Tension}$$

M= mass per unit length

V= frequency, V=velocity of second, P=1, 2, 3,

$$b) \text{ When stretched string vibrates in P loops } \nu P = \frac{P}{2L} \sqrt{\frac{T}{m}} = P\nu$$

$$c) \text{ For string of diameter D and density } \rho \nu = \frac{1}{LD} \sqrt{\frac{T}{\pi P}}$$

$$d) \text{ Law of length } \nu x \propto \frac{1}{L}, \nu L = \text{constant}$$