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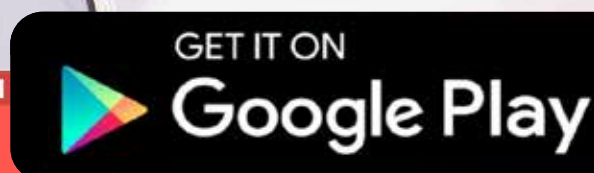
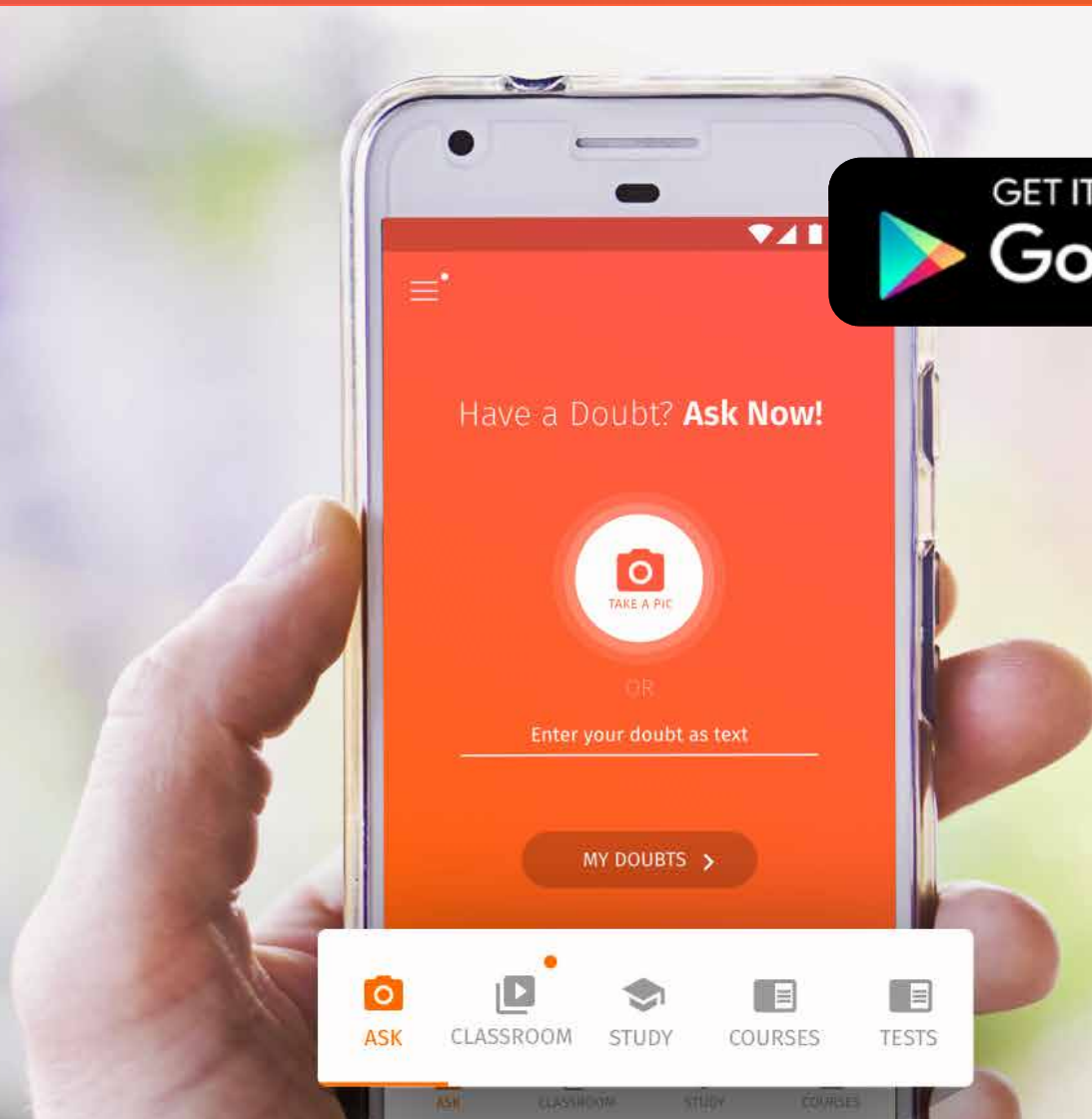
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**Question 1:**

Which of the following expressions are polynomials in one variable and which are not? State reasons for your answer.

(i)  $4x^2 - 3x + 7$

(ii)  $y^2 + \sqrt{2}$

(iii)  $3\sqrt{t} + t\sqrt{2}$

(iv)  $y + \frac{2}{y}$

(v)  $y + 2y^{-1}$

**Solution 1:**

i)  $4x^2 - 3x + 7$

One variable is involved in given polynomial which is 'x'  
Therefore, it is a polynomial in one variable 'x'.

(ii)  $y^2 + \sqrt{2}$

One variable is involved in given polynomial which is 'y'  
Therefore, it is a polynomial in one variable 'y'.

(iii)  $3\sqrt{t} + t\sqrt{2}$

No. It can be observed that the exponent of variable t in term  $3\sqrt{t}$  is  $\frac{1}{2}$ , which is not a whole number. Therefore, this expression is not a polynomial.

(iv)  $y + \frac{2}{y}$

$$= y + 2y^{-1}$$

The power of variable 'y' is -1 which is not a whole number.  
Therefore, it is not a polynomial in one variable

No. It can be observed that the exponent of variable y in term  $\frac{2}{y}$  is -1, which is not a whole number. Therefore, this expression is not a polynomial.

(v)  $x^{10} + y^3 + t^{50}$

In the given expression there are 3 variables which are 'x, y, t' involved.

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Therefore, it is not a polynomial in one variable.

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**Question 2:**

Write the coefficients of  $x^2$  in each of the following:

(i)  $2 + x^2 + x$

(ii)  $2 - x^2 + x^3$

(iii)  $\frac{\pi}{2}x^2 + x$

(iv)  $\sqrt{2}x - 1$

**Solution 2:**

(i)  $2 + x^2 + x^3$   
 $= 2 + 1(x^2) + x$

The coefficient of  $x^2$  is 1.

(ii)  $2 - x^2 + x^3$   
 $= 2 - 1(x^2) + x$

The coefficient of  $x^2$  is  $-1$ .

(iii)  $\frac{\pi}{2}x^2 + x$

The coefficient  $x^2$  of is  $\frac{\pi}{2}$ .

(iv)  $\sqrt{2}x - 1 = 0x^2 + \sqrt{2}x - 1$

The coefficient of  $x^2$  is 0.

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**Question 3:**

Give one example each of a binomial of degree 35, and of a monomial of degree 100.

**Solution 3 :**

Binomial of degree 35 means a polynomial is having

1. Two terms
2. Highest degree is 35

Example:  $x^{35} + x^{34}$

Monomial of degree 100 means a polynomial is having

1. One term
2. Highest degree is 100

Example :  $x^{100}$ .

#### Question 4:

Write the degree of each of the following polynomials:

(i)  $5x^3 + 4x^2 + 7x$

(ii)  $4 - y^2$

(iii)  $5t - \sqrt{7}$

(iv) 3

#### Solution 4:

Degree of a polynomial is the highest power of the variable in the polynomial.

(i)  $5x^3 + 4x^2 + 7x$

Highest power of variable 'x' is 3. Therefore, the degree of this polynomial is 3

(ii)  $4 - y^2$

Highest power of variable 'y' is 2. Therefore, the degree of this polynomial is 2.

(iii)  $5t - \sqrt{7}$

Highest power of variable 't' is 1. Therefore, the degree of this polynomial is 1.

(iv) 3

This is a constant polynomial. Degree of a constant polynomial is always 0.

**Question 5:** Classify the following as linear, quadratic and cubic polynomial:

(i)  $x^2 + x$

(ii)  $x - x^3$

(iii)  $y + y^2 + 4$

- (iv)  $1+x$
- (v)  $3t$
- (vi)  $r^2$
- (vii)  $7x^2 - 7x^3$

**Solution 5:**

Linear polynomial – whose variable power is ‘1’

Quadratic polynomial - whose variable highest power is ‘2’

Cubic polynomial- whose variable highest power is ‘3’

- (i)  $x^2 + x$  is a quadratic polynomial as its highest degree is 2.
- (ii)  $x - x^3$  is a cubic polynomial as its highest degree is 3.
- (iii)  $y + y^2 + 4$  is a quadratic polynomial as its highest degree is 2.
- (iv)  $1 + x$  is a linear polynomial as its degree is 1.
- (v)  $3t$  is a linear polynomial as its degree is 1.
- (vi)  $r^2$  is a quadratic polynomial as its degree is 2.
- (vii)  $7x^2 - 7x^3$  is a cubic polynomial as highest its degree is 3.

## Exercise 2.2

**Question 1:**

Find the value of the polynomial at  $5x - 4x^2 + 3$  at

- (i)  $x = 0$
- (ii)  $x = -1$
- (iii)  $x = 2$

**Solution 1:**

$$(i) \quad p(x) = 5x - 4x^2 + 3$$

$$p(0) = 5(0) - 4(0)^2 + 3 = 3$$

$$(ii) \quad p(x) = 5x - 4x^2 + 3$$

$$\begin{aligned} p(-1) &= 5(-1) - 4(-1)^2 + 3 \\ &= -5 - 4(1) + 3 = -6 \end{aligned}$$

$$(iii) \quad p(x) = 5x - 4x^2 + 3$$

$$p(2) = 5(2) - 4(2)^2 + 3 = 10 - 16 + 3 = -3$$

### Question 2:

Find  $p(0)$ ,  $p(1)$  and  $p(2)$  for each of the following polynomials:

- (i)  $p(y) = y^2 - y + 1$
- (ii)  $p(t) = 2 + t + 2t^2 - t^3$
- (iii)  $p(x) = x^3$
- (iv)  $p(x) = (x - 1)(x + 1)$

### Solution 2:

(i)  $p(y) = y^2 - y + 1$

- $p(0) = (0)^2 - (0) + 1 = 1$
- $p(1) = (1)^2 - (1) + 1 = 1 - 1 + 1 = 1$
- $p(2) = (2)^2 - (2) + 1 = 4 - 2 + 1 = 3$

(ii)  $p(t) = 2 + t + 2t^2 - t^3$

- $p(0) = 2 + 0 + 2(0)^2 - (0)^3 = 2$
- $p(1) = 2 + (1) + 2(1)^2 - (1)^3 = 2 + 1 + 2 - 1 = 4$
- $p(2) = 2 + 2 + 2(2)^2 - (2)^3$   
 $= 2 + 2 + 8 - 8 = 4$

(iii)  $p(x) = x^3$

- $p(0) = (0)^3 = 0$
- $p(1) = (1)^3 = 1$
- $p(2) = (2)^3 = 8$

(v)  $p(x) = (x - 1)(x + 1)$

- $p(0) = (0 - 1)(0 + 1) = (-1)(1) = -1$
- $p(1) = (1 - 1)(1 + 1) = 0(2) = 0$
- $p(2) = (2 - 1)(2 + 1) = 1(3) = 3$

### Question 3:

Verify whether the following are zeroes of the polynomial, indicated against them.

(i)  $p(x) = 3x + 1, x = -\frac{1}{3}$

(ii)  $p(x) = 5x - \pi, x = \frac{4}{5}$

(iii)  $p(x) = x^2 - 1, x = 1, -1$

(iv)  $p(x) = (x+1)(x-2), x = -1, 2$

(v)  $p(x) = x^2, x = 0$

(vi)  $p(x) = lx + m, x = -\frac{m}{l}$

(vii)  $p(x) = 3x^2 - 1, x = -\frac{1}{\sqrt{3}}, \frac{2}{\sqrt{3}}$

(viii)  $p(x) = 2x + 1, x = \frac{1}{2}$

### Solution 3:

(i) If  $x = -\frac{1}{3}$  is a zero of given polynomial  $p(x) = 3x + 1$ , then  $p\left(-\frac{1}{3}\right)$  should be 0.

$$\text{Here, } p\left(-\frac{1}{3}\right) = 3\left(-\frac{1}{3}\right) + 1 = -1 + 1 = 0$$

Therefore,  $-\frac{1}{3}$  is a zero of the given polynomial.

(ii) If  $x = \frac{4}{5}$  is a zero of polynomial  $p(x) = 5x - \pi$ , then  $p\left(\frac{4}{5}\right)$  should be 0.

$$\text{Here, } p\left(\frac{4}{5}\right) = 5\left(\frac{4}{5}\right) - \pi = 4 - \pi$$

$$\text{As } p\left(\frac{4}{5}\right) \neq 0$$

Therefore,  $x = \frac{4}{5}$  is not a zero of the given polynomial.

(iii) If  $x = 1$  and  $x = -1$  are zeroes of polynomial  $p(x) = x^2 - 1$ , then  $p(1)$  and  $p(-1)$  should be 0.

Here,  $p(1) = (1)^2 - 1 = 0$ , and

$$p(-1) = (-1)^2 - 1 = 0$$

Hence,  $x = 1$  and  $-1$  are zeroes of the given polynomial.

(iv) If  $x = -1$  and  $x = 2$  are zeroes of polynomial  $p(x) = (x + 1)(x - 2)$ , then  $p(-1)$  and  $p(2)$  should be 0.

Here,  $p(-1) = (-1 + 1)(-1 - 2) = 0(-3) = 0$ , and

$$p(2) = (2 + 1)(2 - 2) = 3(0) = 0$$

Therefore,  $x = -1$  and  $x = 2$  are zeroes of the given polynomial.

(v) If  $x = 0$  is a zero of polynomial  $p(x) = x^2$ , then  $p(0)$  should be zero.

$$\text{Here, } p(0) = (0)^2 = 0$$

Hence,  $x = 0$  is a zero of the given polynomial.

(vi) If  $p\left(\frac{-m}{l}\right)$  is a zero of polynomial  $p(x) = lx + m$ , then  $p\left(\frac{-m}{l}\right)$  should be 0.

$$\text{Here, } p\left(\frac{-m}{l}\right) = l\left(\frac{-m}{l}\right) + m = -m + m = 0$$

Therefore,  $x = \frac{-m}{l}$  is a zero of the given polynomial.

(vii) If  $x = \frac{-1}{\sqrt{3}}$  and  $x = \frac{2}{\sqrt{3}}$  are zeroes of polynomial  $p(x) = 3x^2 - 1$ , then

$$p\left(\frac{-1}{\sqrt{3}}\right) \text{ and } p\left(\frac{2}{\sqrt{3}}\right) \text{ should be 0.}$$

Here,  $p\left(\frac{-1}{\sqrt{3}}\right) = 3\left(\frac{-1}{\sqrt{3}}\right)^2 - 1 = 3\left(\frac{1}{3}\right) - 1 = 1 - 1 = 0$ , and

$$p\left(\frac{2}{\sqrt{3}}\right) = 3\left(\frac{2}{\sqrt{3}}\right)^2 - 1 = 3\left(\frac{4}{3}\right) - 1 = 4 - 1 = 3$$

Hence,  $x = \frac{-1}{\sqrt{3}}$  is a zero of the given polynomial.

However,  $x = \frac{2}{\sqrt{3}}$  is not a zero of the given polynomial.

(viii) If  $x = \frac{1}{2}$  is a zero of polynomial  $p(x) = 2x + 1$ , then  $p\left(\frac{1}{2}\right)$  should be 0.

Here,  $p\left(\frac{1}{2}\right) = 2\left(\frac{1}{2}\right) + 1 = 1 + 1 = 2$

As  $p\left(\frac{1}{2}\right) \neq 0$ ,

Therefore,  $x = \frac{1}{2}$  is not a zero of the given polynomial.

#### Question 4:

Find the zero of the polynomial in each of the following cases:

(i)  $p(x) = x + 5$

(ii)  $p(x) = x - 5$

(iii)  $p(x) = 2x + 5$

(iv)  $p(x) = 3x - 2$

(v)  $p(x) = 3x$

(vi)  $p(x) = ax, a \neq 0$

(vii)  $p(x) = cx + d, c \neq 0, c, d$  are real numbers.

#### Solution 4:

Zero of a polynomial is that value of the variable at which the value of the polynomial is obtained as 0.

(i)  $p(x) = x + 5$

Let  $p(x) = 0$

$$x + 5 = 0$$

$$x = -5$$

Therefore, for  $x = -5$ , the value of the polynomial is 0 and hence,  $x = -5$  is a zero of the given polynomial.

(ii)  $p(x) = x - 5$

Let  $p(x) = 0$

$$x - 5 = 0$$

$$x = 5$$

Therefore, for  $x = 5$ , the value of the polynomial is 0 and hence,  $x = 5$  is a zero of the given polynomial.

(iii)  $p(x) = 2x + 5$

Let  $p(x) = 0$

$$2x + 5 = 0$$

$$2x = -5$$

$$x = -\frac{5}{2}$$

Therefore, for  $x = -\frac{5}{2}$ , the value of the polynomial is 0 and hence,  $x = -\frac{5}{2}$  is a zero of the given polynomial.

(iv)  $p(x) = 3x - 2$

$p(x) = 0$

$$3x - 2 = 0$$

Therefore, for  $x = \frac{2}{3}$ , the value of the polynomial is 0 and hence,  $x = \frac{2}{3}$  is a zero of the given polynomial.

(v)  $p(x) = 3x$

Let  $p(x) = 0$

$3x = 0$

$x = 0$

Therefore, for  $x = 0$ , the value of the polynomial is 0 and hence,  $x = 0$  is a zero of the given polynomial.

(vi)  $p(x) = ax$

Let  $p(x) = 0$

$ax = 0$

$x = 0$

Therefore, for  $x = 0$ , the value of the polynomial is 0 and hence,  $x = 0$  is a zero of the given polynomial.

(vii)  $p(x) = cx + d$

Let  $p(x) = 0$

$cx + d = 0$

$x = \frac{-d}{c}$

Therefore, for  $x = \frac{-d}{c}$ , the value of the polynomial is 0 and hence,  $x = \frac{-d}{c}$  is a zero of the given polynomial.

## Exercise 2.3

### Question 1:

Find the remainder when  $x^3 + 3x^2 + 3x + 1$  is divided by

(i)  $x + 1$

(ii)  $x - \frac{1}{2}$

(iii)  $x$

(iv)  $x + \pi$

(v)  $5 + 2x$

### Solution 1:

(i)  $x^3 + 3x^2 + 3x + 1 \div x + 1$

By long division, we get

$$\begin{array}{r} x^2 + 2x + 1 \\ x+1 \overline{) x^3 + 3x^2 + 3x + 1} \\ \underline{x^3 + x^2} \phantom{+ 1} \\ 2x^2 + 3x + 1 \\ \underline{2x^2 + 2x} \phantom{+ 1} \\ x + 1 \\ \underline{x + 1} \\ 0 \end{array}$$

Therefore, the remainder is 0.

(ii)  $x^3 + 3x^2 + 3x + 1 \div x - \frac{1}{2}$

By long division,

$$\begin{array}{r}
 x^2 + \frac{7}{2}x + \frac{19}{4} \\
 x - \frac{1}{2} \overline{) x^3 + 3x^2 + 3x + 1} \\
 \underline{x^3 - \frac{x^2}{2}} \phantom{+ 1} \\
 \phantom{x^3} + \frac{7}{2}x^2 + 3x + 1 \\
 \underline{\phantom{x^3} \frac{7}{2}x^2 - \frac{7}{4}x} \phantom{+ 1} \\
 \phantom{x^3} \phantom{\frac{7}{2}x^2} + \frac{19}{4}x + 1 \\
 \underline{\phantom{x^3} \phantom{\frac{7}{2}x^2} \frac{19}{4}x - \frac{19}{8}} \\
 \phantom{x^3} \phantom{\frac{7}{2}x^2} \phantom{\frac{19}{4}x} + \frac{27}{8} \\
 \underline{\phantom{x^3} \phantom{\frac{7}{2}x^2} \phantom{\frac{19}{4}x} \frac{27}{8}} \\
 \phantom{x^3} \phantom{\frac{7}{2}x^2} \phantom{\frac{19}{4}x} \phantom{\frac{27}{8}} 0
 \end{array}$$

Therefore, the remainder is  $\frac{27}{8}$ .

(iii)  $x^3 + 3x^2 + 3x + 1 \div x$

By long division,

$$\begin{array}{r}
 x^2 + 3x + 3 \\
 x \overline{) x^3 + 3x^2 + 3x + 1} \\
 \underline{x^3} \phantom{+ 3x^2} \phantom{+ 3x} \phantom{+ 1} \\
 \phantom{x^3} 3x^2 + 3x + 1 \\
 \underline{3x^2} \phantom{+ 3x} \phantom{+ 1} \\
 \phantom{x^3} \phantom{3x^2} 3x + 1 \\
 \underline{3x} \phantom{+ 1} \\
 \phantom{x^3} \phantom{3x^2} \phantom{3x} 1 \\
 \underline{1} \\
 \phantom{x^3} \phantom{3x^2} \phantom{3x} \phantom{1} 0
 \end{array}$$

Therefore, the remainder is 1.

(iv)  $x^3 + 3x^2 + 3x + 1 \div x + \pi$

By long division, we get

$$\begin{array}{r}
 x^2 + (3 - \pi)x + (3 - 3\pi + \pi^2) \\
 x + \pi \overline{) x^3 + 3x^2 + 3x + 1} \\
 \underline{x^3 + \pi x^2} \phantom{+ 3x + 1} \\
 (3 - \pi)x^2 + 3x + 1 \\
 \underline{(3 - \pi)x^2 + (3 - \pi)\pi x} \phantom{+ 1} \\
 [3 - 3\pi + \pi^2]x + 1 \\
 \underline{[3 - 3\pi + \pi^2]x + (3 - 3\pi + \pi^2)\pi} \\
 [1 - 3\pi + 3\pi^2 - \pi^3]
 \end{array}$$

Therefore, the remainder is  $-\pi^3 + 3\pi^2 - 3\pi + 1$ .

(v)  $5 + 2x$

By long division, we get

$$\begin{array}{r}
 \frac{x^2}{2} + \frac{x}{4} + \frac{7}{8} \\
 2x+5 \overline{) x^3 + 3x^2 + 3x + 1} \\
 \underline{x^3 + \frac{5}{2}x^2} \phantom{+ 3x + 1} \\
 - \phantom{x^3} - \\
 \frac{x^2}{2} + 3x + 1 \\
 \underline{\frac{x^2}{2} + \frac{5x}{4}} \\
 - \phantom{x^2} - \\
 \frac{7x}{4} + 1 \\
 \underline{\frac{7x}{4} + \frac{35}{8}} \\
 - \phantom{x^2} - \\
 \frac{27}{8}
 \end{array}$$

Therefore, the remainder is  $-\frac{27}{8}$ .

### Question 2:

Find the remainder when  $x^3 - ax^2 + 6x - a$  is divided by  $x - a$ .

### Solution 2:

$$x^3 - ax^2 + 6x - a \div x - a$$

By long division,

$$\begin{array}{r}
 x^2 + 6 \\
 x-a \overline{) x^3 - ax^2 + 6x - a} \\
 \underline{x^3 - ax^2} \phantom{+ 6x - a} \\
 - \phantom{x^3} + \\
 6x - a \\
 \underline{6x - 6a} \\
 - \phantom{x^3} + \\
 5a
 \end{array}$$



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