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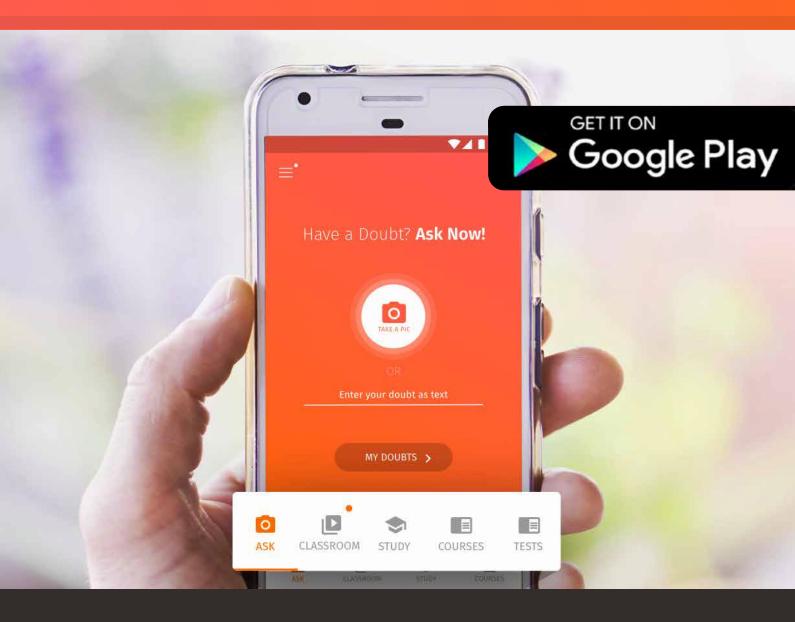
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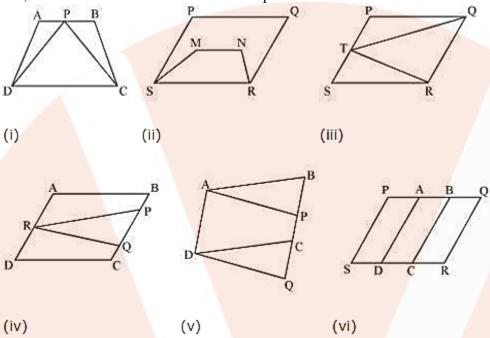


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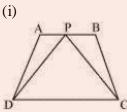


Question 1:

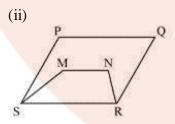
Which of the following figures lie on the same base and between the same parallels. In such a case, write the common base and the two parallels.



Solution 1:



Yes.It can be observed that trapezium ABCD and triangle PCD have a common base CD and these are lying between the same parallel lines AB and CD.



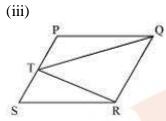
No. It can be observed that parallelogram PQRS and trapezium MNRS have a common base RS. However, their vertices, (i.e., opposite to the common base) P, Q of parallelogram and M, N of trapezium, are not lying on the same line.

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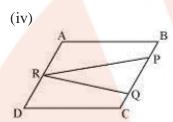
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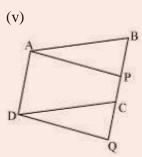




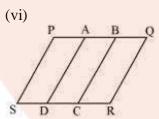
Yes. It can be observed that parallelogram PQRS and triangle TQR have a common base QR and they are lying between the same parallel lines PS and QR.



No. It can be observed that parallelogram ABCD and triangle PQR are lying between same parallel lines AD and BC. However, these do not have any common base.



Yes. It can be observed that parallelogram ABCD and parallelogram APQD have a common base AD and these are lying between the same parallel lines AD and BQ.



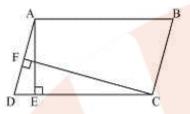
No. It can be observed that parallelogram PBCS and PQRS are lying on the same base PS. However, these do not lie between the same parallel lines.

Exercise (9.2)



Question 1:

In the given figure, ABCD is parallelogram, AE \perp DC and CF \perp AD. If AB = 16 cm, AE = 8 cm and CF = 10 cm, find AD.



Solution 1:

In parallelogram ABCD, CD = AB = 16 cm

[Opposite sides of a parallelogram are equal]

We know that

Area of a parallelogram = Base \times Corresponding altitude

Area of parallelogram $ABCD = CD \times AE = AD \times CF$

 $16 \text{ cm} \times 8 \text{ cm} = \text{AD} \times 10 \text{ cm}$

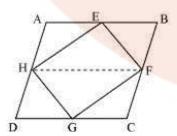
$$AD = \frac{16 \times 8}{10} \text{ cm} = 12.8 \text{ cm}$$

Thus, the length of AD is 12.8 cm.

Question 2:

If E, F, G and H are respectively the mid-points of the sides of a parallelogram ABCD show that $ar(EFGH) = \frac{1}{2}ar(ABCD)$

Solution 2:



Let us join HF.



In parallelogram ABCD,

AD = BC and AD || BC (Opposite sides of a parallelogram are equal and parallel)

AB = CD (Opposite sides of a parallelogram are equal)

$$\Rightarrow \frac{1}{2}AD = \frac{1}{2}BC$$
 and $AH \parallel BF$

 \Rightarrow AH = BF and AH || BF (: H and F are the mid-points of AD and BC)

Therefore, ABFH is a parallelogram.

Since Δ HEF and parallelogram ABFH are on the same base HF and between the same parallel lines AB and HF,

∴ Area (
$$\triangle$$
HEF) = $\frac{1}{2}$ Area (ABFH) ... (1)

Similarly, it can be proved that

Area (
$$\Delta$$
HGF) = $\frac{1}{2}$ Area (HDCF) ... (2)

On adding Equations (1) and (2), we obtain

Area (
$$\Delta$$
HEF) + Area (Δ HGF) = $\frac{1}{2}$ Area (ABFH) + $\frac{1}{2}$ Area (HDCF)

$$= \frac{1}{2} [Area (ABFH) + Area (HDCF)]$$

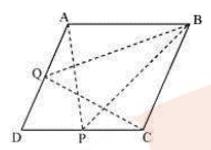
$$\Rightarrow$$
 Area (EFGH) = $\frac{1}{2}$ Area (ABCD)

Question 3:

P and Q are any two points lying on the sides DC and AD respectively of a parallelogram ABCD. Show that ar (APB) = ar (BQC).

Solution 3:





It can be observed that ΔBQC and parallelogram ABCD lie on the same base BC and these are between the same parallel lines AD and BC.

∴ Area (
$$\triangle$$
BQC) = $\frac{1}{2}$ Area (ABCD) ... (1)

Similarly, \triangle APB and parallelogram ABCD lie on the same base AB and between the same parallel lines AB and DC.

∴ Area (
$$\triangle$$
APB) = $\frac{1}{2}$ Area (ABCD) ... (2)

From Equations (1) and (2), we obtain

Area (ΔBQC) = Area (ΔAPB)

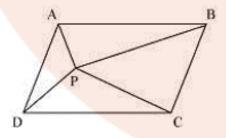
Question 4:

In the given figure, P is a point in the interior of a parallelogram ABCD. Show that

(i) ar (APB) + ar (PCD) =
$$\frac{1}{2}$$
 ar (ABCD)

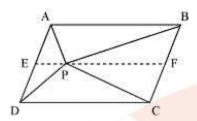
(ii)
$$ar(APD) + ar(PBC) = ar(APB) + ar(PCD)$$

[Hint: Through. P, draw a line parallel to AB]



Solution 4:





(i) Let us draw a line segment EF, passing through point P and parallel to line segment AB. In parallelogram ABCD,

ABCD is a parallelogram.

$$\Rightarrow$$
 AE || BF ... (2)

From Equations (1) and (2), we obtain

Therefore, quadrilateral ABFE is a parallelogram.

It can be observed that $\triangle APB$ and parallelogram ABFE are lying on the same base AB and between the same parallel lines AB and EF.

∴ Area (
$$\triangle APB$$
) = $\frac{1}{2}$ Area ($\triangle ABFE$) ... (3)

Similarly, for ΔPCD and parallelogram EFCD,

Area (
$$\triangle PCD$$
) = $\frac{1}{2}$ Area (EFCD) ... (4)

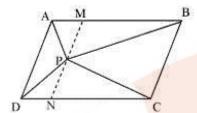
Adding Equations (3) and (4), we obtain

Area (
$$\triangle APB$$
) + Area ($\triangle PCD$) = $\frac{1}{2}$ [Area (ABFE) + Area (EFCD)]

Area (
$$\triangle APB$$
) + Area ($\triangle PCD$) = $\frac{1}{2}$ Area (ABCD) ... (5)



(ii)



Let us draw a line segment MN, passing through point P and parallel to line segment AD. In parallelogram ABCD,

MN || AD (By construction)

... (6)

ABCD is a parallelogram.

∴ AB || DC (Opposite sides of a parallelogram)

 \Rightarrow AM || DN ... (7)

From Equations (6) and (7), we obtain

 $MN \parallel AD$ and $AM \parallel DN$

Therefore, quadrilateral AMND is a parallelogram.

It can be observed that $\triangle APD$ and parallelogram AMND are lying on the same base AD and between the same parallel lines AD and MN.

∴ Area (
$$\triangle$$
APD) = $\frac{1}{2}$ Area (AMND) ... (8)

Similarly, for ΔPCB and parallelogram MNCB,

Area (
$$\triangle PCB$$
) = $\frac{1}{2}$ Area (MNCB) ... (9)

Adding Equations (8) and (9), we obtain

Area (
$$\triangle$$
APD) + Area (\triangle PCB) = $\frac{1}{2}$ [Area (AMND) + Area (MNCB)]

Area (
$$\triangle$$
APD) + Area (\triangle PCB) = $\frac{1}{2}$ Area (ABCD) ... (10)



On comparing Equations (5) and (10), we obtain

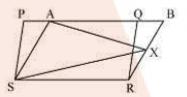
Area (\triangle APD) + Area (\triangle PBC) = Area (\triangle APB) + Area (\triangle PCD)

Question 5:

In the given figure, PQRS and ABRS are parallelograms and X is any point on side BR. Show that

(i)
$$ar(PQRS) = ar(ABRS)$$

(ii) ar
$$(\Delta PXS) = \frac{1}{2}$$
 ar $(PQRS)$



Solution 5:

(i) It can be observed that parallelogram PQRS and ABRS lie on the same base SR and also, these lie in between the same parallel lines SR and PB.

$$\therefore$$
 Area (PQRS) = Area (ABRS) ... (1)

(ii) Consider ΔAXS and parallelogram ABRS.

As these lie on the same base and are between the same parallel lines AS and BR,

∴ Area (
$$\triangle AXS$$
) = $\frac{1}{2}$ Area (ABRS) ... (2)

From Equations (1) and (2), we obtain

Area (
$$\triangle AXS$$
) = $\frac{1}{2}$ Area (PQRS)

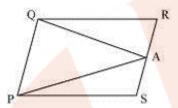
Question 6:

A farmer was having a field in the form of a parallelogram PQRS. She took any point A on RS and joined it to points P and Q. In how many parts the field is divided? What are the shapes of



these parts? The farmer wants to sow wheat and pulses in equal portions of the field separately. How should she do it?

Solution 6:



From the figure, it can be observed that point A divides the field into three parts.

These parts are triangular in shape – Δ PSA, Δ PAQ, and Δ QRA

Area of $\triangle PSA$ + Area of $\triangle PAQ$ + Area of $\triangle QRA$ = Area of parallelogram PQRS ... (1)

We know that if a parallelogram and a triangle are on the same base and between the same parallels, then the area of the triangle is half the area of the parallelogram.

∴ Area (
$$\triangle PAQ$$
) = $\frac{1}{2}$ Area (PQRS) ... (2)

From Equations (1) and (2), we obtain

Area (
$$\triangle PSA$$
) + Area ($\triangle QRA$) = $\frac{1}{2}$ Area (PQRS) ... (3)

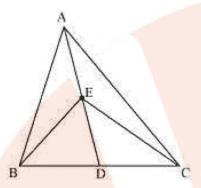
Clearly, it can be observed that the farmer must sow wheat in triangular part PAQ and pulses in other two triangular parts PSA and QRA or wheat in triangular parts PSA and QRA and pulses in triangular parts PAQ.

Exercise (9.3)



Question 1:

In the given figure, E is any point on median AD of a \triangle ABC. Show that ar (ABE) = ar (ACE)



Solution 1:

AD is the median of \triangle ABC. Therefore, it will divide \triangle ABC into two triangles of equal areas.

∴ Area (\triangle ABD) = Area (\triangle ACD) ... (1)

ED is the median of \triangle EBC.

∴ Area (\triangle EBD) = Area (\triangle ECD) ... (2)

On subtracting Equation (2) from Equation (1), we obtain

Area (\triangle ABD) – Area (EBD) = Area (\triangle ACD) – Area (\triangle ECD)

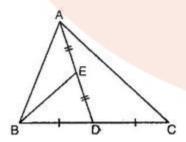
Area (\triangle ABE) = Area (\triangle ACE)

Question 2: In a triangle ABC, E is the mid-point of median AD.

Show that $ar(\Delta BED) = 1/4 ar(\Delta ABC)$.

Solution 2:

Given: A \triangle ABC, AD is the median and E is the mid-point of median AD.





To prove: $ar(\Delta BED) = 1/4 ar(\Delta ABC)$

Proof : In \triangle ABC, AD is the median.

$$\therefore$$
 ar (\triangle ABD) = ar (\triangle ADC)

[: Median divides a Δ into two Δ s of equal area]

$$ar(\Delta ABD) = \frac{1}{2} ar(ABC)$$
(i)

In \triangle ABD, BE is the median.

$$ar (\Delta BED) = ar (\Delta BAE)$$

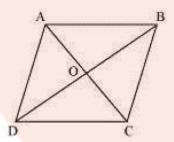
$$\therefore \operatorname{ar}(\Delta \operatorname{BED}) = \frac{1}{2} \operatorname{ar}(\Delta \operatorname{ABD})$$

= ar (
$$\triangle$$
BED) = $\frac{1}{2} \left[\frac{1}{2} \operatorname{ar} \left(\triangle ABC \right) \right] = \frac{1}{2} \operatorname{ar} \left(\triangle ABC \right)$

Question 3:

Show that the diagonals of a parallelogram divide it into four triangles of equal area.

Solution 3:



We know that diagonals of parallelogram bisect each other.

Therefore, O is the mid-point of AC and BD.

BO is the median in \triangle ABC. Therefore, it will divide it into two triangles of equal areas.

∴ Area (
$$\triangle$$
AOB) = Area (\triangle BOC) ... (1)

In $\triangle BCD$, CO is the median.



∴ Area (
$$\triangle BOC$$
) = Area ($\triangle COD$) ... (2)

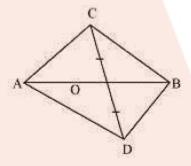
Similarly, Area (
$$\triangle COD$$
) = Area ($\triangle AOD$) ... (3)

Area (
$$\triangle AOB$$
) = Area ($\triangle BOC$) = Area ($\triangle COD$) = Area ($\triangle AOD$)

Therefore, it is evident that the diagonals of a parallelogram divide it into four triangles of equal area.

Question 4:

In the given figure, ABC and ABD are two triangles on the same base AB. If line-segment CD is bisected by AB at O, show that ar (ABC) = ar (ABD).



Solution 4:

Consider $\triangle ACD$.

Line-segment CD is bisected by AB at O. Therefore, AO is the median of \triangle ACD.

∴ Area (
$$\triangle$$
ACO) = Area (\triangle ADO) ... (1)

Considering $\triangle BCD$, BO is the median.

∴ Area (
$$\triangle$$
BCO) = Area (\triangle BDO) ... (2)

Adding Equations (1) and (2), we obtain



Area (
$$\triangle$$
ACO) + Area (\triangle BCO) = Area (\triangle ADO) + Area (\triangle BDO)
 \Rightarrow Area (\triangle ABC) = Area (\triangle ABD)

Question 5:

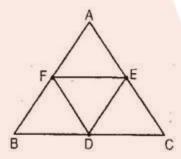
- D, E and F are respectively the mid-points of the sides BC, CA and AB of a ΔABC. Show that:
- (i) BDEF is a parallelogram.

(ii) ar (DEF) =
$$\frac{1}{4}$$
ar (ABC)

(iii) ar (BDEF) =
$$\frac{1}{2}$$
ar (ABC)

Solution 5:

- (i) F is the mid-point of AB and E is the mid-point of AC.
- ∴ FE | BC and FE $=\frac{1}{2}$ BD



Line joining the mid-points of two sides of a triangle is parallel to the third and half of It

∴FE BD BD is the part of BC

And
$$FE = BD$$

Also, D is the mid-point of BC.

$$\therefore BD = \frac{1}{2}BC$$

And $FE \parallel BC$ and FE = BD



Again E is the mid-point of AC and D is the mid-point of BC.

$$\therefore$$
 DE || AB and DE = $\frac{1}{2}$ AB

DE AB BF is the part of AB

And DE = BF

Again F is the mid-point of AB.

$$\therefore BF = \frac{1}{2}AB$$

But DE =
$$\frac{1}{2}$$
 AB

$$\therefore$$
 DE = BF

Now we have FE BD and DE BF

And FE = BD and DE = BF

Therefore, BDEF is a parallelogram.

(ii) BDEF is a parallelogram.

[diagonals of parallelogram divides it in two triangles of equal area] DCEF is also parallelogram.

$$\therefore$$
 ar $(\triangle DEF) = ar (\triangle DEC) \dots (ii)$

Also, AEDF is also parallelogram.

$$\therefore$$
 ar (\triangle AFE) = ar (\triangle DEF)(iii)

From eq. (i), (ii) and (iii),



$$ar(\Delta DEF) = ar(\Delta BDF) = ar(\Delta DEC) = ar(\Delta AFE) \dots (iv)$$

Now, ar
$$(\Delta ABC)$$
 = ar (ΔDEF) + ar (ΔBDF) + ar (ΔDEC) + ar (ΔAFE) (v) ar (ΔABC) = ar (ΔDEF) + ar (ΔDEF) + ar (ΔDEF) + ar (ΔDEF)

[Using (iv) & (v)]

$$ar (\Delta ABC) = 4 \times ar (\Delta DEF)$$

$$ar(\Delta DEF) = \frac{1}{4} ar(\Delta ABC)$$

(iii) ar (
$$\parallel$$
gm BDEF) = ar (Δ BDF) + ar (Δ DEF) = ar (Δ DEF) + ar (Δ DEF) [Using (iv)]

$$ar(\|gm BDEF) = 2 ar(\Delta DEF)$$

$$ar(\|gm BDEF) = 2 \times \frac{1}{4} ar(\Delta ABC)$$

$$ar(\|gm BDEF) = \frac{1}{2}ar(\Delta ABC)$$

Question 6:

In the given figure, diagonals AC and BD of quadrilateral ABCD intersect at O such that OB = OD. If AB = CD, then show that:

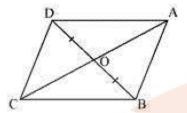
(i)
$$ar(DOC) = ar(AOB)$$

(ii)
$$ar(DCB) = ar(ACB)$$

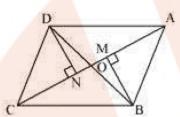
(iii) DA || CB or ABCD is a parallelogram.

[Hint: From D and B, draw perpendiculars to AC.]





Solution 6:



Let us draw DN \perp AC and BM \perp AC.

(i) In $\triangle DON$ and $\triangle BOM$,

 $\angle DNO = \angle BMO$ (By construction)

 $\angle DON = \angle BOM$ (Vertically opposite angles)

OD = OB (Given)

By AAS congruence rule,

 $\Delta DON \cong \Delta BOM$

 $DN = BM \qquad ... (1)$

We know that congruent triangles have equal areas.

Area (Δ DON) = Area (Δ BOM) ... (2)

In $\triangle DNC$ and $\triangle BMA$,

 $\angle DNC = \angle BMA$ (By construction)

CD = AB (given)

DN = BM [Using Equation (1)]

 $\therefore \Delta DNC \cong \Delta BMA (RHS congruence rule)$

∴ Area (\triangle DNC) = Area (\triangle BMA) ... (3)



On adding Equations (2) and (3), we obtain

Area (
$$\Delta$$
DON) + Area (Δ DNC) = Area (Δ BOM) + Area (Δ BMA)
Therefore, Area (Δ DOC) = Area (Δ AOB)

(ii) We obtained,

Area (
$$\triangle DOC$$
) = Area ($\triangle AOB$)

∴ Area (
$$\triangle DOC$$
) + Area ($\triangle OCB$) = Area ($\triangle AOB$) + Area ($\triangle OCB$) (Adding Area ($\triangle OCB$) to both sides)

$$\therefore$$
 Area ($\triangle DCB$) = Area ($\triangle ACB$)

(iii) We obtained,

Area (
$$\triangle DCB$$
) = Area ($\triangle ACB$)

If two triangles have the same base and equal areas, then these will lie between the same parallels.

In quadrilateral ABCD, one pair of opposite sides is equal (AB = CD) and the other pair of opposite sides is parallel (DA \parallel CB).

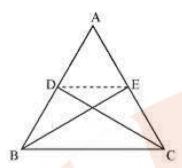
Therefore, ABCD is a parallelogram.

Question 7:

D and E are points on sides AB and AC respectively of \triangle ABC such that ar (DBC) = ar (EBC). Prove that DE || BC.

Solution 7:





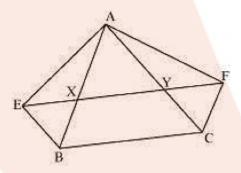
Since ΔBCE and ΔBCD are lying on a common base BC and also have equal areas, ΔBCE and ΔBCD will lie between the same parallel lines.

Question 8:

XY is a line parallel to side BC of a triangle ABC. If BE \parallel AC and CF \parallel AB meet XY at E and F respectively, show that

$$ar(ABE) = ar(ACF)$$

Solution 8:



It is given that

$$XY \parallel BC = EY \parallel BC$$

$$BE \parallel AC = BE \parallel CY$$

Therefore, EBCY is a parallelogram.

It is given that

$$XY \parallel BC = XF \parallel BC$$

$$FC \parallel AB = FC \parallel XB$$

Therefore, BCFX is a parallelogram.



Parallelograms EBCY and BCFX are on the same base BC and between the same parallels BC and EF.

$$\therefore \text{ Area (EBCY)} = \frac{1}{2} \text{ Area (BCFX)} \quad \dots \text{ (1)}$$

Consider parallelogram EBCY and ΔAEB

These lie on the same base BE and are between the same parallels BE and AC.

∴ Area (
$$\triangle$$
ABE) = $\frac{1}{2}$ Area (EBCY) ... (2)

Also, parallelogram Δ CFX and Δ ACF are on the same base CF and between the same parallels CF and AB.

∴ Area (
$$\triangle$$
ACF) = $\frac{1}{2}$ Area (BCFX) ... (3)

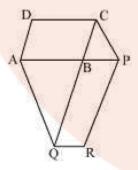
From Equations (1), (2), and (3), we obtain

Area (
$$\triangle$$
ABE) = Area (\triangle ACF)

Question 9:

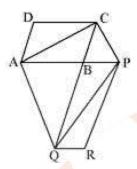
The side AB of a parallelogram ABCD is produced to any point P. A line through A and parallel to CP meets CB produced at Q and then parallelogram PBQR is completed (see the following figure). Show that ar (ABCD) = ar (PBQR).

[Hint: Join AC and PQ. Now compare area (ACQ) and area (APQ)]



Solution 9:





Let us join AC and PQ.

 \triangle ACQ and \triangle AQP are on the same base AQ and between the same parallels AQ and CP.

Area (ΔACQ) = Area (ΔAPQ)

Area (ΔACQ) – Area (ΔABQ) = Area (ΔAPQ) – Area (ΔABQ)

Area (ΔABC) = Area (ΔQBP) ... (1)

Since AC and PQ are diagonals of parallelograms ABCD and PBQR respectively,

Area ($\triangle ABC$) = $\frac{1}{2}$ Area (ABCD) ... (2)

Area ($\triangle QBP$) = $\frac{1}{2}$ Area (PBQR) ... (3)

From Equations (1), (2), and (3), we obtain

 $\frac{1}{2}$ Area (ABCD) = $\frac{1}{2}$ Area (PBQR)

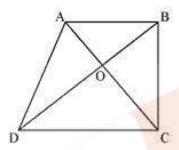
Area (ABCD) = Area (PBQR)

Question 10:

Diagonals AC and BD of a trapezium ABCD with AB \parallel DC intersect each other at O. Prove that ar (AOD) = ar (BOC).

Solution 10:





It can be observed that ΔDAC and ΔDBC lie on the same base DC and between the same parallels AB and CD.

Area (ΔDAC) = Area (ΔDBC)

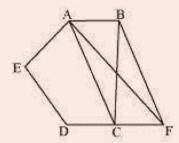
Area (ΔDAC) – Area (ΔDOC) = Area (ΔDBC) – Area (ΔDOC)

Area $(\Delta AOD) = Area (\Delta BOC)$

Question 11:

In the given figure, ABCDE is a pentagon. A line through B parallel to AC meets DC produced at F. Show that

- (i) ar(ACB) = ar(ACF)
- (ii) ar(AEDF) = ar(ABCDE)



Solution 11:

(i) \triangle ACB and \triangle ACF lie on the same base AC and are between

The same parallels AC and BF.

Area (ΔACB) = Area (ΔACF)

(ii) It can be observed that

Area (\triangle ACB) = Area (\triangle ACF)

Area (\triangle ACB) + Area (ACDE) = Area (\triangle ACF) + Area (ACDE)

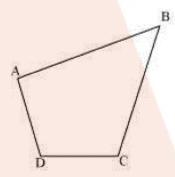
Area (ABCDE) = Area (AEDF)



Question 12:

A villager Itwaari has a plot of land of the shape of a quadrilateral. The Gram Panchayat of the village decided to take over some portion of his plot from one of the corners to construct a Health Centre. Itwaari agrees to the above proposal with the condition that he should be given equal amount of land in lieu of his land adjoining his plot so as to form a triangular plot. Explain how this proposal will be implemented.

Solution 12:



Let quadrilateral ABCD be the original shape of the field.

The proposal may be implemented as follows.

Join diagonal BD and draw a line parallel to BD through point A.

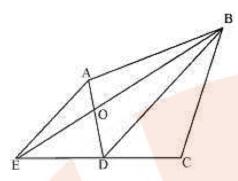
Let it meet the extended side CD of ABCD at point E.

Join BE and AD. Let them intersect each other at O.

Then, portion $\triangle AOB$ can be cut from the original field so that the new shape of the field will be $\triangle BCE$. (See figure).

We have to prove that the area of $\triangle AOB$ (portion that was cut so as to construct Health Centre) is equal to the area of $\triangle DEO$ (portion added to the field so as to make the area of the new field so formed equal to the area of the original field).





It can be observed that ΔDEB and ΔDAB lie on the same base BD and are between the same parallels BD and AE.

Area (ΔDEB) = Area (ΔDAB)

Area ($\triangle DEB$) – Area ($\triangle DOB$) = Area ($\triangle DAB$) – Area ($\triangle DOB$)

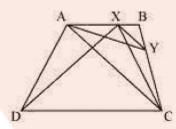
Area ($\triangle DEO$) = Area ($\triangle AOB$)

Question 13:

ABCD is a trapezium with AB \parallel DC. A line parallel to AC intersects AB at X and BC at Y. Prove that ar (ADX) = ar (ACY).

[Hint: Join CX.]

Solution 13:



It can be observed that ΔADX and ΔACX lie on the same base AX and are between the same parallels AB and DC.

Area
$$(\Delta ADX)$$
 = Area (ΔACX) ... (1)

 \triangle ACY and \triangle ACX lie on the same base AC and are between the same parallels AC and XY.

Area
$$(\Delta ACY)$$
 = Area (ACX) ... (2)

From Equations (1) and (2), we obtain

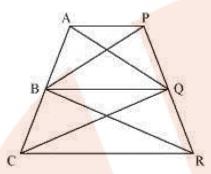
Area (ΔADX) = Area (ΔACY)



Question 14:

In the given figure, $AP \parallel BQ \parallel CR$. Prove that ar (AQC) = ar (PBR).

Solution 14:



Since $\triangle ABQ$ and $\triangle PBQ$ lie on the same base BQ and are between the same parallels AP and BQ,

∴ Area (
$$\triangle$$
ABQ) = Area (\triangle PBQ) ... (1)

Again, Δ BCQ and Δ BRQ lie on the same base BQ and are between the same parallels BQ and CR.

$$\therefore$$
 Area (ΔBCQ) = Area (ΔBRQ) ... (2)

On adding Equations (1) and (2), we obtain

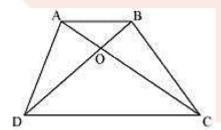
Area
$$(\Delta ABQ)$$
 + Area (ΔBCQ) = Area (ΔPBQ) + Area (ΔBRQ)

$$\therefore$$
 Area (\triangle AQC) = Area (\triangle PBR)

Question 15:

Diagonals AC and BD of a quadrilateral ABCD intersect at O in such a way that ar (AOD) = ar (BOC). Prove that ABCD is a trapezium.

Solution 15:





It is given that

Area ($\triangle AOD$) = Area ($\triangle BOC$)

Area ($\triangle AOD$) + Area ($\triangle AOB$) = Area ($\triangle BOC$) + Area ($\triangle AOB$)

Area (\triangle ADB) = Area (\triangle ACB)

We know that triangles on the same base having areas equal to each other lie between the same parallels.

Therefore, these triangles, \triangle ADB and \triangle ACB, are lying between the same parallels.

i.e., AB || CD

Therefore, ABCD is a trapezium.

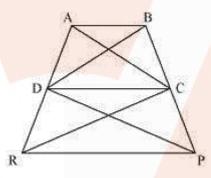
Question 16:

In the given figure, ar (DRC) = ar (DPC) and ar (BDP) = ar (ARC). Show that both the quadrilaterals ABCD and DCPR are trapeziums.

Solution 16:

It is given that

Area ($\triangle DRC$) = Area ($\triangle DPC$)



As $\triangle DRC$ and $\triangle DPC$ lie on the same base DC and have equal areas, therefore, they must lie between the same parallel lines.

∴ DC || RP

Therefore, DCPR is a trapezium.

It is also given that

Area ($\triangle BDP$) = Area ($\triangle ARC$)

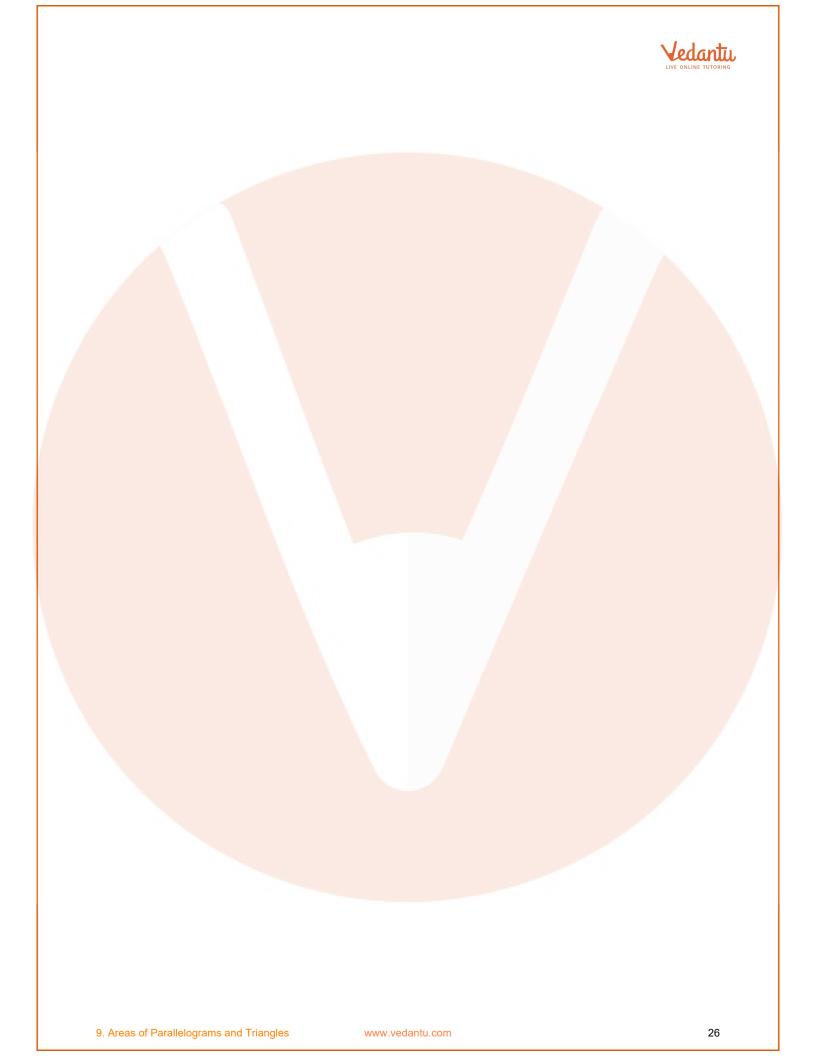
Area ($\triangle BDP$) – Area ($\triangle DPC$) = Area ($\triangle ARC$) – Area ($\triangle DRC$)

 \therefore Area (\triangle BDC) = Area (\triangle ADC)

Since $\triangle BDC$ and $\triangle ADC$ are on the same base CD and have equal areas, they must lie between the same parallel lines.

∴ AB || CD

Therefore, ABCD is a trapezium.



Exercise (9.4)



Question 1:

Parallelogram ABCD and rectangle ABEF are on the same base AB and have equal areas. Show that the perimeter of the parallelogram is greater than that of the rectangle.

Solution 1: As the parallelogram and the rectangle have the same base and equal area, therefore, these will also lie between the same parallels.

Consider the parallelogram ABCD and rectangle ABEF as follows.



Here, it can be observed that parallelogram ABCD and rectangle ABEF are between the same parallels AB and CF.

We know that opposite sides of a parallelogram or a rectangle are of equal lengths.

Therefore,

AB = EF (For rectangle)

AB = CD (For parallelogram)

 \therefore CD = EF

$$\therefore AB + CD = AB + EF \qquad \dots (1)$$

Of all the line segments that can be drawn to a given line from a point not lying on it, the perpendicular line segment is the shortest.

 $\therefore AF < AD$

And similarly, BE < BC

$$\therefore AF + BE < AD + BC \qquad \dots (2)$$

From Equations (1) and (2), we obtain

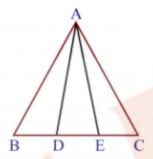
$$AB + EF + AF + BE < AD + BC + AB + CD$$

Perimeter of rectangle ABEF < Perimeter of parallelogram ABCD.

Question 2:

In the following figure, D and E are two points on BC such that BD = DE = EC. Show that ABD = ABD



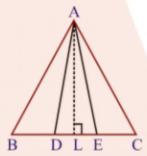


Can you now answer the question that you have left in the 'Introduction' of this chapter, whether the field of Budhia has been actually divided into three parts of equal area?

[Remark: Note that by taking BD = DE = EC, the triangle ABC is divided into three triangles ABD, ADE and AEC of equal areas. In the same way, by dividing BC into n equal parts and joining the points of division so obtained to the opposite vertex of BC, you can divide \triangle ABC into n triangles of equal areas.]

Solution 2:

Let us draw a line segment $AL \perp BC$.



We know that,

Area of a triangle =
$$\frac{1}{2} \times \text{Base} \times \text{Altitude}$$

Area (
$$\triangle ADE$$
) = $\frac{1}{2} \times DE \times AL$

Area (
$$\triangle ABD$$
) = $\frac{1}{2} \times BD \times AL$

Area (
$$\triangle AEC$$
) = $\frac{1}{2} \times EC \times AL$

It is given that DE = BD = EC

$$\frac{1}{2} \times DE \times AL = \frac{1}{2} \times BD \times AL = \frac{1}{2} \times EC \times AL$$

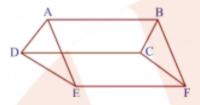
Area (
$$\triangle$$
ADE) = Area (\triangle ABD) = Area (\triangle AEC)

It can be observed that *Budhia* has divided her field into 3 equal parts.



Question 3:

In the following figure, ABCD, DCFE and ABFE are parallelograms. Show that ar $(\Delta ADE) = ar(\Delta BCF)$.



Solution 3:

It is given that ABCD is a parallelogram. We know that opposite sides of a parallelogram are equal.

 \therefore AD = BC ... (1)

Similarly, for parallelograms DCEF and ABFE, it can be proved that

DE = CF ... (2)

And, EA = FB ... (3)

In \triangle ADE and \triangle BCF,

AD = BC [Using equation (1)]

DE = CF [Using equation (2)]

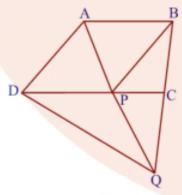
EA = FB [Using equation (3)]

 $\therefore \triangle ADE \cong \triangle BCF (SSS congruence rule)$

 \therefore Area (\triangle ADE) = Area (\triangle BCF)

Question 4:

In the following figure, ABCD is parallelogram and BC is produced to a point Q such that AD = CQ. If AQ intersect DC at P, show that ar (ΔBPC) = ar (ΔDPQ) .



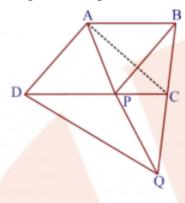
[*Hint:* Join AC.]

Solution 4:

It is given that ABCD is a parallelogram.



AD \parallel BC and AB \parallel DC(Opposite sides of a parallelogram are parallel to each other) Join point A to point C.



Consider $\triangle APC$ and $\triangle BPC$

 Δ APC and Δ BPC are lying on the same base PC and between the same parallels PC and AB. Therefore,

Area (\triangle APC) = Area (\triangle BPC) ... (1)

In quadrilateral ACDQ, it is given that

AD = CQ

Since ABCD is a parallelogram,

AD || BC (Opposite sides of a parallelogram are parallel)

CQ is a line segment which is obtained when line segment BC is produced.

∴ AD || CQ

We have,

AC = DQ and $AC \parallel DQ$

Hence, ACQD is a parallelogram.

Consider BDCQ and BACQ

These are on the same base CQ and between the same parallels CQ and AD.

Therefore,

Area (ΔDCQ) = Area (ΔACQ)

∴ Area ($\triangle DCQ$) – Area ($\triangle PQC$) = Area ($\triangle ACQ$) – Area ($\triangle PQC$)

 \therefore Area (\triangle DPQ) = Area (\triangle APC) ... (2)

From equations (1) and (2), we obtain

Area ($\triangle BPC$) = Area ($\triangle DPQ$)



Question 5:

In the following figure, ABC and BDE are two equilateral triangles such that D is the mid-point of BC. If AE intersects BC at F, show that

(i)
$$\operatorname{ar}(BDE) = \frac{1}{4} \operatorname{ar}(ABC)$$

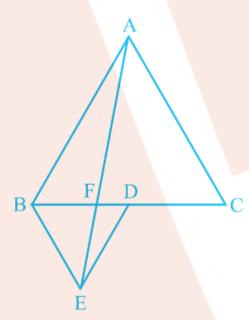
(ii)
$$\operatorname{ar}(BDE) = \frac{1}{2} \operatorname{ar}(BAE)$$

(iii)
$$ar(ABC) = 2 ar(BEC)$$

(iv)
$$ar(BFE) = ar(AFD)$$

(v)
$$ar(BFE) = 2 ar(FED)$$

(vi)
$$\operatorname{ar}(FED) = \frac{1}{8} \operatorname{ar}(AFC)$$

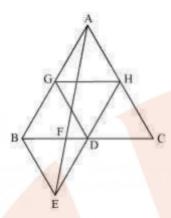


[Hint: Join EC and AD. Show that BE || AC and DE || AB etc.]

Solution 5:

(i) Let G and H be the mid-points of side AB and AC respectively. Line segment GH is joining the mid-points and is parallel to third side. Therefore, BC will be half of the length of BC (mid-point theorem).





∴ GH =
$$\frac{1}{2}$$
 BC and GH || BD

 \therefore GH = BD = DC and GH || BD (D is the mid-point of BC)

Similarly,

• GD = HC = HA

• HD = AG = BG

Therefore, clearly $\triangle ABC$ is divided into 4 equal equilateral triangles viz $\triangle BGD$, $\triangle AGH$, $\triangle DHC$ and $\triangle GHD$

In other words, $\triangle BGD = \frac{1}{4} \triangle ABC$

Now consider $\triangle BDG$ and $\triangle BDE$

BD = BD (Common base)

As both triangles are equilateral triangle, we can say

BG = BE

DG = DE

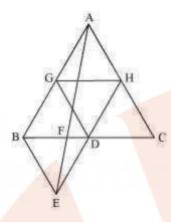
Therefore, $\triangle BDG \cong \triangle BDE$ [By SSS congruency]

Thus, area ($\triangle BDG$) = area ($\triangle BDE$)

$$ar(\Delta BDE) = \frac{1}{4} ar(\Delta ABC)$$

Hence proved





(ii) Area (
$$\Delta BDE$$
) = Area (ΔAED) (Common base DE and DE||AB)
Area (ΔBDE) - Area (ΔFED) = Area (ΔAED) - Area (ΔFED)
Area (ΔBEF) = Area (ΔAFD) ... (1)

Now, Area (ΔABD) = Area (ΔABF) + Area (ΔAFD)

Area (ΔABD) = Area (ΔABF) + Area (ΔBEF) [From equation (1)]

Area (ΔABD) = Area (ΔABE) ... (2)

AD is the median in \triangle ABC.

ar
$$(\Delta ABD) = \frac{1}{2} \operatorname{ar} (\Delta ABC)$$

= $\frac{4}{2} \operatorname{ar} (\Delta BDE)$ (As proved earlier)

$$ar (\Delta ABD) = 2ar (\Delta BDE)$$
 (3)

From (2) and (3), we obtain 2 ar ($\triangle BDE$) = ar ($\triangle ABE$) ar (BDE) = $\frac{1}{2}$ ar (BAE)

(iii)
ar (
$$\triangle$$
ABE) = ar (\triangle BEC) (Common base BE and BE||AC)
ar (\triangle ABF) + ar (\triangle BEF) = ar (\triangle BEC)

Using equation (1), we obtain ar (ΔABF) + ar (ΔAFD) = ar (ΔBEC) ar (ΔABD) = ar (ΔBEC)

$$\frac{1}{2}$$
 ar ($\triangle ABC$) = ar ($\triangle BEC$)

 $ar(\Delta ABC) = 2 ar(\Delta BEC)$



(iv) It is seen that ΔBDE and ar ΔAED lie on the same base (DE) and between the parallels DE and AB.

∴ ar
$$(\Delta BDE)$$
 = ar (ΔAED)
∴ ar (ΔBDE) - ar (ΔFED) = ar (ΔAED) - ar (ΔFED)
∴ ar (ΔBFE) = ar (ΔAFD)

(v) Let h be the height of vertex E, corresponding to the side BD in \triangle BDE. Let H be the height of vertex A, corresponding to the side BC in \triangle ABC.

In (i), it was shown that ar (BDE) =
$$\frac{1}{4}$$
 ar (ABC)

In (iv), it was shown that ar $(\Delta BFE) = ar (\Delta AFD)$.

∴ ar (
$$\triangle$$
BFE) = ar (\triangle AFD)
= 2 ar (\triangle FED)

Hence,

(vi)

ar (
$$^{\Delta}$$
 AFC) = ar ($^{\Delta}$ AFD) + ar ($^{\Delta}$ ADC) = 2 ar ($^{\Delta}$ FED) + $\frac{1}{2}$ ar ($^{\Delta}$ ABC) [using (v)

= 2 ar (
$$^{\Delta}$$
FED) + $\frac{1}{2}$ [4 × ar ($^{\Delta}$ BDE)] [Using result of part (i)]

= 2 ar (
$$^{\Delta}$$
 FED) + 2 ar ($^{\Delta}$ BDE) = 2 ar ($^{\Delta}$ FED) + 2 ar ($^{\Delta}$ AED)

[$^{\Delta}$ BDE and $^{\Delta}$ AED are on the same base and between same parallels]

= 2 ar (
$$^{\Delta}$$
 FED) + 2 [ar ($^{\Delta}$ AFD) + ar ($^{\Delta}$ FED)]

= 2 ar (
$$^{\Delta}$$
 FED) + 2 ar ($^{\Delta}$ AFD) + 2 ar ($^{\Delta}$ FED) [Using (viii)]

= 4 ar (
$$^{\Delta}$$
 FED) + 4 ar ($^{\Delta}$ FED)

$$\Rightarrow$$
 ar (\triangle AFC) = 8 ar (\triangle FED)

$$\Rightarrow$$
 ar $(^{\Delta}\text{FED}) = \frac{1}{8} \text{ ar } (^{\Delta}\text{AFC})$

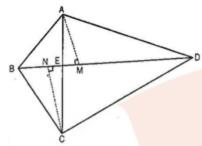
Question 6:

Diagonals AC and BD of a quadrilateral ABCD intersect each other at P. Show that [Hint: From A and C, draw perpendiculars to BD]

Solution 6:

Given: A quadrilateral ABCD, in which diagonals AC and BD intersect each other at point E.





To Prove: $ar(\Delta AED) \times ar(\Delta BEC)$ = $ar(\Delta ABE) \times ar(\Delta CDE)$

Construction: From A, draw $AM \perp BD$ AM BD and from C, draw $CN \perp BD$.

Proof :
$$ar(\Delta ABE) = \frac{1}{2} \times BE \times AM....(i)$$

$$ar(\Delta AED) = \frac{1}{2} \times DE \times AM....(ii)$$

Dividing eq. (ii) by (i), we get,

$$\frac{\operatorname{ar}(\Delta AED)}{\operatorname{ar}(\Delta ABE)} = \frac{\frac{1}{2} \times DE \times AM}{\frac{1}{2} \times BE \times AM}$$

$$\Rightarrow \frac{\operatorname{ar}(\Delta AED)}{\operatorname{ar}(\Delta ABE)} = \frac{DE}{BE}...(iii)$$

Similarly
$$\frac{\operatorname{ar}(\Delta CDE)}{\operatorname{ar}(\Delta BEC)} = \frac{DE}{BE}$$
....(iv)

From eq. (iii) and (iv), we get

$$\frac{\operatorname{ar}(\Delta AED)}{\operatorname{ar}(\Delta ABE)} = \frac{\operatorname{ar}(\Delta CDE)}{\operatorname{ar}(\Delta BEC)}$$

$$\Rightarrow$$
 ar(\triangle AED) \times ar(\triangle BEC) = ar(\triangle ABE) \times ar(\triangle CDE)

Hence proved.

Question 7:

P and Q are respectively the mid-points of sides AB and BC of a triangle ABC and R is the mid-point of AP, show that

(i) ar (PRQ) =
$$\frac{1}{2}$$
 ar (ARC)



(ii) ar (RQC) =
$$\frac{3}{8}$$
 ar (ABC)

$$(iii)$$
 ar $(PBQ) = ar (ARC)$

Solution 7:

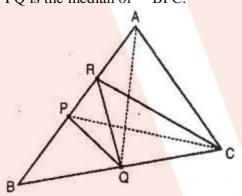
(i) PC is the median of \triangle ABC.

$$\therefore$$
 ar (\triangle BPC) = ar (\triangle APC)(i)

RC is the median \triangle of APC.

$$\therefore \operatorname{ar} (\Delta \operatorname{ARC}) = \frac{1}{2} \operatorname{ar} (\Delta \operatorname{APC}) \dots (ii)$$

[Median divides the triangle into two triangles of equal area] PQ is the median of \triangle BPC.



$$\therefore \operatorname{ar} \left(^{\Delta} \operatorname{PQC} \right) = \frac{1}{2} \operatorname{ar} \left(^{\Delta} \operatorname{BPC} \right) \dots (iii)$$

From eq. (i) and (iii), we get,

ar
$$(^{\Delta}PQC) = \frac{1}{2}$$
 ar $(^{\Delta}APC)$ (iv)

From eq. (ii) and (iv), we get,

$$\operatorname{ar}\left(\Delta\operatorname{PQC}\right) = \operatorname{ar}\left(\Delta\operatorname{ARC}\right)....(v)$$

We are given that P and Q are the mid-points of AB and BC respectively.

$$\therefore$$
 PQ || AC and PA = $\frac{1}{2}$ AC

 \Rightarrow ar (\triangle APQ) = ar (\triangle PQC)(vi) [triangles between same parallel are equal in area]

From eq. (v) and (vi), we get

$$\operatorname{ar}(\Delta APQ) = \operatorname{ar}(\Delta ARC) \dots (vii)$$

R is the mid-point of AP. Therefore RQ is the median of \triangle APQ.

$$\therefore$$
 ar $(\triangle PRQ) = \frac{1}{2}$ ar $(\triangle APQ)$ (viii)

From (vii) and (viii), we get,

ar (
$$^{\Delta}$$
PRQ) = $\frac{1}{2}$ ar ($^{\Delta}$ ARC)



(ii) PQ is the median of \triangle BPC

$$\therefore \operatorname{ar} (\Delta \operatorname{PQC}) = \frac{1}{2} \operatorname{ar} (\Delta \operatorname{BPC}) = \frac{1}{2} \times \frac{1}{2} \operatorname{ar} (\Delta \operatorname{ABC}) = \frac{1}{4} \operatorname{ar} (\Delta \operatorname{ABC}) \dots (\operatorname{ix})$$

Also ar
$$(^{\Delta}PRC) = \frac{1}{2}$$
 ar $(^{\Delta}APC)$ [Using (iv)]

$$\Rightarrow$$
 ar $(\triangle PRC) = \frac{1}{2} \times \frac{1}{2}$ ar $(\triangle ABC) = \frac{1}{4}$ ar $(\triangle ABC)$ (x)

Adding eq. (ix) and (x), we get,

ar
$$(\Delta PQC)$$
 + ar (ΔPRC) = $\left(\frac{1}{4} + \frac{1}{4}\right)$ ar (ΔABC)

$$\Rightarrow$$
 ar (quad. PQCR) = $\frac{1}{2}$ ar (\triangle ABC)(xi)

Subtracting ar ($^{\Delta}$ PRQ) from the both sides,

ar (quad. PQCR) – ar (
$$^{\Delta}$$
PRQ) = $\frac{1}{2}$ ar ($^{\Delta}$ ABC) – ar ($^{\Delta}$ PRQ)

$$\Rightarrow$$
 ar $(^{\Delta}RQC) = \frac{1}{2}$ ar $(^{\Delta}ABC) - \frac{1}{2}$ ar $(^{\Delta}ARC)$ [Using result (i)]

$$\Rightarrow$$
 ar $(^{\Delta}ARC) = \frac{1}{2}$ ar $(^{\Delta}ABC) - \frac{1}{2} \times \frac{1}{2}$ ar $(^{\Delta}APC)$

$$\Rightarrow$$
 ar $(^{\Delta}RQC) = \frac{1}{2}$ ar $(^{\Delta}ABC) - \frac{1}{4}$ ar $(^{\Delta}APC)$

$$\Rightarrow_{\text{ar}} (^{\Delta} \text{RQC}) = \frac{1}{2} \text{ ar } (^{\Delta} \text{ABC}) - \frac{1}{4} \times \frac{1}{2} \text{ ar } (^{\Delta} \text{ABC}) \text{ [PC is median of } ^{\Delta} \text{ABC]}$$

$$\Rightarrow \operatorname{ar} (^{\Delta} \operatorname{RQC}) = \frac{1}{2} \operatorname{ar} (^{\Delta} \operatorname{ABC}) - \frac{1}{8} \operatorname{ar} (^{\Delta} \operatorname{ABC})$$

$$\Rightarrow_{\text{ar}} (\Delta_{\text{RQC}}) = \left(\frac{1}{2} - \frac{1}{8}\right) \times \text{ar} (\Delta_{\text{ABC}})$$

$$\Rightarrow_{ar} (\Delta_{RQC}) = \frac{3}{8} ar (\Delta_{ABC})$$

(iii) ar
$$(^{\Delta}PRQ) = \frac{1}{2}$$
 ar $(^{\Delta}ARC)$ [Using result (i)] \Rightarrow 2 ar $(^{\Delta}PRQ) =$ ar $(^{\Delta}ARC)$...(xii)

ar
$$(^{\Delta}PRQ) = \frac{1}{2}$$
 ar $(^{\Delta}APQ)$ [RQ is the median of $^{\Delta}APQ$](xiii)

But ar $(^{\Delta}APQ)$ = ar $(^{\Delta}PQC)$ [Using reason of eq. (vi)](xiv)

From eq. (xiii) and (xiv), we get,

ar
$$(^{\Delta}PRQ) = \frac{1}{2}$$
 ar $(^{\Delta}PQC)$ (xv)

But ar $(^{\Delta}BPQ)$ = ar $(^{\Delta}PQC)$ [PQ is the median of $^{\Delta}BPC$](xvi) From eq. (xv) and (xvi), we get,

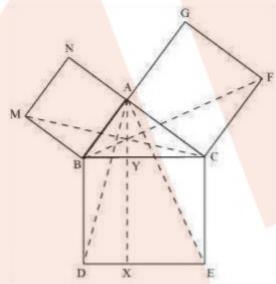


ar (
$$^{\Delta}$$
PRQ) = $\frac{1}{2}$ ar ($^{\Delta}$ BPQ)(xvii)

Now from (xii) and (xvii), we get,

$$2 \times \frac{1}{2} ar(\Delta BPQ) = ar(\Delta ARC) \Rightarrow ar(\Delta BPQ) = ar(\Delta ARC)$$

Question 8: In the following figure, ABC is a right triangle right angled at A. BCED, ACFG and ABMN are squares on the sides BC, CA and AB respectively. Line segment $AX \perp DE$ meets BC at Y.



Show that:

- (i) \triangle MBC $\cong \triangle$ ABD
- (ii) ar(BYXD) = 2ar(MBC)
- (iii) ar(BYXD) = 2ar(ABMN)
- (iv) $\triangle FCB \cong \triangle ACE$
- (v) ar(CYXE) = 2ar(FCB)
- (vi) ar(CYXE) = ar(ACFG)
- (vii) ar(BCED) = ar(ABMN) + ar(ACFG)

Note: Result (vii) is the famous *Theorem of Pythagoras*. You shall learn a simpler proof of this theorem in class X.

Solution 8: (i) We know that each angle of a square is 90°.

Hence,
$$\angle ABM = \angle DBC = 90^{\circ}$$

$$\therefore \angle ABM + \angle ABC = \angle DBC + \angle ABC$$

$$\therefore \angle MBC = \angle ABD$$



```
In \triangleMBC and \triangleABD,
\angleMBC = \angleABD (Proved above)
MB = AB (Sides of square ABMN)
BC = BD (Sides of square BCED)
\therefore \Delta MBC \cong \Delta ABD (SAS congruence rule)
(ii) We have
\DeltaMBC \cong \DeltaABD
\therefore ar (\triangleMBC) = ar (\triangleABD) ... (1)
It is given that AX \perp DE and BD \perp DE (Adjacent sides of square BDEC)
: BD || AX (Two lines perpendicular to same line are parallel to each other)
AABD and parallelogram BYXD are on the same base BD and between the same parallels BD
and AX.
Area (\Delta YXD) = 2 Area (\Delta MBC) [Using equation (1)] ... (2)
(iii) ΔMBC and parallelogram ABMN are lying on the same base MB and between
same parallels MB and NC.
2 \operatorname{ar} (\Delta MBC) = \operatorname{ar} (ABMN)
ar(\Delta YXD) = ar(ABMN) [Using equation (2)] ... (3)
(iv) We know that each angle of a square is 90°.
\therefore \angle FCA = \angle BCE = 90^{\circ}
\therefore \angle FCA + \angle ACB = \angle BCE + \angle ACB
∴ ∠FCB = ∠ACE
In \triangleFCB and \triangleACE,
\angle FCB = \angle ACE
FC = AC (Sides of square ACFG)
CB = CE (Sides of square BCED)
\Delta FCB \cong \Delta ACE (SAS congruence rule)
(v) It is given that AX \perp DE and CE \perp DE (Adjacent sides of square BDEC)
Hence, CE | AX (Two lines perpendicular to the same line are parallel to each other)
Consider BACE and parallelogram CYXE
BACE and parallelogram CYXE are on the same base CE and between the same
parallels CE and AX.
\therefore ar (\Delta YXE) = 2 ar (\Delta ACE) \dots (4)
We had proved that
\therefore \Delta FCB \cong \Delta ACE
ar (\Delta FCB) \cong ar (\Delta ACE) ... (5)
On comparing equations (4) and (5), we obtain
ar (CYXE) = 2 ar (\DeltaFCB) ... (6)
(vi) Consider BFCB and parallelogram ACFG
BFCB and parallelogram ACFG are lying on the same base CF and between the same
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$$\therefore$$
 ar (ACFG) = 2 ar (\triangle FCB)

parallels CF and BG.



∴ ar (ACFG) = ar (CYXE) [Using equation (6)] ... (7) (vii) From the figure, it is evident that ar $(\Delta CED) = ar (\Delta YXD) + ar (CYXE)$ ∴ ar $(\Delta CED) = ar (ABMN) + ar (ACFG)$ [Using equations (3) and (7)].



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