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EXERCISE NO: 12.1



Question 1:

The radii of two circles are 19 cm and 9 cm respectively. Find the radius of the circle which has circumference equal to the sum of the circumferences of the two circles.

Solution 1:

Radius (r_1) of 1st circle = 19 cm Radius (r_2) or 2nd circle = 9 cm Let the radius of 3rd circle be r. Circumference of 1st circle = 2 $\pi r_1 = 2\pi$ (19) = 38 π Circumference of 2nd circle = 2 $\pi r_2 = 2\pi$ (9) = 18 π Circumference of 3rd circle = 2 πr Given that, Circumference of 3rd circle = Circumference of 1st circle + Circumference of 2nd circle 2 $\pi r = 38\pi + 18\pi = 56\pi$ $r = \frac{56\pi}{2\pi} = 28$

Therefore, the radius of the circle which has circumference equal to the sum of the circumference of the given two circles is 28 cm.

Question 2:

The radii of two circles are 8 cm and 6 cm respectively. Find the radius of the circle having area equal to the sum of the areas of the two circles.

Solution 2: Padius of (r) 1st

Radius of $(r_1) 1^{st}$ circle = 8 cm Radius of $(r_2) 2^{nd}$ circle = 6 cm Let the radius of 3^{rd} circle be r. Area of 1^{st} circle = $\pi r_1^2 = \pi (8)^2 = 64\pi$ Area of 2^{nd} circle = $\pi r_2^2 = \pi (6)^2 = 36\pi$ Given that, Area of 3rd circle = Area of 1^{st} circle + Area of 2^{nd} circle



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 $\pi r^{2} = \pi r_{1}^{2} + \pi r_{2}^{2}$ $\pi r^{2} = 64\pi + 36\pi$ $\pi r^{2} = 100\pi$ $r^{2} = 100$ $r = \pm 10$

However, the radius cannot be negative. Therefore, the radius of the circle having area equal to the sum of the areas of the two circles is 10 cm.

Question 3:

Given figure depicts an archery target marked with its five scoring areas from the centre outwards as Gold, Red, Blue, Black and White. The diameter of the region representing Gold score is 21 cm and each of the other bands is 10.5

cm wide. Find the area of each of the five scoring regions. Use $\pi = \frac{22}{7}$



Solution 3:



Radius (r_i) of gold region (i.e., 1^{st} circle) $=\frac{21}{2}=10.5$ cm Given that each circle is 10.5 cm wider than the previous circle.



Therefore, radius (r_2) of 2^{nd} circle = 10.5 + 10.5 = 21 cm Radius (r_3) of 3^{rd} circle = 21 + 10.5= 31.5 cm Radius (r_4) of 4^{th} circle = 31.5 + 10.5= 42 cm Radius (r_5) of 5^{th} circle = 42 + 10.5= 52.5 cm

Area of gold region = Area of 1st circle = $\pi r_1^2 = \pi (10.5)^2 = 346.5 \text{ cm}^2$

Area of red region = Area of 2nd circle – Area of 1st circle $= \pi r_2^2 - \pi r_1^2$ $= \pi (21)^2 - (10.5)^2$ $= 441\pi - 110.25\pi = 330.75\pi$ $= 1039.5 \text{ cm}^2$

Area of blue region = Area of 3rd circle - Area of 2nd circle = $\pi r_3^2 - \pi r_1^2$ = $\pi (31.5)^2 - \pi (21)^2$ = 992.25 $\pi - 441\pi = 551.25\pi$ = 1732.5 cm²

Area of black region = Area of 4th circle – Area of 3rd circle = $\pi r_4^2 - \pi r_3^2$ = $\pi (42)^2 - \pi (31.5)^2$ = $1764\pi - 992.25\pi$ = $771.75\pi = 2425.5 \text{ cm}^2$

Area of white region = Area of 5th circle – Area of 4th circle = $\pi r_5^2 - \pi r_4^2$ = $\pi (52.5)^2 - \pi (42)^2$ = 2756.25 π - 1764 π = 992.25 π = 3118.5 cm²

Therefore, areas of gold, red, blue, black, and white regions are 346.5 cm², 1039.5 cm², 1732.5 cm², 2425.5 cm² and 3118.5 cm² respectively.



Question 4:

The wheels of a car are of diameter 80 cm each. How many complete revolutions does each wheel make in 10 minutes when the car is traveling at a speed of 66 km per hour?

Solution 4:

Diameter of the wheel of the car = 80 cm Radius (r) of the wheel of the car = 40 cm Circumference of wheel = $2\pi r$ = $2\pi (40) = 80\pi$ cm Speed of car = 66 km/hour = $\frac{66 \times 100000}{60}$ cm/min = 110000 cm/min Distance travelled by the car in 10 minutes = $110000 \times 10 = 1100000$ cm

Let the number of revolutions of the wheel of the car be n.

 $n \times \text{Distance travelled in 1 revolution (i.e., circumference)}$

= Distance travelled in 10 minutes

```
n \times 80\pi = 1100000n = \frac{1100000 \times 7}{80 \times 22}= \frac{35000}{8} = 4375
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Therefore, each wheel of the car will make 4375 revolutions.



Question 5:

Tick the correct answer in the following and justify your choice: If the perimeter and the area of a circle are numerically equal, then the radius of the circle is (A) 2 units (B) π units (C) 4 units (D) 7 units

Solution 5:

Let the radius of the circle be r. Circumference of circle = $2\pi r$ Area of circle = πr^2 Given that, the circumference of the circle and the area of the circle are equal. This implies $2\pi r = \pi r^2$ 2 = rTherefore, the radius of the circle is 2 units. Hence, the correct answer is A.

EXERCISE NO: 12.2



Question 1:

Find the area of a sector of a circle with radius 6 cm if angle of the sector is

$$60^\circ \cdot \left[\text{Use } \pi = \frac{22}{7} \right]$$

Solution 1:



Let OACB be a sector of the circle making 60° angle at centre O of the circle. Area of sector of angle $\theta = \frac{\theta}{360^{\circ}} \times \pi r^2$ Area of sector OACB $= \frac{60^{\circ}}{360^{\circ}} \times \frac{22}{7} \times (6)^2$ $= \frac{1}{6} \times \frac{22}{7} \times 6 \times 6 = \frac{132}{7} \text{ cm}^2$ Therefore, the area of the sector of the circle making 60° at the centre of the circle is $\frac{132}{7} \text{ cm}^2$

Question 2:

Find the area of a quadrant of a circle whose circumference is 22 cm.

Use
$$\pi = \frac{22}{7}$$

Solution 2:



Let the radius of the circle be *r*. Circumference = 22 cm $2\pi r = 22$ $r = \frac{22}{2\pi} = \frac{11}{\pi}$



Quadrant of circle will subtend 90° angle at the centre of the circle.

Area of such quadrant of the circle = $\frac{90^{\circ}}{360^{\circ}} \times \pi \times r^2$

$$= \frac{1}{4} \times \pi \times \left(\frac{11}{\pi}\right)$$
$$= \frac{121}{4\pi}$$
$$= \frac{121 \times 7}{4 \times 22}$$
$$= \frac{77}{8} \text{ cm}^{2}$$

Question 3:

The length of the minute hand of a clock is 14 cm. Find the area swept by the minute hand in 5 minutes. $\left[\text{Use } \pi = \frac{22}{7} \right]$

Solution 3:



We know that in 1 hour (i.e., 60 minutes), the minute hand rotates 360°.

In 5 minutes, minute hand will rotate $=\frac{360^{\circ}}{60^{\circ}} \times 5 = 30^{\circ}$

Therefore, the area swept by the minute hand in 5 minutes will be the area of a sector of 30° in a circle of 14 cm radius.

Area of sector of angle
$$\theta = \frac{\theta}{360^{\circ}} \times \pi r^2$$

Area of sector of $30^{\circ} = \frac{30^{\circ}}{360^{\circ}} \times \frac{22}{7} \times 14 \times 14$
$$= \frac{22}{12} \times 2 \times 14$$
$$= \frac{11 \times 14}{3}$$
$$= \frac{154}{3} cm^2$$



Therefore, the area swept by the minute hand in 5 minutes is $\frac{154}{3}$ cm²

Question 4:

A chord of a circle of radius 10 cm subtends a right angle at the centre. Find the area of the corresponding:

(i) Minor segment (ii) Major sector [Use $\pi = 3.14$]

Solution 4:



Let AB be the chord of the circle subtending 90° angle at centre O of the circle.

Area of major sector OADB = $= \left(\frac{360^{\circ} - 90^{\circ}}{360^{\circ}}\right) \times \pi r^2 = \left(\frac{270^{\circ}}{360^{\circ}}\right) \pi r^2$ $= \frac{3}{4} \times 3.14 \times 10 \times 10$ $= 235.5 \text{ cm}^2$ Area of minor sector OACB $= \frac{90^{\circ}}{360^{\circ}} \times \pi r^2$ $= \frac{1}{4} \times 3.14 \times 10 \times 10$ $= 78.5 \text{ cm}^2$ Area of $\triangle OAB = \frac{1}{2} \times OA \times OB = \frac{1}{2} \times 10 \times 10$ $= 50 \text{ cm}^2$ Area of minor segment ACBA = Area of minor sector OACB -

Area of $\triangle OAB = 78.5 - 50 = 28.5 \, \text{cm}^2$



Question 5:

In a circle of radius 21 cm, an arc subtends an angle of 60° at the centre. Find:

(i) The length of the arc

(ii) Area of the sector formed by the arc

(iii) Area of the segment formed by the corresponding chord

$$\left[\text{Use } \pi = \frac{22}{7} \right]$$

Solution 5:

Radius (r) of circle = 21 cmAngle subtended by the given arc = 60°

Length of an arc of a sector of angle $\theta = \frac{\theta}{360^{\circ}} \times 2\pi r$



Length of arc ACB = $\frac{60^{\circ}}{360^{\circ}} \times 2 \times \frac{22}{7} \times 21$ = $\frac{1}{6} \times 2 \times 22 \times 3$ = 22 cm Area of sector OACB = $\frac{60^{\circ}}{360^{\circ}} \times \pi r^{2}$ = $\frac{1}{6} \times \frac{22}{7} \times 21 \times 21$ = 231cm²

In $\triangle OAB$, $\angle OAB = \angle OBA (As radius OA = OB)$ $\angle OAB + \angle AOB + \angle OBA = 180^{\circ}$ $2\angle OAB + 60^{\circ} = 180^{\circ}$ $\angle OAB = 60^{\circ}$ Therefore, $\triangle OAB$ is an equilateral triangle.



Area of
$$\triangle OAB = \frac{\sqrt{3}}{4} \times (Side)^2$$

= $\frac{\sqrt{3}}{4} \times (21)^2 = \frac{441\sqrt{3}}{4} \text{ cm}^2$

Area of segment $ACB = Area of sector OACB - Area of \Delta OAB$

$$\left(231 - \frac{441\sqrt{3}}{4}\right)$$
 cm²

Question 6:

A chord of a circle of radius 15 cm subtends an angle of 60° at the centre. Find the areas of the corresponding minor and major segments of the circle. [Use $\pi = 3.14$ and $\sqrt{3} = 1.73$]

Solution 6:



Radius (r) of circle = 15 cm Area of sector OPRQ = $\frac{60^{\circ}}{360^{\circ}} \times \pi r^{2}$

$$=\frac{1}{6} \times 3.14(15)$$

= 117.75 cm² In $\triangle OPQ$, $\angle OPQ = \angle OQP(As \text{ radius } OP = OQ)$ $\angle OPQ + \angle OQP + \angle POQ = 180^{\circ}$ $2\angle OPQ = 120^{\circ}$ $\angle OPQ = 60^{\circ}$ $\triangle OPQ$, is an equilateral triangle. Area of $\triangle OPQ = = \frac{\sqrt{3}}{4} \times (\text{Side})^2$



$$= \frac{\sqrt{3}}{4} \times (15)^2 = \frac{225\sqrt{3}}{4} \text{ cm}^2$$

= 56.25 $\sqrt{3}$
= 97.3125 cm²
Area of minor segment PRQP = Area of sector OPRQ - Area of ΔOPQ
= 117.75 - 97.3125
= 20.4375 cm²
Area of major segment PSQP = Area of circle - Area of minor segment
PRQP
= $\pi (15)^2 - 20.4375$
= 3.14 × 225 - 20.4375
= 706.5 - 20.4375
= 686.0625 cm²

Question 7:

A chord of a circle of radius 12 cm subtends an angle of 120° at the centre. Find the area of the corresponding segment of the circle. [Use $\pi = 3.14$ and $\sqrt{3} = 1.73$]

Solution 7:



Let us draw a perpendicular OV on chord ST. It will bisect the chord ST. SV = VT

In $\triangle OVS$, $\frac{OV}{OS} = \cos 60^{\circ}$ $\frac{OV}{12} = \frac{1}{2}$ OV = 6cm



 $\frac{SV}{SO} = \sin 60^{\circ} = \frac{\sqrt{3}}{2}$ $\frac{SV}{12} = \frac{\sqrt{3}}{2}$ $SV = 6\sqrt{3} \text{ cm}$ $ST = 2SV = 2 \times 6\sqrt{3} = 12\sqrt{3} \text{ cm}$ Area of $\Delta OST = \frac{1}{2} \times ST \times OV$ $= \frac{1}{2} \times 12\sqrt{3} \times 6$ $= 36\sqrt{3} = 36 \times 1.73 = 62.28 \text{ cm}^2$ Area of sector OSUT $= \frac{120^{\circ}}{360^{\circ}} \times \pi (12)^2$ $= \frac{1}{3} \times 3.14 \times 144 = 150.72 \text{ cm}^2$ Area of segment SUTS = Area of sector OSUT - Area of ΔOST = 150.72 - 62.28 $= 88.44 \text{ cm}^2$

Question 8:

A horse is tied to a peg at one corner of a square shaped grass field of side 15 m by means of a 5 m long rope (see the given figure). Find

- (i) The area of that part of the field in which the horse can graze.
- (ii) The increase in the grazing area if the rope were 10 m long instead of 5 m. [Use $\pi = 3.14$]





Solution 8:



From the figure, it can be observed that the horse can graze a sector of 90° in a circle of 5 m radius.

Area that can be grazed by horse = Area of sector OACB

$$= \frac{90^{\circ}}{360^{\circ}} \pi r^{2}$$
$$= \frac{1}{4} \times 3.14 \times (5)^{2}$$
$$= 19.625 \text{ m}^{2}$$

Area that can be grazed by the horse when length of rope is 10 m long

$$= \frac{90^{\circ}}{360^{\circ}} \times \pi \times (10)^{2}$$

= $\frac{1}{4} \times 3.14 \times 100$
= 78.5 m²
Increase in grazing area = (78.5 - 19.625) m²
= 58.875 m²

Question 9:

A brooch is made with silver wire in the form of a circle with diameter 35 mm. The wire is also used in making 5 diameters which divide the circle into 10 equal sectors as shown in figure. Find.

(i) The total length of the silver wire required.

(ii) The area of each sector of the brooch

$$\left[\text{use }\pi = \frac{22}{7}\right]$$





Solution 9:

Total length of wire required will be the length of 5 diameters and the circumference of the brooch.

Radius of circle = $\frac{35}{2}$ mm

Circumference of brooch = $2\pi r$

$$=2\times\frac{22}{7}\times\left(\frac{35}{2}\right)$$

= 110 mm Length of wire required = $110 + 5 \times 35$ = 110 + 175 = 285 mm It can be observed from the figure that each of 10 sectors of the circle is subtending 36° (i.e. $360^{\circ}/10=36^{\circ}$) at the centre of the circle.



Therefore, area of each sector $=\frac{36^{\circ}}{360^{\circ}} \times \pi r^2$

$$= \frac{1}{10} \times \frac{22}{7} \times \left(\frac{35}{2}\right) \times \left(\frac{35}{2}\right)$$
$$= \frac{385}{4} \text{ mm}^2$$

Question 10:

An umbrella has 8 ribs which are equally spaced (see figure). Assuming umbrella to be a flat circle of radius 45 cm, find the area between the two

consecutive ribs of the umbrella. $\left[\text{use } \pi = \frac{22}{7} \right]$





Solution 10:

There are 8 ribs in an umbrella. The area between two consecutive ribs is subtending $\frac{360^{\circ}}{8} = 45^{\circ}$ at the centre of the assumed flat circle.



Area between two consecutive ribs of circle $=\frac{45^{\circ}}{360^{\circ}} \times \pi r^2$

$$= \frac{1}{8} \times \frac{22}{7} \times (45)^{2}$$
$$= \frac{11}{28} \times 2025 = \frac{22275}{28} \text{ cm}^{2}$$

Question 11:

A car has two wipers which do not overlap. Each wiper has blade of length 25 cm sweeping through an angle of 115°. Find the total area cleaned at each



Solution 11:

It can be observed from the figure that each blade of wiper will sweep an area of a sector of 115° in a circle of 25 cm radius.

Area of such sector
$$=\frac{115^{\circ}}{360^{\circ}} \times \pi \times (25)^2$$



 $= \frac{23}{72} \times \frac{22}{7} \times 25 \times 25$ = $\frac{158125}{252}$ cm² Area swept by 2 blades = $2 \times \frac{158125}{252}$ = $\frac{158125}{126}$ cm²

Question 12:

To warn ships for underwater rocks, a lighthouse spreads a red coloured light over a sector of angle 80° to a distance of 16.5 km. Find the area of the sea over which the ships warned. [Use $\pi = 3.14$]





It can be observed from the figure that the lighthouse spreads light across a sector of 80° in a circle of 16.5 km radius.

Area of sector OACB =
$$=\frac{80^{\circ}}{360^{\circ}} \times \pi r^2$$

= $\frac{2}{9} \times 3.14 \times 16.5 \times 16.5$
= 189.97 km²

Question 13:

A round table cover has six equal designs as shown in figure. If the radius of the cover is 28 cm, find the cost of making the designs at the rate of Rs.0.35 per cm². [Use $\sqrt{3} = 1.7$]





Solution 13:



It can be observed that these designs are segments of the circle. Consider segment APB. Chord AB is a side of the hexagon. Each chord will substitute at $\frac{360^{\circ}}{6} = 60^{\circ}$ at the centre of the circle. In $\triangle OAB$, $\angle OAB = \angle OBA (As OA = OB)$ $\angle OAB = \angle OBA + \angle AOB = 180^{\circ}$ $2\angle OAB = 180^{\circ} - 60^{\circ} = 120^{\circ}$ $\angle OAB = 60^{\circ}$ Therefore, $\triangle OAB$ is an equilateral triangle. Area of $\triangle OAB = = \frac{\sqrt{3}}{4} \times (\text{Side})^2$ $= \frac{\sqrt{3}}{4} \times (28)^2 = 196\sqrt{3} = 196 \times 1.7 = 333.2 \text{ cm}^2$ Area of sector OAPB $= \frac{60^{\circ}}{360^{\circ}} \times \pi r^2$ $= \frac{1}{6} \times \frac{22}{7} \times 28 \times 28$ $= \frac{1232}{3} \text{ cm}^2$ Area of segment APBA = Area of sector OAPB - Area of $\triangle OAB$

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$$= \left(\frac{1232}{3} - 333.2\right) \text{cm}^{2}$$

Therefore, area of designs $= 6 \times \left(\frac{1232}{3} - 333.2\right) \text{cm}^{2}$
 $= (2464 - 1999.2) \text{ cm}^{2}$

 $= 464.8 \text{ cm}^2$

Cost of making $1 \text{ cm}^2 \text{ designs} = \text{Rs } 0.35$

Cost of making 464.76 cm² designs = $464.8 \times 0.35 = \text{Rs} \ 162.68$

Therefore, the cost of making such designs is Rs 162.68.

Question 14:

Tick the correct answer in the following:

Area of a sector of angle p (in degrees) of a circle with radius R is

(A)
$$\frac{P}{180} \times 2\pi R$$
, (B) $\frac{P}{180} \times 2\pi R^2$ (C) $\frac{P}{180} \times 2\pi R$ (D) $\frac{P}{720} \times 2\pi R^2$

Solution 14:

We know that area of sector of angle $\theta = \frac{\theta}{360^{\circ}} \times \pi R^2$

Area of sector of angle P = $\frac{P}{360^{\circ}} (\pi R^2)$

$$= \left(\frac{\mathrm{P}}{720^{\circ}}\right) \left(2\pi \mathrm{R}^2\right)$$

Hence, (D) is the correct answer.

EXERCISE NO: 12.3



Question 1:

Find the area of the shaded region in the given figure, if PQ = 24 cm, PR = 7 cm and O is the centre of the circle. use $\pi = \frac{22}{7}$



Solution 1:

It can be observed that RQ is the diameter of the circle. Therefore, \angle RPQ will be 90°

By applying Pythagoras theorem in $\triangle PQR$, RP² + PQ² = RQ²

 $(7)^2 + (24)^2 = RQ^2$ RQ = $\sqrt{625} = 25$

Radius of circle, OR = $\frac{RQ}{2} = \frac{25}{2}$

Since RQ is the diameter of the circle, it divides the circle in two equal parts.

Area of semicircle RPQOR =
$$\frac{1}{2}\pi r^2$$

$$= \frac{1}{2}\pi \left(\frac{25}{2}\right)^2$$
$$= \frac{1}{2} \times \frac{22}{7} \times \frac{625}{4}$$
$$= \frac{6875}{28} \text{ cm}^2$$

Area of $\triangle PQR = \frac{1}{2} \times PQ \times PR$

$$=\frac{1}{2} \times 24 \times 7$$

 $= 84 \,\mathrm{cm}^2$

Area of shaded region = Area of semi - circle RPQOR - Area of \triangle PQR



$$= \frac{6875}{28} - 84$$
$$= \frac{6874 - 2352}{28}$$
$$= \frac{4523}{28} \text{ cm}^2$$

Question 2:

Find the area of the shaded region in the given figure, if radii of the two concentric circles with centre O are 7 cm and 14 cm respectively and $\angle AOC$



Solution 2:



Radius of inner circle = 7 cm Radius of outer circle = 14 cm Area of shaded region = Area of sector OAFC – Area of sector OBED



$$= \frac{40^{\circ}}{360^{\circ}} \times \pi (14)^{2} == \frac{40^{\circ}}{360^{\circ}} \times \pi (7)^{2}$$
$$= \frac{1}{9} \times \frac{22}{7} \times 14 \times 14 - \frac{1}{9} \times \frac{22}{7} \times 7 \times 7$$
$$= \frac{616}{9} - \frac{154}{9} = \frac{462}{9}$$
$$= \frac{154}{3} \text{ cm}^{2}$$

Question 3:

Find the area of the shaded region in the given figure, if ABCD is a square of side 14 cm and APD and BPC are semicircles. use $\pi = \frac{22}{7}$



Solution 3:

It can be observed from the figure that the radius of each semi-circle is 7 cm.



Area of each semi-circle = $\frac{1}{2}\pi r^2$

$$=\frac{1}{2}\times\frac{22}{7}\times(7)^2$$
$$=77\,\mathrm{cm}^2$$

Area of square $ABCD = (Side)^2 = (14)^2 = 196 \text{ cm}^2$ Area of the shaded region = Area of square ABCD – Area of semi-circle APD – Area of semi-circle BPC



$$= 196 - 77 - 77 = 196 - 154 = 42 \text{ cm}^2$$

Question 4:

Find the area of the shaded region in the given figure, where a circular arc of radius 6 cm has been drawn with vertex O of an equilateral triangle OAB of

side 12 cm as centre. $\left[\text{use } \pi = \frac{22}{7} \right]$

Solution 4:

We know that each interior angle of an equilateral triangle is of measure 60°.



Area of sector OCDE = $\frac{60^{\circ}}{360^{\circ}}\pi r^2$

$$= \frac{1}{6} \times \frac{22}{7} \times 6 \times 6$$
$$= \frac{132}{7} \text{ cm}^2$$

Area of $\triangle OAB = \frac{\sqrt{3}}{4} (12)^2 = \frac{\sqrt{3} \times 12 \times 12}{4} = 36\sqrt{3} \text{ cm}^2$ Area of circle $= \pi \text{r}^2 = \frac{22}{7} \times 6 \times 6 = \frac{792}{7} \text{ cm}^2$

Area of shaded region = Area of $\triangle OAB$ + Area of circle – Area of sector OCDE



$$= 36\sqrt{3} + \frac{792}{7} - \frac{132}{7}$$
$$= \left(36\sqrt{3} + \frac{660}{7}\right) \text{cm}^2$$

Question 5:

From each corner of a square of side 4 cm a quadrant of a circle of radius 1 cm is cut and also a circle of diameter 2 cm is cut as shown in the given

figure. Find the area of the remaining portion of the square. use $\pi = \frac{22}{7}$



Solution 5:



Each quadrant is a sector of 90° in a circle of 1 cm radius.

Area of each quadrant $=\frac{90^{\circ}}{360^{\circ}}\pi r^2$

$$=\frac{1}{4}\times\frac{22}{7}\times(1)^2=\frac{22}{28}\mathrm{cm}^2$$

Area of square = $(Side)^2 = (4)^2 = 16 \text{ cm}^2$

Area of circle = $\pi r^2 = \pi (1)^2$



$$=\frac{22}{7}$$
 cm²

Area of the shaded region = Area of square – Area of circle – $4 \times$ Area of

quadrant

$$= 16 - \frac{22}{7} - 4 \times \frac{22}{28}$$
$$= 16 - \frac{22}{7} - \frac{22}{7} = 16 - \frac{44}{7}$$
$$= \frac{112 - 44}{7} = \frac{68}{7} \text{ cm}^2$$

Question 6:

In a circular table cover of radius 32 cm, a design is formed leaving an equilateral triangle ABC in the middle as shown in the given figure. Find the

area of the design (Shaded region). $\left[\text{use } \pi = \frac{22}{7} \right]$







Radius (r) of circle = 32 cm AD is the median of ABC. OA = 2/3 ADAD = 48 cmIn $\triangle ABD$,



$$AB^{2} = AD^{2} + BD^{2}$$
$$AB^{2} = (48)^{2} + \left(\frac{BC}{2}\right)^{2}$$
$$AB^{2} = (48)^{2} + \left(\frac{AB}{2}\right)^{2}$$
$$\frac{3AB^{2}}{4} = (48)^{2}$$
$$AB = \frac{48 \times 2}{\sqrt{3}} = \frac{96}{\sqrt{3}}$$
$$= 32\sqrt{3} \text{ cm}$$

Area of equilateral triangle, = $\frac{\sqrt{3}}{4} \times 32 \times 32 \times 3 = 96 \times 8 \times \sqrt{3}$ = $768\sqrt{3}$ cm²

Area of circle = πr^2

$$= \frac{22}{7} \times (32)^2$$
$$= \frac{22}{7} \times 1024$$
$$= \frac{22528}{7} \text{ cm}^2$$

Area of design = Area of circle - Area of $\triangle ABC$ = $\left(\frac{22528}{7} - 768\sqrt{3}\right)$ cm²

Question 7:

In the given figure, ABCD is a square of side 14 cm. With centres A, B, C and D, four circles are drawn such that each circle touches externally two of the remaining three circles. Find the area of the shaded region. $\left[\text{use } \pi = \frac{22}{7} \right]$





Solution 7:



Area of each of the 4 sectors is equal to each other and is a sector of 90° in a circle of 7 cm radius.

Area of each sector
$$= \frac{90^{\circ}}{360^{\circ}} \pi (7)^{2}$$
$$= \frac{1}{4} \times \frac{22}{7} \times 7 \times 7$$
$$= \frac{77}{2} \text{ cm}^{2}$$

Area of square $ABCD = (Side)^2 = (14)^2 = 196 \text{ cm}^2$ Area of shaded portion = Area of square $ABCD - 4 \times \text{Area of each sector}$



$$=196-4\times\frac{77}{2}=196-154$$

 $= 42 \text{ cm}^2$ Therefore, the area of shaded portion is 42 cm^2 .

Question 8:

The given figure depicts a racing track whose left and right ends are semicircular.



The distance between the two inner parallel line segments is 60 m and they are each 106 m long. If the track is 10 m wide, find :

(i) The distance around the track along its inner edge

(ii) The area of the track

use $\pi = \frac{22}{7}$

Solution 8:



Distance around the track along its inner edge = AB + arc BEC + CD + arc DFA

$$= 106 + \frac{1}{2} \times 2\pi r + 106 + \frac{1}{2} \times 2\pi r$$
$$= 212 + \frac{1}{2} \times 2 \times \frac{22}{7} \times 30 + \frac{1}{2} \times 2 \times \frac{22}{7} \times 30$$
$$= 212 + 2 \times \frac{22}{7} \times 30$$
$$= 212 + \frac{1320}{7}$$
$$= \frac{1484 + 1320}{7} = \frac{2804}{7} m$$



Area of the track = (Area of GHIJ – Area of ABCD) + (Area of semi-circle HKI – Area of semi-circle BEC) + (Area of semi-circle GLJ – Area of semi-circle AFD)

$$= 106 \times 80 - 106 \times 60 + \frac{1}{2} \times \frac{22}{7} \times (40)^{2} - \frac{1}{2} \times \frac{22}{7} \times (30)^{2} + \frac{1}{2} \times \frac{22}{7} \times (40)^{2} - \frac{1}{2} \times \frac{22}{7} \times (30)^{2}$$

= $106(80 - 60) + \frac{22}{7} \times (40)^{2} - \frac{22}{7} \times (30)^{2}$
= $106(20) + \frac{22}{7} [(40)^{2} - (30)^{2}]$
= $2120 + \frac{22}{7} (40 - 30) (40 + 30)$
= $2120 + (\frac{22}{7}) (10) (70)$
= $2120 + 2200$
= 4320 m^{2}

Therefore, the area of the track is 4320 m^2 .

Question 9:

In the given figure, AB and CD are two diameters of a circle (with centre O) perpendicular to each other and OD is the diameter of the smaller circle. If

OA = 7 cm, find the area of the shaded region. $\left[\text{use } \pi = \frac{22}{7} \right]$



Solution 9:





Radius (r₁) of larger circle = 7 cm Radius (r₂) of smaller circle = $\frac{7}{2}$ cm Area of smaller circle = πr_1^2

$$= \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2}$$
$$= \frac{77}{2} \text{ cm}^2$$

Area of semi-circle AECFB of larger circle $=\frac{1}{2}\pi r_2^2$

$$= \frac{1}{2} \times \frac{22}{7} \times (7)^{2}$$
$$= \frac{77}{2} \text{ cm}^{2}$$
Area of $\triangle ABC = \frac{1}{2} \times AB \times OC$
$$= \frac{1}{2} \times 14 \times 7 = 49 \text{ cm}^{2}$$

Area of the shaded region

= Area of smaller circle + Area of semi-circle AECFB – Area of \triangle ABC

$$= \frac{77}{2} + 77 - 49$$
$$= 28 + \frac{77}{2} = 28 + 38.5 = 66.5 \text{ cm}$$

Question 10:

The area of an equilateral triangle ABC is 17320.5 cm². With each vertex of the triangle as centre, a circle is drawn with radius equal to half the length of the side of the triangle (See the given figure). Find the area of shaded region. [Use $\pi = 3.14$ and $\sqrt{3} = 1.73205$]





Solution 10:

Let the side of the equilateral triangle be *a*. Area of equilateral triangle = 17320.5 cm^2

$$\frac{\sqrt{3}}{4}(a)^2 = 17320.5$$
$$\frac{1.73205}{4}a^2 = 17320.5$$
$$a^2 = 4 \times 10000$$
$$a = 200 \text{ cm}$$



Each sector is of measure 60°. Area of sector ADEF = $\frac{60^{\circ}}{360^{\circ}} \times \pi \times r^{2}$



$$= \frac{1}{6} \times \pi \times (100)^{2}$$

$$= \frac{3.14 \times 10000}{6}$$

$$= \frac{15700}{3} \text{ cm}^{2}$$
Area of shaded region = Area of equilateral triangle - 3 × Area of each sector
$$= 17320.5 - 3 \times \frac{15700}{3}$$

$$= 17320.5 - 15700 = 1620.5 \text{ cm}^{2}$$

Question 11:

On a square handkerchief, nine circular designs each of radius 7 cm are made (see the given figure). Find the area of the remaining portion of the

handkerchief. use $\pi = \frac{22}{7}$



Solution 11:





From the figure, it can be observed that the side of the square is 42 cm. Area of square = $(\text{Side})^2 = (42)^2 = 1764 \text{ cm}^2$

Area of each circle = $\pi r^2 = \frac{22}{7} \times (7)^2 = 154 \text{ cm}^2$

Area of 9 circles = $9 \times 154 = 1386$ cm²

Area of the remaining portion of the handkerchief = $1764 - 1386 = 378 \text{ cm}^2$ Question 12:

In the given figure, OACB is a quadrant of circle with centre O and radius 3.5 cm. If

OD = 2 cm, find the area of the

(i) Quadrant OACB

(ii) Shaded region

use
$$\pi = \frac{22}{7}$$



Solution 12:



(i) Since OACB is a quadrant, it will subtend 90° angle at O.

Area of quadrant OACB =
$$\frac{90^{\circ}}{360^{\circ}} \times \pi r$$

= $\frac{1}{4} \times \frac{22}{7} \times (3.5)^2 = \frac{1}{4} \times \frac{22}{7} \times \left(\frac{7}{2}\right)^2$
= $\frac{11 \times 7 \times 7}{2 \times 7 \times 2 \times 2} = \frac{77}{8} \text{ cm}^2$



(ii) Area of
$$\triangle OBD = \frac{1}{2} \times OB \times OD$$

= $\frac{1}{2} \times 3.5 \times 2$
= $\frac{1}{2} \times \frac{7}{2} \times 2$
= $\frac{7}{2}$ cm²

Area of the shaded region = Area of quadrant OACB – Area of GOBD

 $=\frac{77}{8}-\frac{7}{2}$ $=\frac{77-28}{8}$ $=\frac{49}{8}$ cm²

Question 13:

In the given figure, a square OABC is inscribed in a quadrant OPBQ. If OA = 20 cm, find the area of the shaded region. [Use $\pi = 3.14$]



Solution 13:



In $\triangle OAB$, $OB^2 = OA^2 + AB^2$



$$= (20)^{2} + (20)^{2}$$

$$OB = 20\sqrt{2}$$

Radius (r) of circle $20\sqrt{2}$ cm
Area of quadrant OPBQ $= \frac{90^{\circ}}{360^{\circ}} \times 3.14 \times (20\sqrt{2})^{2}$
 $= \frac{1}{4} \times 3.14 \times 800$
 $= 628 \text{ cm}^{2}$
Area of OABC = (Side)^{2} = (20)^{2} = 400 \text{ cm}^{2}
Area of shaded region = Area of quadrant OPBQ - Area of OABC
 $= (628 - 400) \text{ cm}^{2}$
 $= 228 \text{ cm}^{2}$

Question 14:

AB and CD are respectively arcs of two concentric circles of radii 21 cm and 7 cm and centre O (see the given figure). If $\angle AOB = 30^\circ$, find the area of the

shaded region. use
$$\pi = \frac{22}{7}$$

10.



Area of the shaded region = Area of sector OAEB - Area of sector OCFD

$$= \frac{30^{\circ}}{360^{\circ}} \times \pi \times (21)^{2} - \frac{30^{\circ}}{360^{\circ}} \times \pi \times (7)^{2}$$
$$= \frac{1}{12} \pi [(21 - 7)(21 + 7)]$$
$$= \frac{22 \times 14 \times 28}{12 \times 7}$$
$$= \frac{308}{3} \text{ cm}^{2}$$

Question 15:

In the given figure, ABC is a quadrant of a circle of radius 14 cm and a semicircle is drawn with BC as diameter. Find the area of the shaded region.



Solution:



As ABC is a quadrant of the circle, $\angle BAC$ will be of measure 90°. In $\triangle ABC$, $BC^2 = AC^2 + AB^2$

 $BC^{2} = AC^{2} + AB^{2}$ $= (14)^{2} + (14)^{2}$ $BC = 14\sqrt{2}$

Radius (r₁) of semi-circle drawn on BC = $\frac{14\sqrt{2}}{2} = 7\sqrt{2}$ cm



Area of
$$\triangle ABC = \frac{1}{2} \times AB \times AC$$

$$= \frac{1}{2} \times 14 \times 14$$

$$= 98 \text{ cm}^2$$
Area of sector $ABDC = \frac{90^{\circ}}{360^{\circ}} \times \pi r^2$

$$= \frac{1}{4} \times \frac{22}{7} \times 14 \times 14$$

$$= 154 \text{ cm}^2$$
Area of semi-circle drawn on BC $= \frac{1}{2} \times \pi \times r^2$

Area of semi-circle drawn on BC = $\frac{1}{2} \times \pi \times r_1^2 = \frac{1}{2} \times \frac{22}{7} \times (7\sqrt{2})^2$ = $\frac{1}{2} \times \frac{22}{7} \times 98 = 154 \text{ cm}^2$

Area of shaded region = Area of semi-circle on BC – (Area of sector ABDC – Area of $\triangle ABC$) = 154 – (154 – 98) = 98 cm²

Question 16:

Calculate the area of the designed region in the given figure common between the two quadrants of circles of radius 8 cm each. $\left[use \pi = \frac{22}{7} \right]$



Solution 16:



The designed area is the common region between two sectors BAEC and DAFC.



Area of sector BAEC =
$$\frac{90^{\circ}}{360^{\circ}} \times \frac{22}{7} \times (8)^{2}$$

= $\frac{1}{4} \times \frac{22}{7} \times 64$
= $\frac{22 \times 16}{7}$
= $\frac{352}{7}$ cm²
Area of $\Delta BAC = \frac{1}{2} \times BA \times BC$
= $\frac{1}{2} \times 8 \times 8 = 32$ cm²
Area of the designed portion = $2 \times (Area \text{ of segment AEC})$
= $2 \times (Area \text{ of sector BAEC} - Area \text{ of } \Delta BAC)$
= $2 \times (\frac{352}{7} - 32) = 2(\frac{352 - 224}{7})$
= $\frac{2 \times 128}{7}$
= $\frac{256}{7}$ cm²

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