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INVERSE TRIGONOMETRIC FUNCTIONS

## BASIC CONCEPTS

## INVERSE CIRCULAR FUNCTIONS

| Function | Domain | Range |  |
| :---: | :--- | :--- | :--- |
| 1. | $y=\sin ^{-1} x$ iff $x=\sin y$ | $-1 \leq x \leq 1$, | $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$ |
| 2. | $y=\cos ^{-1} x$ iff $x=\cos y$ | $-1 \leq x \leq 1$ | $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ |
| 3. | $y=\tan ^{-1} x$ iff $x=\tan y$ | $-\infty<x<\infty$ | $[0, \pi]$ |
| 4. | $y=\cot ^{-1} x$ iff $x=\cot y$ | $(-\infty,-1] \cup[1, \infty]$ | $\left[-\frac{\pi}{2} .0\right) \cup\left(0, \frac{\pi}{2}\right]$ |
| 5. | $y=\operatorname{cosec}^{-1} x$ iff $x=\operatorname{cosec} y$ | $(-\infty,-1] \cup[1, \infty]$ | $\left[0 . \frac{\pi}{2}\right) \cup\left(\frac{\pi}{2}, \pi\right]$ |
| 6. | $y=\sec ^{-1} x$ iff $x=\sec y$ |  |  |


(i) $\operatorname{Sin}^{-1} \mathrm{x} \& \tan ^{-1} \mathrm{x}$ are increasing functions in their domain.
(ii) $\operatorname{Cos}^{-1} \mathrm{x} \& \cot ^{-1} \mathrm{x}$ are decreasing functions in over domain.

## PROPERTY - I

(i) $\quad \sin ^{-1} \mathrm{x}+\cos ^{1} \mathrm{x}=\pi / 2$, for all $\mathrm{x} \in[-1,1]$

Sol. Let, $\sin ^{-1} x=\theta$
.. (i)
then, $\theta \in[-\pi / 2, \pi / 2]$
$[\because \mathrm{x} \in[-1,1]]$
$\Rightarrow \quad-\pi / 2 \leq \theta \leq \pi / 2$
$\Rightarrow-\pi / 2 \leq-\theta \leq \pi / 2$
$\Rightarrow \quad 0 \leq \frac{\pi}{2}-\theta \leq \pi$
$\Rightarrow \quad \frac{\pi}{2}-\theta \in[0, \pi]$
Now, $\sin ^{-1} \mathrm{x}=\theta$

$$
\begin{array}{ll}
\Rightarrow & \mathrm{x}=\sin \theta \\
\Rightarrow & \mathrm{x}=\cos \left(\frac{\pi}{2}-\theta\right) \\
\Rightarrow & \cos ^{-1} \mathrm{x}=\frac{\pi}{2}-\theta \\
& \{\because \mathrm{x} \in[-1,1] \text { and }(\pi / 2-\theta) \in[0, \pi]) \\
\Rightarrow \quad & \theta+\cos ^{-1} \mathrm{x}=\pi / 2 \quad \ldots(\text { ii }) \\
& \text { from (i) and (ii), we get } \\
& \sin ^{-1} \mathrm{x}+\cos ^{-1} \mathrm{x}=\frac{\pi}{2}
\end{array}
$$

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NEET Previous Year Question Paper
(ii) $\tan ^{-1} \mathrm{x}+\cot ^{-1} \mathrm{x}=\pi / 2$, for all $\mathrm{x} \in \mathrm{R}$

Sol. Let, $\tan ^{-1} x=\theta$
then, $\theta \in(-\pi / 2, \pi / 2)$
$\{\because x \in R)$
$\Rightarrow \quad-\frac{\pi}{2}<\theta<\frac{\pi}{2}$
$\Rightarrow \quad-\frac{\pi}{2}<-\theta<\frac{\pi}{2}$
$\Rightarrow \quad 0<\frac{\pi}{2}-\theta<\pi$
$\Rightarrow \quad\left(\frac{\pi}{2}-\theta\right) \in(0, \pi)$
Now, $\tan ^{-1} \mathrm{x}=\theta$
$\Rightarrow \quad \mathrm{x}=\tan \theta$
$\Rightarrow \quad \mathrm{x}=\cot (\pi / 2-\theta)$
$\Rightarrow \quad \cot ^{-1} \mathrm{x}=\frac{\pi}{2}-\theta$
$\{\because \pi / 2-\theta \in(0, \pi)\}$
$\Rightarrow \quad \theta+\cot ^{-1} \mathrm{x}=\frac{\pi}{2}$
from (i) and (ii), we get
$\tan ^{-1} \mathrm{x}+\cot ^{-1} \mathrm{x}=\pi / 2$
(iii) $\sec ^{-1}+\operatorname{cosec}^{-1} x=\frac{\pi}{2}$, for all $\mathrm{x} \in(-\infty,-1] \cup[1, \infty)$

Sol. Let, $\sec ^{-1} \mathrm{x}=\theta$
then, $\theta \in[0, \pi]-\{\pi / 2\}$
$\{\because \mathrm{x} \in(-\infty,-1] \cup[1, \infty)\}$
$\Rightarrow \quad 0 \leq \theta \leq \pi, \theta \neq \pi / 2$
$\Rightarrow \quad-\pi \leq-\theta \leq 0, \theta \neq \pi / 2$
$\Rightarrow \quad-\frac{\pi}{2} \leq \frac{\pi}{2}-\theta \leq \frac{\pi}{2}, \frac{\pi}{2}-\theta \neq 0$
$\Rightarrow \quad\left(\frac{\pi}{2}-\theta\right) \in\left[-\frac{\pi}{2}, \frac{\pi}{2}\right], \frac{\pi}{2}-\theta \neq 0$
Now, $\sec ^{-1} x=\theta$
$\Rightarrow \quad \mathrm{x}=\sec \theta$
$\Rightarrow \quad \mathrm{x}=\operatorname{cosec}(\pi / 2-\theta)$
$\Rightarrow \quad \operatorname{cosec}^{-1} \mathrm{x}=\pi / 2-\theta$

$$
\left\{\because\left(\frac{\pi}{2}-\theta\right) \in\left[-\frac{\pi}{2}, \frac{\pi}{2}\right], \frac{\pi}{2}-\theta \neq 0\right\}
$$

$\Rightarrow \quad \theta+\operatorname{cosec}^{-1} \mathrm{x}=\pi / 2$
from (i) and (ii); we get
$\sec ^{-1} x+\operatorname{cosec}^{-1} x=\pi / 2$

## PROPERTY - II

(i) $\sin ^{-1}\left(\frac{1}{x}\right)=\operatorname{cosec}^{-1} x$, for all $x \in(-\infty, 1] \cup[1, \infty)$

Sol. Let, $\operatorname{cosec}^{-1} \mathrm{x}=\theta$
then, $x=\operatorname{cosec} \theta$
$\Rightarrow \quad \frac{1}{\mathrm{x}}=\sin \theta$
$\left\{\because \mathrm{x} \in(-\infty,-1] \cup[1, \infty) \Rightarrow \frac{1}{\mathrm{x}} \in[-1,1]\{0\}\right.$
$\operatorname{cosec}^{-1} \mathrm{x}=\theta \Rightarrow \theta \in[-\pi / 2, \pi / 2]-\{0\}$
$\Rightarrow \quad \theta=\sin ^{-1}\left(\frac{1}{x}\right)$
from (i) and (ii); we get
$\sin ^{-1}\left(\frac{1}{x}\right)=\operatorname{cosec}^{-1} x$
(ii) $\cos ^{-1}\left(\frac{1}{x}\right)=\sec ^{-1} x$, for all $x \in(-\infty, 1] \cup[1, \infty)$

Sol. Let, $\sec ^{-1} \mathrm{x}=\theta$
then, $x \in(-\infty, 1] \cup[1, \infty)$ and $\theta \in[0, \pi]-\{\pi / 2\}$
Now, $\sec ^{-1} \mathrm{x}=\theta$
$\Rightarrow \quad \mathrm{x}=\sec \theta$
$\Rightarrow \quad \frac{1}{\mathrm{x}}=\cos \theta$
$\Rightarrow \quad \theta=\cos ^{-1}\left(\frac{1}{\mathrm{x}}\right)$
$\left\{\begin{array}{c}\because \mathrm{x}=(-\infty,-1] \cup[1, \infty) \\ \Rightarrow \frac{1}{\mathrm{x}} \in[-1,1]-\{0\} \text { and } \theta \in[0, \pi]\end{array}\right.$
from(i) \& (ii), we get
$\cos ^{-1}\left(\frac{1}{x}\right)=\sec ^{-1}(x)$
(iii) $\tan ^{-1}\left(\frac{1}{\mathrm{x}}\right)=\left\{\begin{array}{cc}\cot ^{-1} \mathrm{x}, & \text { for } \mathrm{x}>0 \\ -\pi+\cot ^{-1} \mathrm{x}, & \text { for } \mathrm{x}<0\end{array}\right.$

Sol. Let $\cot ^{-1} x=\theta$. Then $x \in R, x \neq 0$ and $\theta \in[0, \pi]$
Now two cases arises :
Case I: When x $>0$
In this case, $\theta \in(0, \pi / 2)$
$\therefore \quad \cot ^{-1} \mathrm{x}=\theta$
$\Rightarrow \quad \mathrm{x}=\cot \theta$
$\Rightarrow \quad \frac{1}{x}=\tan \theta$
$\theta=\tan ^{-1}\left(\frac{1}{\mathrm{x}}\right)$
from (i) and (ii), we get
$\{\because \theta \in(0, \pi / 2)\}$
$\tan ^{-1}\left(\frac{1}{x}\right)=\cot ^{-1} x$, for all $x>0$.
Case II : When $\mathrm{x}<0$
In this case $\theta \in(\pi / 2, \pi) \quad\{\because \mathrm{x}=\cot \theta<0)$
Now, $\frac{\pi}{2}<\theta<\pi$
$\Rightarrow \quad-\frac{\pi}{2}<\theta-\pi<0$
$\Rightarrow \quad \theta-\pi \in(-\pi / 2,0)$
$\therefore \quad \cot ^{-1} \mathrm{x}=\theta$
$\Rightarrow \mathrm{x}=\cot \theta$
$\Rightarrow \quad \frac{1}{x}=\tan \theta$
$\Rightarrow \quad \frac{1}{x}=-\tan (\pi-\theta)$
$\Rightarrow \quad \frac{1}{\mathrm{x}}=\tan (\theta-\pi) \quad\{\because \tan (\pi-\theta)=-\tan \theta\}$
$\Rightarrow \quad \theta-\pi=\tan ^{-1}\left(\frac{1}{x}\right) \quad\{\because \theta-\pi \in(-\pi / 2,0)\}$
$\Rightarrow \quad \tan ^{-1}\left(\frac{1}{\mathrm{x}}\right)=-\pi+\theta$
from (i) and (iii), we get

$$
\tan ^{-1}\left(\frac{1}{x}\right)=-\pi+\cot ^{-1} x \text {, if } x<0
$$

Hence,

$$
\tan ^{-1}\left(\frac{1}{x}\right)=\left\{\begin{array}{cc}
\cot ^{-1} x, & \text { for } x>0 \\
-\pi+\cot ^{-1} x, & \text { for } x<0
\end{array}\right.
$$

## PROPERTY - III

(i) $\cos ^{-1}(-\mathrm{x})=\pi-\cos ^{-1}(\mathrm{x})$, for all $\mathrm{x} \in[-1,1]$
(ii) $\sec ^{-1},(-\mathrm{x})=\pi-\sec ^{-1} \mathrm{x}$, for all $\mathrm{x} \in(-\infty,-1] \cup[1, \infty)$
(iii) $\cot ^{-1}(-x)=\pi-\cot ^{-1} x$, for all $x \in R$
(iv) $\sin ^{-1}(-\mathrm{x})=-\sin ^{-1}(\mathrm{x})$, for all $\mathrm{x} \in[-1,1]$
(v) $\tan ^{-1}(-x)=-\tan ^{-1} x$, for all $x \in R$
(vi) $\operatorname{cosec}^{-1}(-\mathrm{x})=-\operatorname{cosec}^{-1} \mathrm{x}$, for all $\mathrm{x} \in(-\infty,-1] \cup[1, \infty)$

Sol. (ii) Clearly, $-\mathrm{x} \in[-1,1]$ for all $\mathrm{x} \in[-1,1]$
let $\cos ^{-1}(-\mathrm{x})=\theta$
then, $-\mathrm{x}=\cos \theta$
$\Rightarrow \quad \mathrm{x}=-\cos \theta$
$\Rightarrow \quad \mathrm{x}=\cos (\pi-\theta)$
$\{\because \mathrm{x} \in[-1,1]$ and $\pi-\theta \in[0, \pi]$ for all $\theta \in[0, \pi]$
$\cos ^{-1} \mathrm{x}=\pi-\theta$
$\Rightarrow \quad \theta=\pi-\cos ^{-1} \mathrm{x}$
from (i) and (ii), we get
$\cos ^{-1}(-x)=\pi-\cos ^{-1} x$
Similarly, we can prove other results.
(i) Clearly, $-\mathrm{x} \in[-1,1]$ for all $\mathrm{x} \in[-1,1]$
let $\sin ^{-1}(-x)=\theta$
then, $-x=\sin \theta$

$$
\begin{array}{ll}
\Rightarrow & x=-\sin \theta  \tag{i}\\
\Rightarrow & x=\sin (-\theta) \\
\Rightarrow & -\theta=\sin ^{-1} x
\end{array}
$$

$\{\because x \in[-1,1]$ and $-\theta \in[-\pi / 2, \pi / 2]$ for all $\theta \in[-\pi / 2, \pi / 2]$
$\Rightarrow \quad \theta=-\sin ^{-1} \mathrm{x}$
from (i) and (ii), we get
$\sin ^{-1}(-x)=-\sin ^{-1}(x)$

## PROPERTY - IV

(i) $\sin \left(\sin ^{-1} \mathrm{x}\right)=\mathrm{x}$, for all $\mathrm{x} \in[-1,1]$
(ii) $\cos \left(\cos ^{-1} \mathrm{x}\right)=\mathrm{x}$, for all $\mathrm{x} \in[-1,1]$
(iii) $\tan \left(\tan ^{-1} \mathrm{x}\right)=\mathrm{x}$, for all $\mathrm{x} \in \mathrm{R}$
(iv) $\operatorname{cosec}\left(\operatorname{cosec}^{-1} \mathrm{x}\right)=\mathrm{x}$, for all $\mathrm{x} \in(-\infty,-1] \cup[1, \infty)$
(v) $\sec \left(\sec ^{-1} x\right)=x$, for all $x \in(-\infty,-1] \cup[1, \infty)$
(vi) $\cot \left(\cot ^{-1} x\right)=x$, for all $x \in R$

Sol. We know that, if $\mathrm{f}: \mathrm{A} \rightarrow \mathrm{B}$ is a bijection, then $\mathrm{f}^{-1}: \mathrm{B} \rightarrow \mathrm{A}$ exists such that fof ${ }^{-1}(y)=f\left(f^{-1}(y)\right)=y$ for all $y \in B$.

Clearly, all these results are direct consequences of this property.

Aliter : Let $\theta \in[-\pi / 2, \pi / 2]$ and $\mathrm{x} \in[-1,1]$ such that $\sin \theta=$ x.
then, $\theta=\sin ^{-1} \mathrm{x}$
$\therefore \quad \mathrm{x}=\sin \theta=\sin \left(\sin ^{-1} \mathrm{x}\right)$
Hence, $\sin \left(\sin ^{-1} \mathrm{x}\right)=\mathrm{x}$ for all $\mathrm{x} \in[-1,1]$
Similarly, we can prove other results.
Remark : It should be noted that,
$\sin ^{-1}(\sin \theta) \neq \theta$, if $\notin[-\pi / 2, \pi / 2]$. Infact, we have
$\sin ^{-1}(\sin \theta)=\left\{\begin{array}{cc}-\pi-\theta, & \text { if } \theta \in[-3 \pi / 2,-\pi / 2] \\ \theta, & \text { if } \theta \in[-\pi / 2, \pi / 2] \\ \pi-\theta, & \text { if } \theta \in[\pi / 2,3 \pi / 2] \\ -2 \pi+\theta, & \text { if } \theta \in[3 \pi / 2,5 \pi / 2]\end{array}\right.$ and so on.

Similarly,

$$
\begin{aligned}
& \cos ^{-1}(\cos \theta)=\left\{\begin{array}{cc}
-\theta, & \text { if } \theta \in[-\pi, 0] \\
\theta, & \text { if } \theta \in[0, \pi] \\
2 \pi-\theta, & \text { if } \theta \in[\pi, 2 \pi] \\
-2 \pi+\theta, & \text { if } \theta \in[2 \pi, 3 \pi]
\end{array}\right. \text { and so on. }
\end{aligned}
$$

## PROPERTY - V

(i) Sketch the graph for $\mathrm{y}=\sin ^{-1}(\sin \mathrm{x})$

Sol. As, $\mathrm{y}=\sin ^{-1}(\sin \mathrm{x})$ is periodic with period $2 \pi$.
$\therefore \quad$ to draw this graph we should draw the graph for one interval of length $2 \pi$ and repeat for entire values of x .
As we know,

or $\quad \sin ^{-1}(\sin x)=\left\{\begin{array}{cc}x, & -\frac{\pi}{2} \leq x \leq \frac{\pi}{2} \\ \pi-x, & \frac{\pi}{2} \leq x \leq \frac{3 \pi}{2},\end{array}\right.$
which is defined for the interval of length $2 \pi$, plotted as ;


Thus, the graph for $\mathrm{y}=\sin ^{-1}(\sin \mathrm{x})$, is a straight line up and a straight line down with slopes 1 and -1 respectively lying between $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$.

## Noto

Students are adviced to learn the definition of $\sin ^{-1}(\sin x)$ as,

$$
y=\sin ^{-1}(\sin x)=\left\{\begin{array}{ccc}
x+2 \pi & ;-\frac{5 \pi}{2} \leq x \leq-\frac{3 \pi}{2} \\
-\pi-x & ; & -\frac{3 \pi}{2} \leq x \leq-\frac{\pi}{2} \\
x & ; & -\frac{\pi}{2} \leq x \leq \frac{\pi}{2} \\
\pi-x & ; & \frac{\pi}{2} \leq x \leq \frac{3 \pi}{2} \\
x-2 \pi & ; & \frac{3 \pi}{2} \leq x \leq \frac{5 \pi}{2}
\end{array} \quad \ldots\right. \text { and so on }
$$

(ii) Sketch the graph for $\mathrm{y}=\cos ^{-1}(\cos \mathrm{x})$.

Sol. As, $\mathrm{y}=\cos ^{-1}(\cos \mathrm{x})$ is periodic with period $2 \pi$.
$\therefore$ to draw this graph we should draw the graph for one interval of length $2 \pi$ and repear for entire values of $x$ of length $2 \pi$.
As we know;
$\cos ^{-1}(\cos x)=\left\{\begin{array}{cc}x ; & 0 \leq x \leq \pi \\ 2 \pi-x ; & 0 \leq 2 \pi-x \leq \pi,\end{array}\right.$
or $\quad \cos ^{-1}(\cos x)=\left\{\begin{array}{cc}x ; & 0 \leq x \leq \pi \\ 2 \pi-x ; & \pi \leq x \leq 2 \pi,\end{array}\right.$
Thus, it has been defined for $0<x<2 \pi$ that has length $2 \pi$. So, its graph could be plotted as;


Thus, the curve $y=\cos ^{-1}(\cos x)$.
(iii) Sketch the graph for $\mathrm{y}=\tan ^{-1}(\tan \mathrm{x})$.

Sol. As $\mathrm{y}=\tan ^{-1}(\tan \mathrm{x})$ is periodic with period $\pi$.
$\therefore \quad$ to draw this graph we should draw the graph for one interval of length $\pi$ and repeat for entire values of $x$.

As we know; $\tan ^{-1}(\tan x)=\left\{x ;-\frac{\pi}{2}<x<\frac{\pi}{2}\right\}$

Thus, it has been defined for $-\frac{\pi}{2}<x<\frac{\pi}{2}$ that has length $\pi$.
So, its graph could be plotted as;


Thus, the curve for $\mathrm{y}=\tan ^{-1}(\tan \mathrm{x})$, where y is not defined for $x \in(2 n+1) \frac{\pi}{2}$.

## FORMULAS

(i) $\tan ^{-1} x+\tan ^{-1} y=\tan ^{-1} \frac{x+y}{1-x y}, x y<1$
(ii) $\tan ^{-1} x-\tan ^{-1} y=\tan ^{-1} \frac{x-y}{1+x y}, x y>-1$
(iii) $2 \tan ^{-1} x=\tan ^{-1} \frac{2 x}{1-x^{2}},|x|<1$
(iv) $2 \tan ^{-1} \mathrm{x}=\sin ^{-1} \frac{2 \mathrm{x}}{1+\mathrm{x}^{2}},|\mathrm{x}| \leq 1$
(v) $2 \tan ^{-1} \mathrm{x}=\cos ^{-1} \frac{1-\mathrm{x}^{2}}{1+\mathrm{x}^{2}}, \mathrm{x} \geq 0$
(vi) $\sin ^{-1} x+\sin ^{-1} y=\sin ^{-1}\left(x \sqrt{1-y^{2}}+y \sqrt{1-x^{2}}\right)$
(vii) $\sin ^{-1} x-\sin ^{-1} y=\sin ^{-1}\left(x \sqrt{1-y^{2}}-y \sqrt{1-x^{2}}\right)$
(viii) $\cos ^{-1} x+\cos ^{-1} y=\cos ^{-1}\left(x y-\sqrt{1-x^{2}} \sqrt{1-y^{2}}\right)$
(ix) $\cos ^{-1} x-\cos ^{-1} y=\cos ^{-1}\left(x y+\sqrt{1-x^{2}} \sqrt{1-y^{2}}\right)$
(x) If $\tan ^{-1} x+\tan ^{-1} y+\tan ^{-1} z=\tan ^{-1}$
$\left[\frac{x+y+z-x y z}{1-x y-y z-z x}\right]$ if, $x>0, y>0, z>0 \&$
$x y+y z+z x<1$

## Note:

(i) If $\tan ^{-1} x+\tan ^{-1} y+\tan ^{-1} z=\pi$ then $x+y+z=x y z$
(ii) If $\tan ^{-1} x+\tan ^{-1} y+\tan ^{-1} z=\frac{\pi}{2}$ then $x y+y z+z x=1$

## REMEMBERTHAT:

(i) $\sin ^{-1} x+\sin ^{-1} y+\sin ^{-1} z=\frac{3 \pi}{2} \Rightarrow \quad x=y=z=1$
(ii) $\cos ^{-1} \mathrm{x}+\cos ^{-1} \mathrm{y}+\cos ^{-1} \mathrm{z}=3 \pi \mathrm{x}=\mathrm{y}=\mathrm{z}=-1$
(iii) $\tan ^{-1} 1+\tan ^{-1} 2+2 \tan ^{-1} 3=$ $\tan ^{-1} 1+\tan ^{-1} \frac{1}{2}+\tan ^{-1} \frac{1}{3}=\frac{\pi}{2}$

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