

41

# GATE MECHANICAL 2019 ENGINEERING

B

# **Detailed Solution**

EXAM DATE: 02-02-2019 MORNING SESSION (09:30 AM-12:30 PM)

### Office Address

**DELHI:** F-126, Katwaria Sarai, New Delhi - 110 016 **Ph:** 011-41013406, Mobile: 8130909220, 9711853908

NOIDA: B-23 A, 5th Floor, Gaurav Deep Heights, Near Fortis Hospital Sector 62, Noida- 201305 Ph: 0120 415 1100

Web: www.iesmaster.org | E-mail: info@iesmaster.org



# **GATE 2019** Detailed Solution

02-02-2019 | MORNING SESSION

- 1. John Thomas, an \_\_\_\_\_ writer, passed away in 2018.
  - (a) imminent (b) dominant
  - (c) eminent (d) prominent

#### Ans. (c)

- 2. The minister avoided any mention of the issue of women's reservation in the private sector. He was accused of \_\_\_\_\_ the issue.
  - (a) collaring (b) belting
  - (c) tying (d) skirting

#### Ans. (d)

- **3.** The sum and product of two integers are 26 and 165 respectively. The difference between these two integers is \_\_\_\_\_.
  - (a) 4 (b) 2
  - (c) 6 (d) 3

#### Ans. (a)

Sol. Prime factorisation of

 $165 = 3 \times 5 \times 11$ 

165 = 15 × 11

So the two numbers whose sum is 26 and multiplication is 165 is 15 and 11

difference = 15 - 11

= 4

Option (a) 4 is correct

- I permitted him to leave, I wouldn't have had any problem with him being absent \_\_\_\_\_\_\_\_\_
  I?
  - (a) Have, would (b) Have, wouldn't
  - (c) Had, would (d) Had, wouldn't

#### Ans. (c)

5. A worker noticed that the hour hand on the factory clock had moved by 225 degrees during her stay at the factory. For how long did she stay in the factory ?

- (a) 8.5 hours
- (b) 3.75 hours
- (c) 4 hours and 15 minutes

Ans. (d)

**Sol.**  $\therefore$  360° = 12 hours

$$1^\circ = \frac{12}{360}$$
 hours

$$225^{\circ} = \frac{12 \times 225}{360} \text{ hours}$$

= 7.5 hours

Option (d) 7.5 hours is correct

- A person divided an amount of Rs. 100,000 into two parts and invested in two different schemes. In one he got 10% profit and in the other he got 12%. If the profit percentages are interchanged with these investments he would have got Rs. 120 less. Find the ratio between his investments in the two schemes.
  - (a) 9:16 (b) 47:53
  - (c) 11:14 (d) 37:63

#### Ans. (b)

#### Sol.

Let first part = x So second part = 100,000 - x According to question

$$\begin{bmatrix} 0.1x + 0.12(100,000 - x) \end{bmatrix} \\ - \begin{bmatrix} 0.12x + 0.1(100,000 - x) \end{bmatrix} = 120 \\ 0.2x - 0.24x + 1200 - 1000 = 120 \\ -0.04x = -1880 \\ x = 47000 \\ x & 47000 & 47 \end{bmatrix}$$

$$\frac{x}{100,000 - x} = \frac{47000}{53000} = \frac{47}{53}$$



- 7. Under a certain legal system, prisoners are allowed to make one statement. If their statement turns out to be true then they are hanged. If the statement turns out to be false then they are shot. One prisoner made a statement and the judge had no option but to set him free. Which one of the following could be that statement ?
  - (a) I committed the crime
  - (b) You committed the crime
  - (c) I will be shot
  - (d) I did not commit the crime

#### Ans. (c)

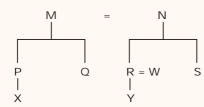
Sol.

If prisoner make the statement "I wil be shot" then only judge have no option and prisoner will be freeze so option (3) I will be shot is correct choice

- 8. M and N had four children P, Q, R and S. Of them, only P and R were married. They had children X and Y respectively. If Y is a legitimate child of W, which one of the following statements is necessarily FALSE ?
  - (a) R is the father of Y
  - (b) W is the wife of R
  - (c) M is the grandmother of Y
  - (d) W is the wife of P

Ans. (d)

Sol.



From the family tree option (d) W is the wife of P can'not possible

So option (d) W is the wife of  ${\sf P}$  is correct choice

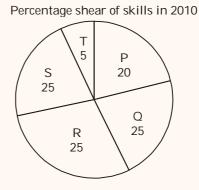
9. Congo was named by Europeans. Congo's dictator Mobuto later changed the name of the country and the river to Zaire with the objective of Africanising names of persons and spaces. However, the name Zaire was a Portuguese alteration of Nzadi o Nzere, a local African term meaning 'River that swallows Rivers'. Zaire was the Portuguese name for the Congo river in the 16th and 17 centuries.

Which one of the following statements can be inferred from the paragraph above ?

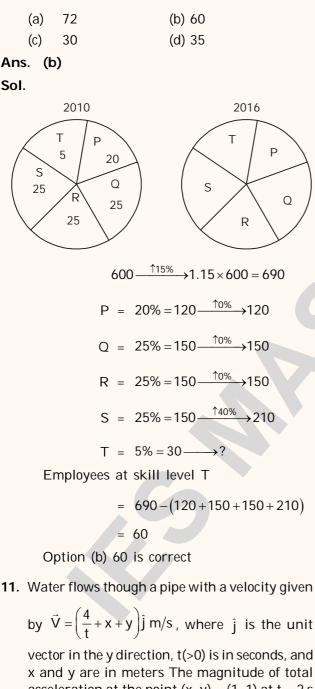
- (a) The term Nzadi o Nzere was of Portuguese origin
- (b) As a dictator Mobuto ordered the Portuguese to alter the name of the river to Zaire
- (c) Mobuto's desire to Africanise names was prevented by the Portuguese
- (d) Mobuto was not entirely successful in Africanising the name of his country

#### Ans. (d)

**10.** A firm hires employees at five different skill levels P, Q, R, S, T. The shares of employment at these skill levels of total employment in 2010 is given in the pie chart as shown. There were a total of 600 employees in 2010 and the total employment increased by 15% from 2010 to 2016. The total employment at skill levels P, Q and R remained unchanged during this period. If the exmployment at skill level S increased by 40% from 2010 to 2016, how many employees were there at skill level T in 2016 ?







x and y are in meters The magnitude of total acceleration at the point (x, y) = (1, 1) at t = 2 s is \_\_\_\_\_ m/s<sup>2</sup>.

 $\overline{V} = \left(\frac{4}{t} + x + y\right)\hat{j}\frac{m}{s}$ 

Ans. (3)

Sol.

# GATE 2019 Detailed Solution

MF

02-02-2019 | MORNING SESSION

- $\overline{V} = u\hat{i} + v\hat{i} + w\hat{k}$ u = 0, w = 0 $V = \left(\frac{4}{t} + x + y\right)\hat{j}$  $\vec{a} = \vec{a}_x \hat{i} + \vec{a}_y \hat{j} + \vec{a}_z \hat{k}$  $\vec{a}_x = u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial v} + w \frac{\partial u}{\partial z} + \frac{\partial u}{\partial t} = 0$  $\vec{a}_z = u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} + \frac{\partial w}{\partial t} = 0$  $\vec{a}_y = u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} + \frac{\partial v}{\partial z}$  $= V \frac{\partial V}{\partial V} + \frac{\partial V}{\partial t}$  $=\left(\frac{4}{t}+x+y\right)\times1+\left(-\frac{4}{t^2}\right)$  $\vec{a}_y = \left(\frac{4}{t} + x + y - \frac{4}{t^2}\right)\hat{j}$ At (x,y) = 1,1 and t = 2 sec. Total acceleration  $\vec{a} = \vec{a}_y = \left(\frac{4}{2} + 1 + 1 - \frac{4}{4}\right) = 3\frac{m}{s^2}$ 12. A spur gear with 20° full depth teeth is transmitting 20 kW at 200 rad/s. The pitch circle diameter of the gear is 100 mm. The magnitude of the force applied on the gear in the radial direction is
  - (a) 0.36 kN (b) 2.78 kN
  - (c) 0.73 kN (d) 1.39 kN

Ans. (c)

Sol.  $\phi = 20^{\circ}$ 

P = 20 kW, w = 200 rad/s PCD = 100 mm



 $F_r = ?$ 

 $F\cos\phi = F_{+}$ 

 $Fsin\phi = F_r$ 

## GATE 2019 Detailed Solution 02-02-2019 | MORNING SESSION

IM E

(a)	510	(b) 530
(c)	536.67	(d) 490

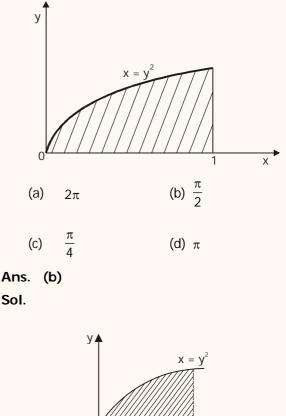
#### Ans. (a)

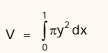
Sol. Three month moving average.

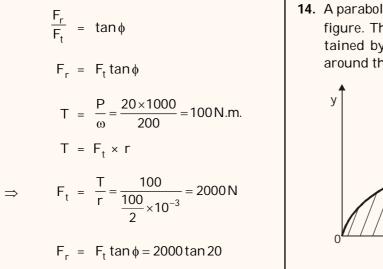
Forecast of the product for the month of september

$$\mathsf{F} = \frac{495 + 475 + 560}{3} = 510$$

**14.** A parabola  $x = y^2$  with  $0 \le x \le 1$  is shown in the figure. The volume of the solid of rotation obtained by rotating the shaded area by 360° around the x-axis is







- = 727.9 N
- = 0.73 kN
- **13.** The table presents the demand of a product. By simple three-months moving average method, the demand-forecast of the product for the month of September is

Month	Demand
January	450
February	440
March	460
April	510
May	520
June	495
July	475
August	560



$$V = \int_{0}^{1} \pi x \, dx$$
$$= \frac{\pi x^{2}}{2} \Big|_{0}^{1} = \frac{\pi}{2}$$

- **15.** As per common design practice, the three types of hydraulic turbines, in descending order of flow rate, are
  - (a) Pelton, Francis, Kaplan
  - (b) Francis, Kaplan, Pelton
  - (c) Pelton, Kaplan, Francis
  - (d) Kaplan, Francis, Pelton

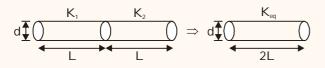
#### Ans. (d)

- Sol. In descending order of flow rate. Kaplan > Francis > Pelton
- **16.** A slender rod of length L, diameter d (L >> d) and thermal conductivity  $k_1$  is joined with another rod of identical dimensions, but of thermal conductivity  $k_2$ , to form a composite cylindrical rod of length 2L. The heat transfer in radial direction and contact resistance are negligible. The effective thermal conductivity of the composite rod is

(a) 
$$\frac{2k_1k_2}{k_1 + k_2}$$
 (b)  $\sqrt{k_1k_2}$   
(c)  $\frac{k_1k_2}{k_1 + k_2}$  (d)  $k_1 + k_2$ 

Ans. (a)

Sol.



Heat transfer in radial direction and contact resistance are negligible.

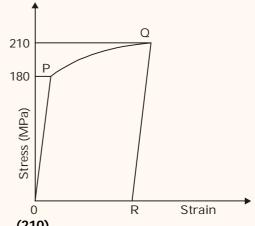
Series connection

# GATE 2019 Detailed Solution

02-02-2019 | MORNING SESSION

$$(R_{th})_{eq} = R_1 + R_2$$
$$\frac{2L}{A K_{eq}} = \frac{L}{A K_1} + \frac{L}{A K_2}$$
$$\frac{2}{K_{eq}} = \frac{1}{K_1} + \frac{1}{K_2}$$
$$\left(K_{eq} = \frac{2K_1 K_2}{K_1 + K_2}\right)$$

**17.** Consider the stress-strain curve for an ideal elastic-plastic strain hardening metal as shown in the figure. The metal was loaded in uniaxial tension starting from O. Upon loading, the stress-strain curve passes through initial yield point at P, and then strain hardens to point Q, where the loading was stopped. From point Q, the specimen was unloaded to point R, where the stress is zero. If the same specimen is reloaded in tension from point R, the value of stress t which the material yields again is \_\_\_\_\_ MPa.



#### Ans. (210)

**Sol.** As the point loaded beyond the yield point is unloaded completely and reloaded then because of strain hardening (residual strain remains in body) increase the yield strength.

In this case material with start yielding from point 'R' instead of 'P'.



# Take Your Preparation for ESE I GATE | PSUs to the Next Level



Announcing Regular and Weekend Batches

Batches starting from

DEL	DELHI		
Regular Batch	Weekend Batch	Weekend Batch	
15 <sup>th</sup> Feb (Morning)	16 <sup>th</sup> Feb	16 <sup>th</sup> Feb	
18 <sup>th</sup> Feb (Evening)			
		Register Now	

F-126 Katwaria Sarai New Delhi-110016 80100 09955 B-23 A Behind Fortis Hospital Sector 62, Noida- 201305 0120 415 1100 ME

CE

EE

ECE



#### 18. During a high cycle fatigue test, a metallic specimen is subjected to cyclic loading with a mean stress of +140 MPa, and a minimum stress of -70 MPa. The R-ratio (minimum stress to maximum stress) for this cycle loading is \_\_\_\_\_ (round off to one decimal place).

Sol.

 $\sigma_{mean}$  = + 140 MPa

$$\sigma_{min}$$
 = - 70 MPa

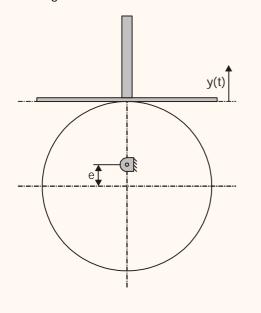
$$\sigma_{\text{mean}} = \frac{\sigma_{\text{max}} + \sigma_{\text{min}}}{2} = 140$$

$$\frac{\sigma_{\text{max}} - 70}{2} = 140$$

$$\sigma_{\text{max}} = 350 \text{ MPa}$$

$$\frac{\sigma_{\text{min}}}{\sigma_{\text{max}}} = \frac{-70}{350} = -0.2$$

19. A flat-faced follower is driven using a circular eccentric cam rotating at a constant angular velocity  $\omega$ . At time t = 0, the vertical position of the follower is y(0) = 0, and the system is in the configuration shown below.



## **GATE 2019 Detailed Solution** 02-02-2019 | MORNING SESSION

The vertical position of the follower face, y(t) is given by

(a) esinωt (c)

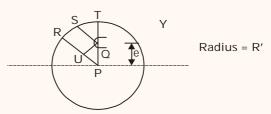
(b)  $e(1 + \cos 2\omega t)$ 

esin2ωt

(d)  $e(1 - \cos \omega t)$ 

Ans. (d)

Sol.



As the follower starts moving, the displacement Y can be shown as marked in the diagram

PR = R'

Υ

 $PU = e\cos\theta$  $\Rightarrow$ 

QT = (R' - e)from geometry Putting the above values in equation (i)

$$Y = e(1 - \cos \theta)$$
$$Y = (1 - \cos \omega t)$$

**20.** For the equation  $\frac{dy}{dx} + 7x^2y = 0$ , if y(0) = 3/7,

then the value of y(1) is

(a) 
$$\frac{3}{7}e^{-7/3}$$
 (b)  $\frac{3}{7}e^{-3/7}$   
(c)  $\frac{7}{3}e^{-3/7}$  (d)  $\frac{7}{3}e^{-7/3}$ 

Ans. (a)

**Sol.** 
$$\frac{dy}{dx} + 7x^2y = 0$$
,  $y(0) = \frac{3}{7}$ ,  $y(1) = ?$ 



$$\frac{dy}{dx} = -7x^{2}y$$

$$\frac{dy}{y} = -7x^{2} dx$$

$$lny = -\frac{7x^{3}}{3} + C$$

$$y = e^{-\frac{7x^{3}}{3} + C}$$

$$y(0) = e^{c} = \frac{3}{7}$$

$$C = ln\left(\frac{3}{7}\right)$$

$$lny = -\frac{7x^{3}}{3} + ln\left(\frac{3}{7}\right)$$

$$ny - ln\left(\frac{3}{7}\right) = -\frac{7x^{3}}{3}$$

$$ln\left(\frac{7y}{3}\right) = -\frac{7x^{3}}{3}$$

$$y = \frac{3}{7}e^{-\frac{7x^{3}}{3}}$$

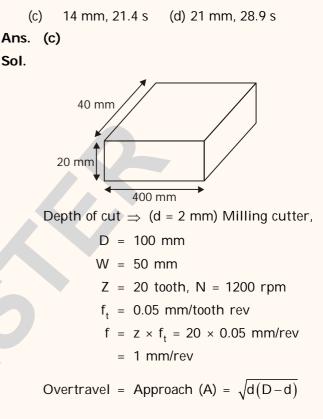
$$y(1) = \frac{3}{7}e^{-7/3}$$

21. The length, width and thickness of a steel sample are 400 mm, 410 mm, 40 mm and 20 mm, respectively. Its thickness needs to be uniformly reduced by 2 mm in a single pass by using horizontal slab miling. The miling cutter (diameter: 100 mm, width; 50 mm) has 20 teeth and rotates at 1200 rpm. The feed per tooth is 0.05 mm. The feed direction is along the length of the sample. If the over-travel distance is the same as the approach distance, the approach distance and time taken to complete the required machining task are :

(a) 21 mm, 39.4 s (b) 14 mm, 18.4 s

## **GATE 2019 Detailed Solution** 02-02-2019 | MORNING SESSION

Sol.



 $= \sqrt{2 \times (100 - 2)} = 14 \,\mathrm{mm}$ 

Total length covered by tool

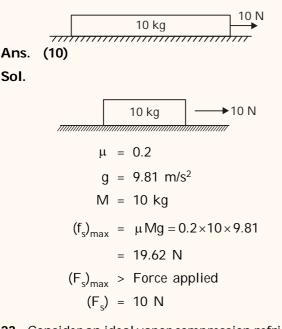
 $L + 2A = 400 + 2 \times 14 = 428 \text{ mm}$ Time for one pass,

$$t = \frac{L}{fN}$$

$$= \frac{428}{1 \times \left(\frac{1200}{60}\right)} = 21.4 \, \text{sec}$$

22. A block mass 10 kg rests on a horizontal floor. The acceleration due to gravity is 9.81 m/s<sup>2</sup>. The coefficient of static friction between the floor and the block is 0.2. A horizontal force of 10 N is applied on the block as shown in the figure. The magnitude of force of friction (in N) on the block is \_\_\_\_\_.

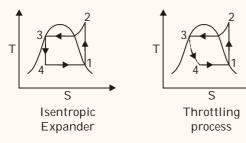




- **23.** Consider an ideal vapor compression refrigeration cycle. If the throttling process is replaced by an isentropic expansion process, keeping all the other processes unchanged, which one of the following statements is true for the modified cycle ?
  - (a) Coefficient of performance is higher than that of the original cycle.
  - (b) Coefficient of performance is the same as that of the original cycle.
  - (c) Coefficient of performance is lower than that of the original cycle.
  - (d) Refrigerating effect is lower than that of the original cycle.

#### Ans. (a)

Sol. V-C-R-S cycle



## GATE 2019 MI Detailed Solution 02-02-2019 | MORNING SESSION

Both cycle required same amount of work input but by use of Isentropic expander, we can get more amount of refrigeration effect, hence

$$\left(\left(\mathsf{COP}\right)_{\mathsf{modified cycle}} > \left(\mathsf{COP}\right)_{\mathsf{original cycle}}\right)$$

**24.** Consider the matrix :

$$\mathbf{P} = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$$

The number of distinct eigenvalues of P is : (a) 3 (b) 0

Ans. (c)

**Sol.** 
$$|\mathbf{P} - \lambda \mathbf{I}| = \begin{vmatrix} 1 - \lambda & 1 & 0 \\ 0 & 1 - \lambda & 1 \\ 0 & 0 & 1 - \lambda \end{vmatrix}$$

$$(1-\lambda)[(1-\lambda)(1-\lambda)-0] = 0$$
$$\lambda = 1.1.1$$

No. of distinct eigen value = 1.

25. For a hydrodynamically and thermally fully developed laminar flow through a circular pipe of constant cross-section. The Nusselt number at constant wall heat flux (Nu<sub>q</sub>) and that at constant wall temperature (Nu<sub>τ</sub>) are related as

(a) 
$$Nu_q = Nu_T$$
 (b)  $Nu_q = (Nu_T)^2$ 

(c) 
$$Nu_q < Nu_T$$
 (d)  $Nu_q > Nu_T$ 

Ans. (d)

**Sol.**  $(Nu)_q$  for constant wall heat flux and  $(N_u)_T$  at constant wall temperature for a hydrodynamically and thermally fully developed laminar flow through a circular



# **CONVENTIONAL QUESTION PRACTICE PROGRAM** for ESE - 2019 Mains Exam

#### **Cash Prize COMPLETE PACKAGE** for Top 10 **Classroom Program Conventional Test Series** 16 includes includes Subject-wise tests 11 Mixed Topic-wise & 6 Full-length tests RANK 2<sup>nd</sup> **Conventional Test Series Classroom Program** ₹2500/-3<sup>rd</sup> ₹2000/-4<sup>th</sup> ₹1500/-5<sup>th</sup> 5<sup>th</sup> 17<sup>th</sup> March | Every Sunday 18<sup>th</sup> Feb | Monday to Saturday 250-300 hrs 8:30 am to 2:30 pm a) New Topics b) Revision Topics Subject wise Practice, Discussion and Test Classroom Solutions + Discussion Practice Booklets with Solution Outlines Improve Question Selection Ability How to Write Answer- Test & Counselling Session Cover all Concepts in Various Topics Discussion and Practice Session of 250-300 hrs Improve Time Management Under Guidance of Mr. Kanchan Kr. Thakur Under Simulated Classroom Exam Env.

Unique Approach : Test on New Topics

+ Revision Topics

Course	Branch	Fees (₹)
Complete Package (Classroom Program + Conventional Test Series) for Non IES Master Students	CE	18000/-
Complete Package (Classroom Program + Conventional Test Series) for Ex- IES Master Students	CE	15000/-
Conventional Classroom Program (For Non IES Master Students)	CE	16000/-
Conventional Classroom Program (For Ex- IES Master Students)	CE	13000/-
Conventional Classroom Program (For Current year IES Master Classroom Program Students)	CE	11000/-
Conventional Offline Test Series (For Non IES Master Students)	CE, ME, EE, ECE	5000/-
Conventional Offline Test Series (For Ex-IES Master Students)	CE, ME, EE, ECE	5000/-
Conventional Offline Test Series (For Current year IES Master Classroom Program Students)	CE, ME, EE, ECE	Free
Conventional Online Test Series (For All Students)	CE, ME, EE, ECE	3000/-

Students can also pay online

#### HOW TO APPLY

Students can register by making payments in person with Cash/DD at our office located at

F-126, Katwaria Sarai, New Delhi - 110016

#### from 9 am to 8:30 pm

For Query 8010009955 9711853908

ENROLL NOW

www.iesmaster.org



### ESE-2019 Conventional Test Schedule, Mechanical Engineering

Date	Торіс			
	N.T. : TH-1, TH-2, HT-1, RAC-1, MS-1, MS-2			
17th Mar 2019	R.T. :			
24th Mar 2019	N.T. : FMM-1, RAC-2, IE-2, RSE-1			
2401 Wai 2013	R.T. : TH-2, MS-1, HT-1			
31st Mar 2019	N.T. : MECH-1, MECH-2, HT-2, RE-1			
	R.T. : RAC-1, RAC-2, MS-2			
07th Apr 2019	N.T.: FMM-2, PPE-1,RSE-2			
	R.T. : HT-1, HT-2, TH-1, FMM-1, IE-2			
14th Apr 2019	N.T.: ICE-1,ToM-2, MR-1			
	<b>R.T.</b> : FMM-2, RSE-1, RSE-2, PPE-1			
21st Apr 2019	N.T. : ToM-1, MR-2, PROD-1			
	<b>R.T.</b> : MS-1, MECH-1, MECH-2,TH-1			
28th Apr 2019	<b>N.T.</b> : IE-1, PPE-2, FMM-3,			
	R.T. : PPE-1, MS-2, HT-1, PROD-1, ToM-1, ICE-1			
05th May 2019	N.T.: PPE-3, PROD-2			
	R.T. : RAC-1, RAC-2, RE-1, IE-1, MR-1, MECH-1			
12th May 2019	1ay 2019 N.T. : ToM-3, ICE-2			
	R.T. : MR-2, RSE-1, RSE-2, HT-1, HT-2, FMM-2			
19th May 2019	N.T.: RE-2, MD-1			
	<b>R.T.</b> : PPE-1, PPE-2, FMM-3, ToM-2, ToM-3			
26th May 2019	N.T.: Mech-3, MD-2			
02ad lup 2010	<b>R.T.</b> FMM-1, FMM-2, PROD-1, PROD-2, MECH-1, ICE-2, MD-1 Full Length-1 (Test Paper-1 + Test Paper-2)			
02nd Jun 2019	Full Length-2 (Test Paper-1 + Test Paper-2)			
09th Jun 2019				
16th Jun 2019	Full Length-3 (Test Paper-1 + Test Paper-2)			
	est Type Timing onventional Test 10:00 A.M. to 1:00 P.M.			
	onventional Full Length Test Paper-1 10:00 A.M. to 1:00 P.M.			
	onventional Full Length Test Paper-2 02:00 P.M. to 5:00 P.M.			
Noto , The timine	e of the test may change on cartain dates. Driver information will be given in this regard			

Note : The timing of the test may change on certain dates. Prior information will be given in this regard. \***N.T.** : New Topic. \***R.T.** : Revision Topic Call us : 8010009955, 011-41013406 or Mail us : info@iesmaster.org

	Subject Code Details					
	TH-1			TH-2		
Thermodynamic	Zeroth, First and Second Laws of The	Thermodynamic systems and processes; Zeroth, First and Second Laws of Thermodynamics. properties of pure substance.				
	HT-1			HT-2		
Heat Transfer	Steady and unsteady heat condu Radiative heat transfer		Free and force	d convection, boiling and condensation, Heat exchanger.		
	ICE-1			ICE-2		
IC Engines	SI and CI Engines, Engine Systems and (	Components, Fuels.		naracteristics and testing of IC Engines; ssion Control. Otto, Diesel and Dual Cycles.		
	RAC-1	RAC-1		RAC-2		
Refrigeration Air Conditioning	Vapour compression refrigeration, Compressors, Other types of refrigeration Absorption, Vapour jet, thermo electric refrigeration and Heat put	systems like Vapour and Vortex tube	Psychometric properties and processes, Comfort chart, Comfort and industrial air conditioning, Load calculations and Condensers, Evaporators and Expansion devices.			
	FMM-1	FM	M-2	FMM-3		
Fluid Mechanics and Machinery	Basic Concepts and Properties of Fluids, Manometry, Fluid Statics, Buoyancy, Equations of Motion such as velocity potential, Stream Function.	Viscous flow of inc Laminar and Turbule	n and applications, compressible fluids, nt flows, Flow through l losses in pipes.	Reciprocating and Centrifugal pumps, Hydraulic Turbines and other hydraulic machines.		
	PPE-1	PP	'E-2	PPE-3		
Power Plant Engineering	Steam and Gas Turbines, Rankine and Brayton cycles with regeneration and reheat.	analysis, Theory Pulse jet and R	roperties, Flue gas of Jet Propulsion – am Jet Engines, Rotary Compressors.	Boilers, power plant components like condensers, air ejectors, Electrostatic precipitators and cooling towers.		
	RSE-1			RSE-2		
Renewable Sources of Energy	Flat Plate andfocusing collectors their materials and performance. Solar Thermal Energy Storage Applications		Bio-mass and T	c Conversion; Harnessing of Wind Energy, idal Energy – Methods and Applications, king principles of Fuel Cells.		
Engineering	Mech-1	Me	ch-2	Mech-3		
Mechanics (SoM)	Analysis of System of Forces, Friction, Centroid and Centre of Gravity, Dynamics.	and Strains, Ben	-Compound Stresses ding Moment and e Diagrams.	Theory of Bending Stresses-Slope and deflection-Torsion, Thin and thick Cylinders, Spheres.		
	MS-1			MS-2		
Engineering Materials	Basic Crystallography, Alloys ar diagrams, Heat Treatmer		Basics of Nand	Ferrous and Non Ferrous Metals, Non metallic materials, Basics of Nano-materials, Mechanical Properties and Testing, Corrosion prevention and control.		
	ToM-1	То	M-2	ToM-3		
Mechanisms and Machines	Mechanisms, Kinematic Analysis, Velocity and Acceleration. CAMs with uniform acceleration, cycloidal motion, oscillatingfollowers; Effect of Gyroscopiccouple on automobiles, ships and aircrafts. Governors.		d damped SDOF ibility Ratio, Vibration	Geometry of tooth profiles, Law of gearing, Interference, Helical, Spiral and Worm Gears, Gear Trains- Simple, compound and Epicyclic. Slider crank mechanisms, Balancing.		
	MD-1			MD-2		
Design of Machine Elements	Design for static and dynamic loading; fatigue strength and the S-N diagram; princi machine elements such as riveted, welder	iples of the design of		ars, rolling and sliding contact bearings, kes and clutches, flywheels.		
	PROD-1	IE	-1	RE-1		
Manufacturing, Industrial and	Metal casting-Metal forming, Metal Joining, computer Integrated manufacturing, FMS.	Inventor	ning and Control, ry control	Failure concepts and characteristics- Reliability, Failure analysis, Machine Vibration, Data acquisition, Fault Detection, Vibration Monitoring.		
Maintenance	PROD-2	IE	-2	RE-2		
Engineering	Machining and machine tool operations, Limits, fits and tolerances, Metrology and inspection.	Operations resea	arch - CPM-PERT	Field Balancing of Rotors, Noise Monitoring, Wear and Debris Analysis, Signature Analysis, NDT Techniques in Condition Monitoring.		
	MR-1 MR-2					
Mechatronics and Robotics	Microprocessors and Micro controllers: Archit I/O,Computer interfacing, Programmable log and actuators, Piezoelectric accelerometer Optical Encoder, Resolver, Inductosyn, Pner actuators, stepper motor, Control Systems- M of Physicalsystems, control signals, controllar	ic controller. Sensors r, Hall effect sensor, umatic and Hydraulic lathematical modeling	Robotics, Robot Classification, Robot Specification, notation     Direct and Inverse Kinematics; Homogeneous Coordinates a     Arm Equation of four Axis SCARA Robot.     ng			



pipe of constant cross-section is 4.36 and 3.66 respectively. Hence,

(b) blister

 $(Nu)_q > (Nu)_T$ 

- 26. In a casting process, a vertical channel through which molten metal flows downward from pouring basin to runner for reaching the model cultivate is called
  - (a) riser
  - (c) pin hole (d) sprue

#### Ans. (d)

27. The position vector  $\overrightarrow{OP}$  of point P(20, 10) is rotated anti-clockwise in X-Y plane by an angle  $\theta = 30^{\circ}$  such that point P occupies position Q, as shown in the figure. The coordinates (x, y) of Q are

(a) 
$$(12.32, 18.66)$$
 (b)  $(18.66, 12.32)$   
(c)  $(22.32, 8.26)$  (d)  $(13.40, 22.32)$ 

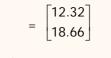
Ans. (a)

Sol.

$${}^{1}P = {}^{2}T_{1} {}^{2}P, \text{ rotates anticlockwise}$$
$$\begin{bmatrix} x'\\y' \end{bmatrix} = \begin{bmatrix} \cos\theta & -\sin\theta\\\sin\theta & \cos\theta \end{bmatrix} \begin{bmatrix} x\\y \end{bmatrix}$$
$$\begin{bmatrix} x'\\y' \end{bmatrix} = \begin{bmatrix} \cos30 & -\sin30\\\sin30 & \cos30 \end{bmatrix} \begin{bmatrix} 20\\10 \end{bmatrix}$$
$$= \begin{bmatrix} 0.866 & -0.5\\0.5 & 0.866 \end{bmatrix} \begin{bmatrix} 20\\10 \end{bmatrix}$$
$$\begin{bmatrix} x'\\y' \end{bmatrix} = \begin{bmatrix} 0.866 \times 20 - 0.5 \times 10\\0.5 \times 20 + 0.866 \times 10 \end{bmatrix}$$

# GATE 2019 ME Detailed Solution

02-02-2019 | MORNING SESSION



(x', y') = (12.32, 18.66)

28. A solid cube of side 1 m is kept at a room temperature of 32° C. The coefficient of linear thermal expansion of the cube material is 1×10<sup>-5</sup>/ °C and the bulk modulus is 200 GPa. If the cube is constrained all around and heated uniformly to 42°C, then the magnitude of volumetric (mean) stress (in MPa) induced due to heating is \_\_\_\_\_.

Ans. (60)

Sol.

a = 1 m  $T_a = 32^{\circ}C, \ \alpha = 1 \times 10^{-5} / {^{\circ}C}$  K = 200 GPa  $\Delta T = 10^{\circ}C$   $\epsilon_v = \frac{(1-2\mu)}{E}(3\sigma) = 3\alpha T$ 

As  $\sigma_1 = \sigma_2 = \sigma_3 = \sigma$ 

(mean volumetric stress)

$$\sigma \frac{(1-2\mu)}{E} = \alpha \Delta T \qquad E = 3K(1-2\mu)$$

$$\sigma = \frac{E\alpha\Delta T}{1-2\mu} \qquad \qquad \frac{E}{1-2\mu} = 3K$$



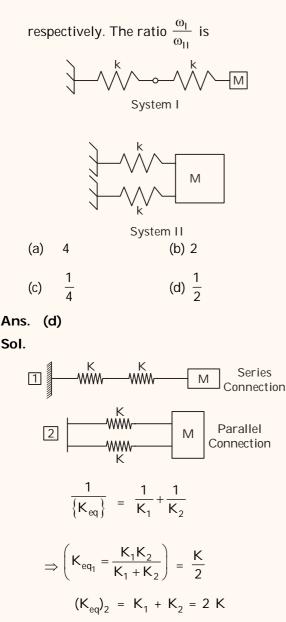


 $\sigma = 3 K \alpha \Delta T$ 

$$= 3 \times 200 \times 10^3 \times 1 \times 10^{-5} \times 10$$

 $\sigma$  = 60 MPa

**29.** The natural frequencies corresponding to the spring-mass system I and II are  $\omega_{I}$  and  $\omega_{II}$ ,



Natural frequency  $\left(\omega = \sqrt{\frac{K}{m}}\right)$ 

$$\frac{\omega_1}{\omega_2} = \frac{\sqrt{\frac{K}{2m}}}{\sqrt{\frac{2K}{m}}} = \frac{1}{2}$$

- **30.** The lengths of a large stock of titanium rods follow a normal distribution with a mean  $(\mu)$  of 440 mm and a standard deviation  $(\sigma)$  of 1 mm. What is the percentage of rods whose lengths lie between 438 mm and 441 mm?
  - (a) 68.4% (b) 99.75%
  - (c) 81.85% (d) 86.64%

Ans. (c)

Sol.

u = 440 mm $\sigma = 1 \text{mm}$  $Z = \frac{X - u}{\pi}$ 

lower limit,

$$Z(x = 438) = \frac{438 - 440}{1} = -2$$

$$440$$

$$438$$

$$438$$

$$441$$

$$441$$

$$z = -2$$

$$z = 1$$

$$Z(x = 441 \text{ mm}) = \frac{441 - 440}{1} = -2$$

Percentage of rods whose lengths lie between 438 mm and 441 mm.

= 0.3413 + (0.5 - 0.0228) = 0.81854 = 81.854%

**31.** Air of mass 1 kg. initially at 300 K and 10 bar, is allowed to expand isothermally till it reaches



a pressure of 1 bar. Assuming air as an ideal gas with gas constant of 0.287 kJ/kg K, the change in entropy of air (in kJ/kg K, round off to two decimal places) is \_\_\_\_\_.

#### Ans. (0.66)

#### Sol.

Air, m = 1 kg T = 300K P<sub>1</sub> = 10 bar R = 0.287 kJ/kg k  $\Delta s = mc_p \ell n \left( \frac{T_p}{T_1} \right)^{\circ} - mR \ell n \left( \frac{P_2}{P_1} \right)$   $= -1 \times 0.287 \ell n \left( \frac{1}{10} \right)$ 

= 0.66 kJ/kg k

- **32.** Which one of the following welding methods provides the highest heat flux (W/mm<sup>2</sup>)?
  - (a) Tungsten inert gas welding
  - (b) Laser beam welding
  - (c) Oxyacetylene gas welding
  - (d) Plasma arc welding

#### Ans. (b)

**33.** A cylindrical rod of diameter 10 mm and length 1.0 m fixed at one end. The other end is twisted by angle of 10° by applying a torque. If the maximum shear strain in the rod is p×10<sup>-3</sup>, then p is equal to \_\_\_\_\_\_ (round off to two decimal places).

Ans. (0.87)

Sol.

$$\theta = 10^{\circ}$$
  
d=10mm L = 1000mm

Torsion equation

# GATE 2019 Detailed Solution

02-02-2019 | MORNING SESSION

$$\frac{T}{J} = \frac{T_{max}}{R_0 \text{ or } R} = \frac{G\theta}{L}$$
$$\frac{T_{max}}{G} = \gamma_{max} = \frac{R\theta}{L} = \frac{5 \times 10 \times \frac{\pi}{180}}{1000}$$
$$= 0.87 \times 10^{-3}$$
$$p = 0.87$$

**34.** Evaluation of  $\int_{2}^{x^{3}} dx$  using a 2-equal-segment trapezoidal rule gives value of \_\_\_\_\_.

Ans. (63)

Sol.

Trapezoidal Rule, h = 1

$$\int y dx = \frac{h}{2} \Big[ (y_0 + y_1) + 2(y_1 + y_2 + \dots) \Big]$$
$$= \frac{1}{2} \Big[ (2^3 + 4^3) + 2(3^3) \Big]$$
$$= \frac{1}{2} \Big[ 8 + 64 + 54 \Big] = 63$$

**35.** During a non-flow thermodynamic process (1-2) executed by a perfect gas, the heat interaction is equal to the work interaction  $(Q_{1,2} = W_{12})$  when the process is

(a) Adiabatic (b) Polytropic

(c) Isothermal (d) Isentropic

Ans. (c)

Sol.

For isothermal process

As per 1st law of thermodynamics

$$\delta \theta = \delta \theta + \delta w$$

$$\overline{\delta \theta = \delta w}$$

36. A project consists of six activities. The immedi-



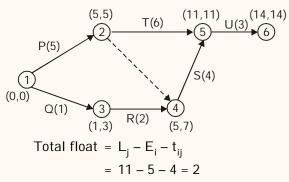
ate predecessor of each activity and the estimated duration is also provided in the table below :

	-	
Activity	Immediate	Estimated duration
Activity	predecessor	(weeks)
Р	-	5
Q	-	1
R	Q	2
S	P,R	4
Т	Р	6
U	S,T	3

If all activities other than S take the estimated amount of time, the maximum duration (in weeks) of the activity S without delaying the completion of the project is \_\_\_\_\_.

#### Ans. (6)

Sol.



Maximum duration of activity S, without delaying the completion of project = Total float + activity time = 2 + 4 = 6

37. Consider an elastic straight beam of length

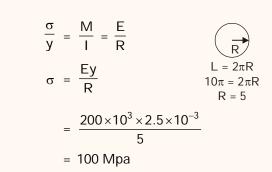
L = 10  $\pi$  m, with square cross-section of side a = 5 mm, and Young's modulus E = 200 GPa. This straight beam was bent in such a way that the two ends meet, to form a circle of mean radius R. Assuming that Euller-Bernoulli beam theory is applicable to this bending problem, the maximum tensile bending stress in the bent beam is \_\_\_\_\_ MPa.



Ends of the beam

Ans. (100)

Sol.



38. In ASA system, the side cutting and end cutting edge angles of a sharp turning tool are 45° and 10°, respectively. The feed during cylindrical turning is 0.1 mm/rev. The center line average surface roughness (in μm, round off to one decimal place) of the generated surface is \_\_\_\_\_.

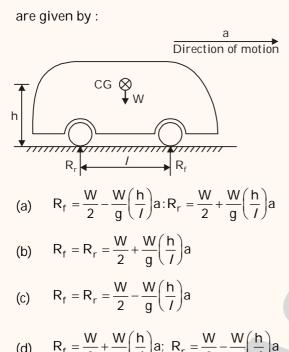
Ans. (3.7)

Sol.

$$R_{a} = \frac{f}{4(\tan C_{s} + \cot C_{E})}$$
$$= \frac{0.1}{4(\tan 45 + \cot 10)}$$
$$= 3.7 \times 10^{-3} \text{ mm}$$
$$\boxed{R_{a} = 3.7 \mu \text{m}}$$

**39.** A car having weight W is moving in the direction as shown in the figure. The center of gravity (CG) of the car is located at height h from the ground, midway between the front and rear wheels. The distance between the front and rear wheels is *I*. The acceleration of the car is a, and acceleration due to gravity is g. The reaction on the front wheels (R<sub>r</sub>) and rear wheels (R<sub>r</sub>)





(d) 
$$R_f = \frac{4}{2} + \frac{4}{g} \left(\frac{1}{I}\right) a; R_r = \frac{4}{2} - \frac{4}{g} \left(\frac{1}{I}\right) a$$

Ans. (a)

Sol.

$$h \underbrace{F_{inertia} \leftarrow CG}_{W} \underbrace{F_{inertia} = \frac{Wa}{g}}_{A \uparrow R_{r}} \underbrace{F_{r}}_{I}$$

$$\sum M_A = 0, F_{inertia} \times h + R_f \times \ell - W \times \frac{\ell}{2} = 0$$

$$R_{f} = \frac{\frac{W\ell}{2} - h \times \frac{w_{a}}{g}}{\ell}$$
$$R_{f} = \frac{W}{2} - \frac{W}{g} \left(\frac{h}{\ell}\right) a$$

$$\sum f_{y} = 0 \quad W = R_{f} + R_{r}$$
$$R_{r} = \frac{W}{2} + \frac{W}{g} \left(\frac{h}{\ell}\right) a$$

#### **GATE 2019** ME **Detailed Solution** 02-02-2019 | MORNING SESSION

**40.** Taylor's tool life equation is given by  $VT^n = C_i$ where V is in m/min and T is in min. In a turning operation, two tools X and Y are used. For tool X, n = 0.3 and C = 60 and for tool Y, n = 0.6and C = 90. Both the tools will have the same tool life for the cutting speed (in m/min, round off to one decimal place) of \_\_\_\_\_.

#### Ans. (40)

Sol.

 $VT^n = c$ 

for Tool X,	for Tool y
$VT^{0.3} = 60$	$VT^{0.6} = 90$

Velocity when both tools have same tool life.

$$\frac{T^{0.3}}{T^{0.6}} = \frac{60}{90}$$

$$(T)^{0.3-0.6} = \frac{6}{9}$$

$$T^{0.3} = 1.5$$

$$T = (1.5)^{1/0.3} \text{ min}$$

$$V = \frac{60}{(1.5)^{0.3/0.3}} = 40 \text{ m/min}.$$

41. A uniform thin disk of mass 1 kg and radius 0.1 m is kept on a surface as shown in the figure. The spring of stiffness  $k_1 = 400$  N/m is connected to the disk center A and another spring of stiffness  $k_2 = 100$  N/m is connected at point B just above point A on the circumference of the disk. Initially, both the springs are unstretched. A assume pure rolling of the disk. For small disturbance from the equilibrium, the natural frequency of vibration of the system is \_\_\_\_\_ rad/ s (round off to one decimal place).



## SUBJECT-WISE IMPROVEMENT PROGRAM

**Complete Guidance in Small Packs** 

SESSION 2019-20 ESE/GATE/PSUs for ME, EE, ECE

Starts from 18<sup>th</sup> February

> FREE Enrolment in GS <u>Batch</u>

> > with any Subject

Improvement

Package

ENROLL NOW

Aiming for ESE, GATE & PSUs, but require expert guidance only for a few selected subjects? Be a part of Subject-wise Improvement Program, a classroom study program designed exclusively for you.

**Program Benefits** 

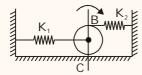
- Customise study package as per requirement
- Save time and energy for self-study
- In-depth understanding of concepts
- Expert guidance and quality study material
- Improve semester grade while ESE & GATE preparation

F-126, Katwaria Sarai, New Delhi-110016 (C) 80 1000 9955, 011 4101 3406 iesmaster.org



Ans. (23.1) Sol.

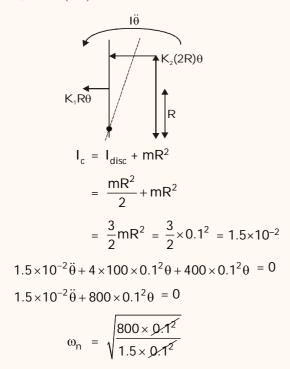
m = 1 kg, R = 0.1m  
$$K_1 = 400 \text{ N/m}, K_2 = 100 \text{ N/m}$$



Assme pure rolling of the disc

$$M_c = 0$$
 at I.C. at point (C)

$$I_{c}\ddot{\theta} + K_{2}(2R)\theta \times 2R + K_{1}R\theta \times R = 0$$

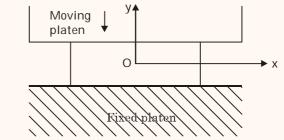


 $\omega_n = 23.1$ 

**42.** A plane-strain compression (forging) of a block is shown in the figure. The strain in the z-direction is zero. The yield strength  $(S_y)$  in uniaxial tension/compression of the material of the block is 300 MPa and it follows the Tresca (maximum shear stress) criterion. Assume that the entire block has started yielding. At a point

where  $\sigma_x$  = 40 MPa (compressive) and  $\tau_{xy}$  = 0 ,

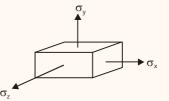
#### the stress component $\sigma_y$ is



- (a) 260 MPa (compressive)
- (b) 260 MPa (tensile)
- (c) 340 MPa (tensile)
- (d) 340 MPa (compressive)
- Ans. (d)

Sol. Plain strain compression (Forging)

 $\sigma_x, \sigma_y \& \sigma_z$  are pricipal stress



under plane strain condition,  $\in_z = 0$ 

$$\Rightarrow \frac{\sigma_z}{E} - \frac{\mu \sigma_y}{E} - \frac{\mu \sigma_x}{E} = 0$$
$$\Rightarrow \sigma_z = \mu (\sigma_x + \sigma_y)$$
but  $\sigma_x = -40$ 



# MASTER TALENT REWARD EXAM (MTRE) A National Level Online Scholarship Test



- Opportunity to get up to 100% off on tuition fee
- Chance to study with the best engineering minds
- 🕳 Learn in a stress-free environment
- Know your ranking at national level

To get the most out of the MTRE, visit iesmaster.org/master-talent-reward-exam

Email: mtre@iesmaster.org

Registrations

Open

F-126, Katwaria Sarai, New Delhi - 110016 | Call 80100 09955, 011 4101 3406 Email info@iesmaster.org



# GATE 2019 Detailed Solution



02-02-2019 | MORNING SESSION

$$\Rightarrow \sigma_z = \mu (-40 + \sigma_y)$$

Assuming,  $(\mu = 0.5)$  at yielding condition.

$$\sigma_z = 0.5(-40 + \sigma_y), \sigma_y, \sigma_x = -40$$

As per Tresca (Maximum shear stress) criterion.

$$\frac{S_{yt}}{2} = \max\left[\left|\frac{\sigma_{x} - \sigma_{y}}{2}\right|, \left|\frac{\sigma_{y} - \sigma_{z}}{2}\right|, \left|\frac{\sigma_{z} - \sigma_{x}}{2}\right|\right]$$

$$\Rightarrow \frac{300}{2} = \left[\frac{\left|40 + \sigma_{y}\right|}{2}, \frac{\left|0.5\sigma_{y} + 20\right|}{2}, \frac{\left|0.5\sigma_{y} + 20\right|}{2}\right]$$

$$\frac{0.5\sigma_y + 20}{2} = \pm \frac{300}{2}$$

 $\sigma_y = +560 \text{ MPa}, -640 \text{ MPa}$ 

$$\frac{\sigma_y + 40}{2} = \pm \frac{300}{2}$$

σ<sub>y</sub> = + 260 MPa, – 340 MPa

As block is under compression in y-direction,

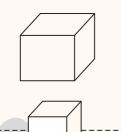
hence, 340 Mpa compression is the correct option.

**43.** A cube of side 100 mm is placed at the bottom of an empty container on one of its faces. The density of the material of the cube is 800 kg/m<sup>3</sup>. Liquid of density 1000 kg/m<sup>3</sup> is now poured into the container. The minimum height to which the liquid needs to be poured into the container for the cube to just lift up is \_\_\_\_\_ mm.

#### Ans. (80)

Sol.

a = 100mm



Minimum height to which the liquid needs to be poured into the container for the cube to just lift up, hence

 $F_B \ge (mg)_{block}$ 

$$\begin{split} \rho_f g V_{fd} &\geq \left( \rho V \right)_{block} \times g \\ 1000 \times 0.1 \times 0.1 \times h &\geq 800 \times 0.1 \times 0.1 \times 0.1 \end{split}$$

 $h \ge 0.08m$ 

 $h \ge 80mm$ 

**44.** In a UTM experiment, a sample of length 100 mm, was loaded in tension until failure. The failure load was 40 kN. The displacement, measured using the cross-head motion, at failure, was 15 mm. The compliance of the UTM is constant and is given by 5×10<sup>8</sup> m/N. The strain at failure in the sample is \_\_\_\_\_%.

#### Ans. (2)

**Sol.** Compliance is the ratio of load point deflection and applied load.

JTM constant = 
$$\frac{\Delta L}{P} = C$$

As per Hooke's law, 
$$\frac{\sigma}{c} = E$$

or, 
$$\frac{\frac{P}{A}}{\frac{\Delta L}{L}} = E$$





 $\Rightarrow \frac{\mathsf{PL}}{\mathsf{A}\Delta\mathsf{L}} = \mathsf{E}$ 

or,  $\frac{\Delta L}{P} = \frac{L}{AE} = UTM \text{ constant} = C$ 

Now, L = 100 mm,  $\Delta L$  = 15 mm, C = 5 × 10<sup>-8</sup> m/N, P = 40 kN

Strain =  $\frac{\Delta L}{L} = \frac{P}{AE} = \frac{P}{L/C}$ =  $\frac{PC}{L} = \frac{40 \times 10^3 \times 5 \times 10^{-8}}{100 \times 10^{-3}} = 2 \times 10^{-2}$  $\therefore$  Strain in % = 2 × 10<sup>-2</sup> × 100% = 2%

**45.** In orthogonal turning of a cylindrical tube of wall thickness 5mm, the axial and the tangential cutting forces were measured at 1259 N and 1601 N, respectively. The measured chip thickness after machining was found to be 0.3 mm. The rake angel was 10° and the axial feed was 100 mm/min. The rotational speed of the spindle was 1000 rpm. Assuming the material to be perfectly plastic and Merchant's first solution, the shear strength of the martial is closest to

Ans. (c)

Sol.

N = 1000 rpm, 
$$\alpha$$
 = 10  
f = 100 mm/min  
=  $\frac{100}{1000} \frac{mm}{rev}$   
f =  $0.1 \frac{mm}{rev}$  = t  
r =  $\frac{t}{t_c} = \frac{0.1}{0.3} = \frac{1}{3}$   
F<sub>s</sub> =  $\tau_s \times \frac{bt}{\sin \phi}$ 

 $\Rightarrow \tau_{s} = \frac{F_{s} \sin \phi}{6 \times t}$   $\tan \phi = \frac{r \cos \alpha}{1 - r \sin \alpha}$   $\Rightarrow \phi = 19.19^{\circ}$   $F_{s} = F_{c} \cos \phi - F_{t} \sin \phi$   $= 1601 \times \cos 19.19^{\circ} - 1259 \sin 19.19$  = 1098.20 N  $\tau_{s} = \frac{1098.20 \times \sin 19.19^{\circ}}{5 \times 0.1}$  = 721.96  $\approx 722 \text{ Mpa}$ 

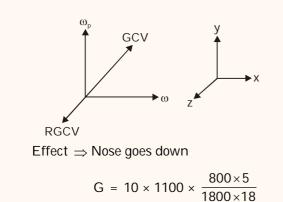
- **46.** The rotor of turbojet engine of an aircraft has a mass 180 kg and polar moment of inertia 10 kg.m<sup>2</sup> about the rotor axis. The rotor rotates at a constant speed of 1100 rad/s in the clockwise direction when viewed from the front of the aircraft. The aircraft while flying at a speed of 800 km per hour takes a turn with a radius of 1.5 km to the left. The gyroscopic moment exerted by the rotor on the aircraft structure and the direction of motion of the nose when the aircraft turns, are
  - (a) 1629.6 N.m and the nose goes up
  - (b) 162.9 N.m and the nose goes up
  - (c) 162.9 N.m and the nose goes down
  - (d) 1629.6 N.m and the nose goes down

#### Ans. (d) Sol.

$$G = I\omega\omega_p$$

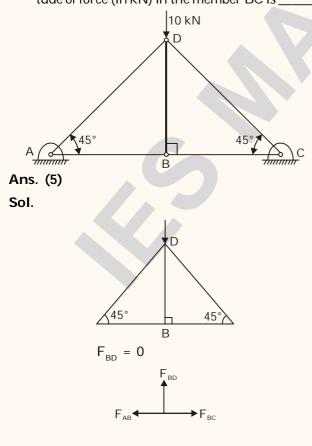
Aircraft





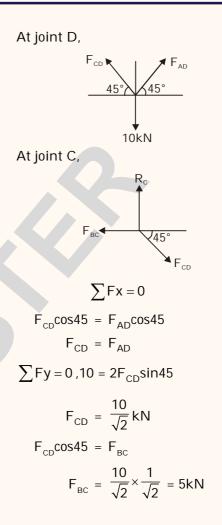
= 1629.63 Nm G = 1629.63 N.m

47. A truss is composed of members AB, BC, CD, AD and BD as shown in the figure. A vertical load of 10 kN is applied at point D. The magnitude of force (in kN) in the member BC is

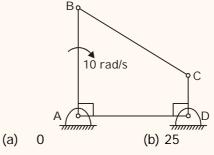


### **GATE 2019** ME **Detailed Solution**

02-02-2019 | MORNING SESSION



**48.** In a four bar planar mechanism shown in the figure, AB = 5 cm, AD = 4 cm and DC = 2 cm. In the configuration shown, both AB and DC are perpendicular to AD. The bar AB rotates with an angular velocity of 10 rad/s. The magnitude of angular velocity (in rad/s) of bar DC at this instant is



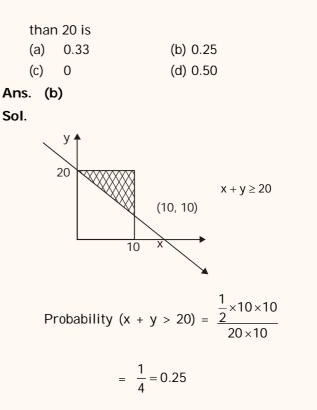


# GATE 2019 Detailed Solution

02-02-2019 | MORNING SESSION

(d) 15 (c) 10 Ans. (b) Sol. AB = 4cmAD = 4cmCD = 2cm $\omega_{\Delta B} = 10 \text{ rad/s}$  $\omega_2(I_{24}I_{12}) = \omega_4(I_{24}I_{14})$ <sup>2</sup><sub>24</sub> <sup>21, 14</sup> 23, 34 8 + 2x = 5x8 = 3x $x = \frac{8}{2}$  $10(x + 4) = \omega \times x$  $10\left(\frac{8}{3}+4\right) = \omega \times \frac{8}{3}$  $10 \times \frac{20}{2} \times \frac{3}{9} = \omega$ 

- $\omega = \frac{200}{8} = 25 \text{ rad/s}$
- 49. The variable x takes a value between 0 and 10 with uniform probability distribution. The variable y takes a value between 0 and 20 with uniform probability distribution. The probability of the sum of variables (x + y) being greater



**50.** The wall of a constant diameter pipe of length 1 m is heated uniformly with flux q" by wrapping a heater coil around it. The flow at the inlet to the pipe is hydrodynamically fully developed. The fluid is incompressible and the flow is assumed to be laminar and steady all through the pipe. The bulk temperature of the fluid is equal to 0°C at the inlet and 50°C at the exit. The wall temperatures are measured at three locations, P, Q and R as shown in the figure. The flow thermally develops after some distance from the inlet. The following measurements are made :

Point	Р	Q	R
Wall Temp(°C)	50	80	90



# Railway Recruitment Board Junior Engineers (RRB-JE)



# IES Master Announces Classroom Course and Online Test Series RRB-JE 2019

# 1<sup>st</sup> stage CBT

Batches starts from 25<sup>th</sup> Feb

# **Classroom Course**

Subjects Covered:

- Mathematics
- General Intelligence & Reasoning
  - General Awareness
    - General Science

Online Test Series FREE with Classroom Course

Starts from 23<sup>rd</sup> Feb

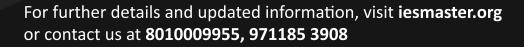
# **Online Test Series**

- 12 Topic-wise
- 4 Subject-wise
- 8 Mixed Subjects Tests
  - 6 Full Length Tests

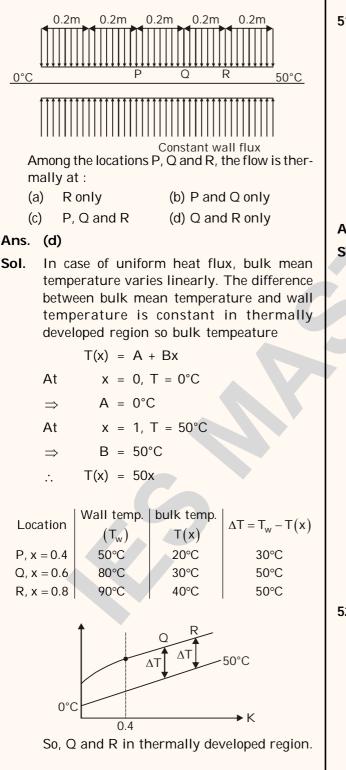
Total: 30 Tests

**Enroll Now** 

Classroom Program and Online Test Series for RRB-JE 2nd Stage CBT to be announced soon.







- **51.** A harmonic function is analytic if it satisfies the Laplace equation. If  $u(x, y) = 2x^2 - 2y^2 + 4xy$ is a harmonic function, then its conjugate harmonic function v (x, y) is
  - (a)  $4y^2 4xy + constant$
  - (b)  $4xy 2x^2 + 2y^2 + constant$
  - (c)  $2x^2 2y^2 + xy + constant$

(d) 
$$-4xy+2y^2-2x^2+constant$$

Ans. (b)

ol. 
$$u(x,y) = 2x^2 - 2y^2 + 4xy$$

 $u_{x} = V_{y}$   $u_{y} = -V_{x}$   $u_{x} = 4x + 4y$   $u_{y} = -4y + 4x$   $\frac{\partial V}{\partial y} = V_{y} = 4x + 4y$   $V = 4xy + 2y^{2} + f(x)$   $\frac{\partial V}{\partial x} = 4y + f'(x) = 4y - 4x$  f'(x) = -4x  $f(x) = -2x^{2} + C$   $V = 2y^{2} - 2x^{2} + 4xy + C$ 

**52.** A steam power cycle with regeneration as shown below on the T-s diagram employs a single open feedwater heater for efficiency improvement. The fluids mix with each other in an open feedwater heater. The turbine is isentropic and the input (bleed) to the feedwater heater from the turbine is at state 2 as shown in the figure. Process 3-4 occurs in the condenser. The pump work is negligible. The in-



# GATE 2019 Detailed Solution

put to the boilder is at state 5. The following information is available from the steam tables .

State	1	2	3	4	5	6
Enthalpy(kJ/kg)	3350	2800	2300	175	700	1000
T 4	5				2	
S						

The mass flow rate of steam bled from the turbine as a percentage of the total mass flow rate at the inlet to the turbine at state 1 is \_\_\_\_\_.

#### Ans. (20)

Sol.

 $xh_{2} + (1 - x)h_{4} = h_{5}$   $x \times 2800 + (1 - x) \times 175 = 700$ x = 0.2

20% of mass flow rate of steam bled from the turbine of total mass flow rate.

53. If one mole of  $H_2$  gas occupies a rigid container with a capacity of 1000 liters and the temperature is raised from 27°C to 37°C, the change in pressure of the contained gas (round off to two decimal places), assuming ideal gas behavior, is \_\_\_\_\_ Pa. (R = 8.314 J/mol.K).

#### Ans. (83.14)

T<sub>1</sub>

Sol.

n = 1, H<sub>2</sub> gas (Rigid container) V = 1000 It = 1m<sup>3</sup> v v v

= 1000 It = 1m<sup>3</sup> 
$$V_1 = V_2$$
  
= 27°C R = 8.314 J/mol k

 $T_{2} = 37^{\circ}C$ 

Change in pressure, 
$$(P_2 - P_1)$$
 Pa  
PV = nRT  
 $P_1V_1 = nRT_1$   
 $P_1 = \frac{nRT_1}{V_1}$   
 $\Delta P = \frac{nRT_2}{V_2} - \frac{nRT_1}{V_1}$   
 $= \frac{nR}{V}[T_2 - T_1]$   
 $= \frac{1 \times 8.314}{1} \times 10$   
 $\Delta P = 83.14$  Pa

54. A circular shaft having diameter  $65.00^{+0.01}_{-0.05}$  mm

is manufactured by turning process. A  $_{50\mu m}$  thick coating of TiN is deposited on the shaft Allowed variation in TiN film thickness is  $\pm 5\,\mu m$ . The minimum hole diameter (in mm) to just provide clearance fit is

Sol.

50 µm thick coating

Shaft = 
$$65^{+0.01}_{-0.05}$$
 mm

$$t = (50 \pm 5) \mu m$$

To proivde clearnace

$$\left(\mathsf{D}_{\mathsf{H}}\right)_{\mathsf{min}} \geq \left(\left(\mathsf{D}\right)_{\mathsf{shaft}}\right)_{\mathsf{max}}$$

$$\geq (D_s)_{max} + 2t_{max}$$

$$= 65.01 + \frac{2 \times 55}{1000} = 65.12$$
mm

55. The set of equations



	x + y + z = 1	
6	a - ay + 3z = 5	
5	x - 3y + az = 6	
h	as infinite solution, if	a =
(2	a) -4	(b) 3
(C	:) 4	(d) -3
Ans.	(c)	
Sol.		
	$\rho(A) = \rho(AB) < \text{no.} c$	of variables
	A  = 0	
	1 1 1	
	$\begin{vmatrix} 1 & 1 & 1 \\ a & -a & 3 \\ 5 & -3 & a \end{vmatrix} = 0$	
	(-a <sup>2</sup> + 9) - (a <sup>2</sup> - 15) +	(–3a + 5a) = 0
	9 – a² + 15 – a² + 2a =	= 0
	$2a^2 - 2a - 24 = 0$	
	$a^2 - a - 12 = 0$	
	$a^2 - 4a + 3a - 12 = 0$	
	(a = 4, -3)	
	ho(AB) < (No. of varia)	ble)
	1 1 1	
	$\begin{vmatrix} 1 & 1 & 1 \\ -a & 3 & 5 \\ 2 & a & 6 \end{vmatrix} = 0$	
	$ -3 \ d \ 0 $	15 + 1 + 2 + 0 = 0
	1(18 – 5a) – 1 (–6a +	
	18 - 5a - 15 + 6a + 9	$-a^{2}=0$
	$a^2 - a - 12 = 0$	
	a = 3, 4 a = 4	
	$\begin{vmatrix} 1 & 1 & 1 \\ a & -a & 5 \\ 5 & -3 & 6 \end{vmatrix} = 0$	
	(–6a + 15) – (6a – 25)	+ (–3a + 5a) = 0
	–6a + 15 – 6a + 25 + 2	2a = 0

10a = 40 a = 4 if a = 4 |AB| = 0

1 1 1 a 3 5 = 0 5 a 6 (18-5a)-(6a-25) $+(a^2-15)=0$  $a^2 - 11a + 28 = 0$ a = 7, 4 a = 4

ME

56. Five jobs (J1, J2, J3, J4 and J5) need to be processed in a factory. Each job can be assigned to any of the five different machines (M1, M2, M3, M4 and M5). The time duration taken (in minutes) by the machines for each of the jobs, are given in the table. However, each job is assigned to a specific machine in such a way that the total processing time is minimum. The total processing time is \_\_\_\_\_ minutes.

	M1	M2	M3	M4	M5
J1	40	30	50	50	58
J2	26	38	60	26	38
J3	40	34	28	24	30
J4	28	40	40	32	48
J5	28	32	38	22	44

Ans. (146)

Sol.

		$M_3$			
10	30	50	50	58	1

$J_1$	40	30	50	50	58
J <sub>2</sub>	26	38	60	26	38
$J_3$	40	34	28	24	30
J <sub>4</sub>	28	40	40	32	48
$J_5$	28	32	38	22	54

Step-I Substracting each row with min. value of each respective row.

10	0	20	20	28
0	12	34	0	12
16	10	4	0	6
0	12	12	4	20
6	10	16	0	22



# General Awareness Classroom Course

for

Branches CE ME EE

#### • Classes by expert faculty in respective domains

- Well-structured study curriculum
- Test Series (online/offline) to determine level of preparation
- Learn how to read, decode, and deduce an answer
- Get rub-off with the best minds aspiring for SSC-JE
- Also, useful for State Engg Services/PSUs/State PSUs/ RRB-JE, etc.

#### **Program includes**

- All General Awareness topics as per SSC-JE syllabus
- 3 Full-length tests (Online/ Offline)

F-126, Katwaria Sarai, New Delhi-110016 | Call +91 801 00 09955 Email: info@iesmaster.org

B-23 A, 5th Floor, Gaurav Deep Heights, Near Fortis Hospital Sector 62, Noida - 201305 | Call 0120 415 1100 Email: info.noida@iesmaster.org | Website: iesmaster.org

#### Batch starting from 25<sup>th</sup> Feb, 2019

**SSC-JE** 

2019

Course Duration 140-150 Hrs (3-4 Hrs a day Monday to Friday)

> **Timing** 05:30 to 08:30

<mark>Fee</mark> ₹ 6,800 + GST (18%)

**ENROLL NOW** 





- Quality questions as per SSC-JE exam syllabus and pattern
- Covers all tech and non-tech topics as per SSC-JE Paper-I syllabus
- Designed to make students get into real exam mode
- Get the desired boost in confidence



F-126, Katwaria Sarai, New Delhi-110016 | Call +91 801 00 09955 Email: info@iesmaster.org

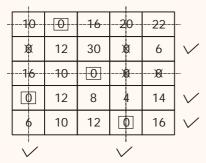
B-23 A, 5th Floor, Gaurav Deep Heights, Near Fortis Hospital Sector 62, Noida - 201305 | Call 0120 415 1100 Email: info.noida@iesmaster.org | Website: iesmaster.org



**Step 2:** Substracting each column with min. value of each respectively value.

10	0	16	20	22
0	12	30	0	6
16	10	0	0	0
0	12	8	4	14
6	10	12	0	16

#### Step-3 Assigning row and column



Step-4

16	0	16	26	22
Ø	6	24	Ø	0
22	10	0	6	Ø
0	6	2	4	8
6	4	6	0	10

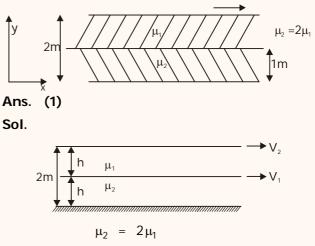
**Step-5** Min. time = 28 + 30 + 28 + 22 + 38 = 146 min

**57.** Two immiscible, incompressible, viscous fluids having same densities but different viscosities are contained between two infinite horizontal parallel plates. 2 m apart as shown below. The bottom plate is fixed and the upper plate moves to the right with a constant velocity of 3 m/s. With the assumptions of Newtonian fluid, steady, and fully developed laminar flow with zero pressure gradient in all directions, the momentum equations simplify to

$$\frac{d^2 u}{dy^2} = 0$$

If the dynamic viscosity of the lower fluid,  $\,\mu_2\,$  is

twice that of the input fluid,  $\mu_1$ , then the velocity at the interface (round off to two decimal places) is \_\_\_\_\_ m/s.



$$V_2 = 3 \text{ m/s}$$

Shear stress value at intermediate plate will be

$$\tau = \frac{\mu_2 V_1}{h} = \frac{\mu_1 (V_2 - V_1)}{h}$$

$$2 V_1 = V_2 - V_1$$

$$V_2 = 3 V_1 V_2 = 3 m/s$$

$$V_1 = 1 m/s$$

**58.** At a critical point in a component, the state of stress is given as  $\sigma_{xx} = 100 \text{ MPa}$ ,  $\sigma_{yy} = 220 \text{ MPa}$ ,  $\sigma_{xy} = \sigma_{yx} = 80 \text{ MPa}$  and all other stress components are zero. The yield

strength of the material is 468 MPa. The factor of safety on the basis of maximum shear stress theory is \_\_\_\_\_ (round off to one decimal place).

Sol.  $\sigma_x = 100 \text{ MPa}$ 

$$\sigma_{y} = 220 \text{ MPa}$$



$$\tau_{xy} = 80 \text{ MPa}$$

$$\sigma_{1,2} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xh}^2}$$

$$= \frac{100+220}{2} \pm \sqrt{\left(\frac{100-220}{2}\right)^2 + 80^2}$$

$$= 160 \pm \sqrt{55^2 + 80^2}$$

$$\sigma_{1,2}$$
 = 160 ± 97.0824

 $\Rightarrow$   $\sigma_1$  = 257.08 Mpa,  $\sigma_2$  = 62.9 MPa

As per maximum shear stress theory

$$\frac{S_{yt}}{2N} = Max \left[ \left| \frac{\sigma_1 - \sigma_2}{2} \right|, \frac{\sigma_1}{2}, \frac{\sigma_2}{2} \right]$$
$$\frac{S_{yt}}{2N} = \frac{\sigma_1}{2} = \frac{257.08}{2}$$
$$N = \frac{468}{257.08} = 1.8$$

**59.** Match the following sand mold casting effects with their respective causes.

	Defect		Cause	
Р	Blow hole	1.	Poor Collapsibility	
Q	Misrum	2.	Mold erosion	
R	Hot tearing	3.	Poor permeability	
S	Wash	4.	Insufficient fludity	
(a)	P-3, Q-4, R-	1, S	-2	
(b)	P-3, Q-4, R-	2, S	-1	
(c)	P-4, Q-3, R-1, S-2			
(d)	P-2, Q-4, R-1, S-3			
Ans. (	Ans. (a)			

**60.** A gas is heated in a duct as it flows over a resistance heater. Consider a 101 kW electric heat-

## GATE 2019 Detailed Solution 02-02-2019 | MORNING SESSION

MF

ing system. The gas enters the heating section of the duct at 100 kPa and 27°C with a volume flow rate of 15 m<sup>3</sup>/s. If heat is lost from the gas in the duct to the surroundings at a rate of 51 kW, the exit temperature of the gas is (Assume constant pressure, ideal gas, negligible change in kinetic and potential energies and constant specific heat :  $C_p = 1 \text{ kJ/kg.K}$ ; R = 0.5 kJ/kg K). (b) 76°C (a) 37°C 53°C (d) 32°C (c) Ans. (d) Sol.  $W_{in} = 101 \text{ kW}$ P = 100kPa www T = 300k ► T<sub>2</sub> = ?  $V_1 = 15m^3/s$  $Q_{lost} = 51 kW$  $C_p = 1 \frac{kJ}{kgK}$  $R = 0.5 \frac{kJ}{kgK}$  $\dot{m} = \frac{P_1 \dot{V}_1}{R T_1} = \frac{100 \times 15}{0.5 \times 300} = 10 \frac{kg}{s}$ Applying steady flow energy equation,  $\dot{m}h_1 + \dot{8} = \dot{m}h_2 + \dot{W}$  $10 \times 1 \times 300 + (-51) = 10 \times 1 \times T_2 + (-101)$  $T_2 = 305 \text{ K} = 32^{\circ}\text{C}$ **61.** The value of the following definite integral is \_\_\_\_\_ (round off to there decimal places).  $\int (x \ln x) dx$ 

Ans. (2.097)

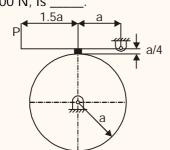
Sol.

$$\int_{1}^{e} x \ln x dx$$



$$= \frac{\ln x^2}{2} - \int \left[\frac{1}{x} \times \frac{x^2}{2}\right] d\lambda$$
$$= \frac{x^2 \ln x}{2} - \frac{x^2}{4} \Big|_1^e$$
$$= \left(\frac{e^2}{2} - \frac{e^2}{4}\right) + \frac{1}{4}$$
$$= \frac{e^2 + 1}{4} = 2.097$$

**62.** A single block brake with a short shoe and torque capacity of 250 N-m is shown. The cylindrical brake drum rotates anticlockwise at 100 rpm and the coefficient of friction is 0.25. The value of a, in mm (round off to one decimal place), such that the maximum actutating force P is 2000 N, is \_\_\_\_\_.



Ans. (212.5) Sol.

T = 250 Nm  $F \times r = 250$   $F = \frac{250}{a}$   $P \longrightarrow 1.5a \longrightarrow F'/\mu a$   $F \longrightarrow a/4$   $F \longrightarrow a/4$   $\sum M_0 = 0$   $P \times 2.5a = F \times \frac{a}{4} + \frac{F}{\mu} \times a$ 

## GATE 2019 ME Detailed Solution 02-02-2019 | MORNING SESSION

$$2000 \times 2.5a = \frac{250 \times a}{a \times 0.25} + \frac{250}{a} \times \frac{a}{4}$$
$$a = \frac{1000 + 62.5}{5000} = 212.5 \text{mm}$$

**63.** Consider a prismatic straight beam of length L =  $\pi$  m, pinned at the two ends as shown in the figure The beam has a square cross-section of side p = 6 mm. The Young's modulus E = 20 GPa, and the coefficient of thermal expansion

 $\alpha = 3 \times 10^{-6} \text{ K}^{-1}$ . The minimum temperature rise required to cause Euler buckling of the beam is \_\_\_\_\_ K.



Ans. (1) Sol.

$$L = \pi m$$

$$P_{th} = P_{axial}$$

$$\alpha TEA = \frac{\pi^2 EI}{L^2}$$

$$3 \times 10^{-6} \times \Delta T \times 6 \times 6 \times 10^{-6} = \frac{\pi^2 \times \frac{1}{12} \times (6 \times 10^{-3})^2}{\pi^2}$$

$$\Delta T = 1K$$

64. A gas turbine with air as the working fluid has an isentropic efficiency of 0.70 when operating at a pressure ratio of 3. Now, the pressure ratio of the turbine is increased to 5, while maintaining the same inlet conditions. Assume air as a perfect gas with specific heat ratio  $\gamma = 1.4$ . If the specific work output remains the same for both the cases, the isentropic efficiency of the turbine at the pressure ratio of 5 is \_\_\_\_\_ (round off to two decimal places).

Ans. (0.51)

Sol.

$$\eta = 0.7, (r_p)_1 = 3$$



Our Star Performers - UPSC ESE 2018 "Consistent Quality, Outstanding Results"

#### **CONGRATULATIONS TO ALL**

Civil Engineering





$$\eta_{2} = ? (r_{p})_{2} = 5$$

$$r = 1.4$$

$$(W_{T})_{1} = (W_{T})_{2}$$
Inlet condition same,
$$T = \frac{1}{1 - \frac{1}{2}} = S$$

$$\eta_{1} = \frac{h_{1} - h_{2}}{h_{1} - h_{2s}}$$

$$= \frac{T_{1} - T_{2}}{T_{1} - T_{2s}} = \frac{T_{1} - T_{2}}{T_{1} - \frac{T_{1}}{x}}$$

$$\eta_{1} \left(T_{1} - \frac{T_{1}}{x}\right) = \eta_{2} \left(T_{1} - \frac{T_{2}}{y}\right)$$

$$0.7 \left(1 - \frac{1}{(3)^{2/7}}\right) = 0.7 \left(1 - \frac{1}{(5)^{2/4}}\right)$$

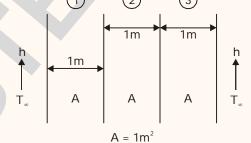
$$\boxed{\eta = 0.51}$$

65. Three slabs are joined together as shown in the figure. There is no thermal contact resistance at the interfaces. The center slab experience a nonuniform internal heat generation with an average value equal to 10000 Wm<sup>-3</sup>, while the left and right slabs have no internal heat generation. All slabs have thickness equal to 1 m and thermal conductivity of each slab is equal to 5 Wm<sup>-1</sup> K<sup>-1</sup>. The two extreme faces are exposed to fluid with heat transfer coefficient 100 Wm<sup>-2</sup>K<sup>-1</sup> and bulk temperature 30°C as shown. The heat transfer in the slabs is assumed to be one dimensional and steady, and all properties are constant. If the left extreme face temperature T1 is measured to be 100°C, the right extreme faced temperature  $T_2$  is \_\_\_\_\_ °C.

#### 02-02-2019 | MORNING SESSION Left extreme $T_2$ face $T_1 = 100^{\circ}C$ 1 m 1 m 1 m 100 w/m<sup>2</sup>.k 100 w/m<sup>2</sup>.k 30°C 30°C Ans. (60) Sol. (1)(2)(3)

**GATE 2019** 

**Detailed Solution** 



Heat generated in the slab (2) will be convected away from the slabs 1 and 3

i.e.  $\dot{E}_{gen} = \dot{Q}_{1,conv} + \dot{Q}_{3,conv}$   $\dot{Q}_{1,conv} = h \times A \times (T_1 - T_{\infty})$   $= 100 \times 1 \times (100 - 30)$  = 7000 W  $\dot{Q}_{3,conv} = h \times A \times (T_3 - T_{\infty})$   $Q_{3,conv} = 100 \times 1 \times (T_3 - 30)$ Now  $\dot{E}_{gen} = 10,000 \times A \times width$   $= 10,000 \times 1 \times 1$   $\dot{E}_{gen} = 10,000 W$   $\Rightarrow 10,000 = 7000 + 100 \times (T_3 - 30)$  $\Rightarrow \overline{T_3 = 60^{\circ}C}$