Note: 1. Graph sheets and statistical tables will be supplied on request.
2. Scientific calculators are allowed.
3. All working steps should be clearly shown.

## Section- A

I. Answer any TEN of the following:
$10 \times 1=10$

1. What is lifetable?
2. Mention one characteristic of index number.
3. What is value index number?
4. Give an example for seasonal variation.
5. What is the probability that a normal variate takes a value greater than mean?
6. Under what conditions Poisson distribution tends to normal distribution?
7. What is parameter space?
8. What is Critical Value?
9. Write the formula of S.E $\left(\bar{X}_{1},-\bar{X}_{2}\right)$.
10. Define acceptance sampling plan.
11. Define E.O.Q.
12. What is Saddle point?

## Section- B

II. Answer any TEN of the following:
13. There was a record of 4000 live births in a city in a year. The number of neonatal deaths was 100 . Calculate the neonatal mortality rate.
14. The sum of the product of current year quantity and base year price is 450 and the sum of the product of base year quantity and price is 350 . Find the quantity index number.
15. Why Fisher's index number is called ideal index number?
16. What is random variation? Give an example.
17. Write down the conditions for applying Newton's advancing difference method of interpolation.
18. Write down the Bernoulli distribution with parameter $\mathrm{p}=0.25$.
19. Write applications of $\chi^{2}$-distribution.
20. Define level of significance and critical region.
21. Given, $\bar{x}=53 \mathrm{gm}, \mu=50 \mathrm{gm}, \mathrm{s}=5 \mathrm{gm}$ and $\mathrm{n}=17$, calculate test statistic t .
22. If $p^{1}=0.02, n=100$ calculate $U C L$ and $L C L$ for $n p$-chart.
23. Define degenerate solution.
24. Define pure and mixed strategy.
Section - C
III. Answer any EIGHT of the following: $8 \times 5=40$
25. From the following data compute N.R.R.

| Age <br> (years) | Female <br> Population | Female <br> Births | Survival <br> Rates |
| :---: | :---: | :---: | :---: |
| $15-19$ | 26730 | 600 | 0.95 |
| $20-24$ | 19725 | 630 | 0.93 |
| $25-29$ | 18600 | 800 | 0.9 |
| $30-34$ | 18000 | 1900 | 0.85 |
| $35-39$ | 17000 | 1600 | 0.8 |
| $40-44$ | 16500 | 800 | 0.75 |
| $45-49$ | 15000 | 630 | 0.72 |

26. Calculate $\mathbf{P}_{01}$ by simple average of price relatives using (i) Arithmetic mean (ii) Geometric mean.

| Items | Prices in 2012 | Prices in 2014 |
| :---: | :---: | :---: |
| A | 26 | 28 |
| B | 32 | 30 |
| C | 18 | 20 |


| D | 12 | 12 |
| :---: | :---: | :---: |
| E | 40 | 45 |

27. Explain the steps involved in the construction of Index numbers.
28. Obtain the trend values by 5 yearly moving average method for the following time series.

| Year | 2001 | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Production (in 000's tones) | 15 | 16 | 18 | 18 | 20 | 19 | 22 | 24 | 25 |

29. Interpolate the missing values from the following data using Binomial expansion method.

| Year | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Value | 64 | 60 | $?$ | 56 | 55 | 50 | $?$ |

30. In an office $20 \%$ of the employees are females. In a random sample of 5 employees obtain the probability that there are (i) no females (ii) females only.
31. A pond has 20 fishes of which 8 are red and remaining are white. Four fish are caught. Find the mean and variance of the number of red fishes caught.
32. From the following table, test whether the sample means differs significantly at 5\% L.O.S.

|  | I | II |
| :---: | ---: | ---: |
| Size | 80 | 90 |
| Means | 52 | 55 |
| S.D. | 8 | 7 |

33. Weight of 10 jack fruits are as follows:

Weight (kgs): 6, 5, 8, 7, 4, 5, 8, 6, 5, 6.
Test at $5 \%$ level of significance that SD differs significantly from 2 kgs .
34. For the following data, find the control limits for $\overline{\mathbf{X}}$ and $\mathbf{R}$ - chart.

| Subgroup No. | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mean | 52 | 48 | 53 | 49 | 50 | 48 |
| Range | 10 | 11 | 8 | 12 | 9 | 10 |

35. From the following pay-off matrix of player A, solve the game by maximin-minimax principle.

| Player A |  | Player B |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{B}_{1}$ | $\mathrm{~B}_{2}$ | $\mathrm{~B}_{3}$ | $\mathrm{~B}_{4}$ |
|  | $\mathrm{~A}_{1}$ | 3 | 2 | 1 | 6 |
|  | $\mathrm{~A}_{2}$ | 3 | 1 | 0 | 4 |
|  | $\mathrm{~A}_{3}$ | 3 | 4 | -3 | 0 |

36. Solve the following L.P.P graphically.

Minimize $Z=4 x+3 y$
Subject to $\quad x+y \leq 2$ $x+3 y \geq 3$ and $x, y \geq 0$

## Section - D

IV. Answer any TWO of the following:
$2 \times 10=20$
37. Compute C.D.R's and S.T.D.R's for the following two populations and compare the mortality.

| Age (years) | Town A |  | Town B |  | Standard Population |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Population | Deaths | Population | Deaths | Deaths |
| $0-9$ | 15000 | 150 | 15000 | 200 | 12000 |
| $10-19$ | 13000 | 80 | 12000 | 150 | 13000 |
| $20-39$ | 10000 | 40 | 20000 | 75 | 14000 |
| $40-59$ | 8000 | 55 | 12000 | 45 | 12000 |
| $60-79$ | 6000 | 110 | 8000 | 175 | 8000 |
| $80+$ | 2000 | 150 | 5000 | 250 | 6000 |

38. Construct Fisher's price index number for the following data. Test whether it satisfies TRT and FRT.

| Commodity | Base year |  | Current year |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Price (Rs) | Quantity | Price (Rs) | Expenditure |
| A | 7 | 70 | 9 | 100 |
| B | 9 | 80 | 11 | 110 |
| C | 15 | 25 | 20 | 40 |
| D | 20 | 30 | 25 | 40 |

39. Fit a straight line trend for the following data and hence find trend values. Estimate the price for the year 2013 of a certain commodity.

| Year | 2007 | 2008 | 2009 | 2010 | 2011 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Price (Rs) | 12 | 20 | 31 | 40 | 47 |

40. Fit a Binomial distribution for the following data and test whether it is a good fit at $\alpha=5 \%$.

| No. of heads | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of tosses | 5 | 28 | 34 | 30 | 21 | 10 |

## Section-E

V. Answer any TWO of the following:
$2 \times 5=10$
41. Heights of 360 children are normally distributed with mean $=120 \mathrm{cms}$ and variance $=4 \mathrm{~cm}^{2}$. Find expected number of children having heights (i) greater than 118 cm (ii) less than 122 cm .
42. A machine produced 6 defective articles among 50 articles. Test whether the proportion of defective articles is less than $10 \%$. (use $\alpha=5 \%$ )
43. From the following data, test whether 'education' and 'employment' are independent at $5 \%$ level of significance.

| Education | Employment |  |
| :---: | :---: | :---: |
|  | Employed | Unemployed |
| Educated | 30 | 28 |
| Uneducated | 25 | 35 |

44. The cost of a scooter is Rs.36,000. Its resale value and maintenance cost at different years is given below.

| Year of Service | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Maintenance Cost (Rs.) | 800 | 1,300 | 1,900 | 2,700 | 3,900 | 5,400 |
| Resale Value (Rs.) | 28,000 | 22,000 | 20,000 | 18,000 | 17,000 | 16,000 |

Determine the optimal year for replacement of the scooter.

