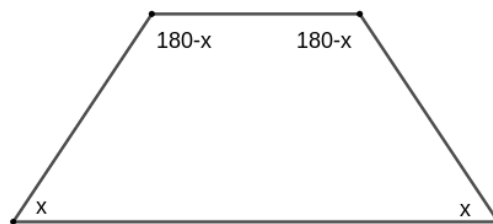
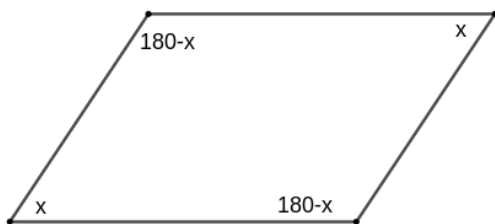
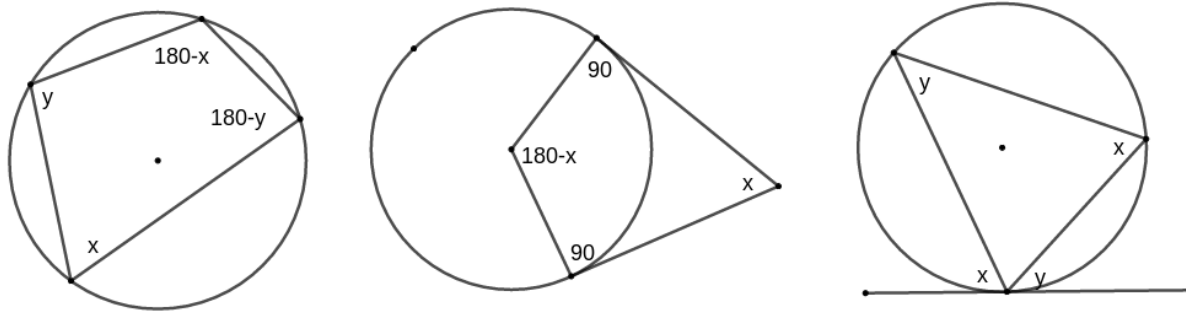
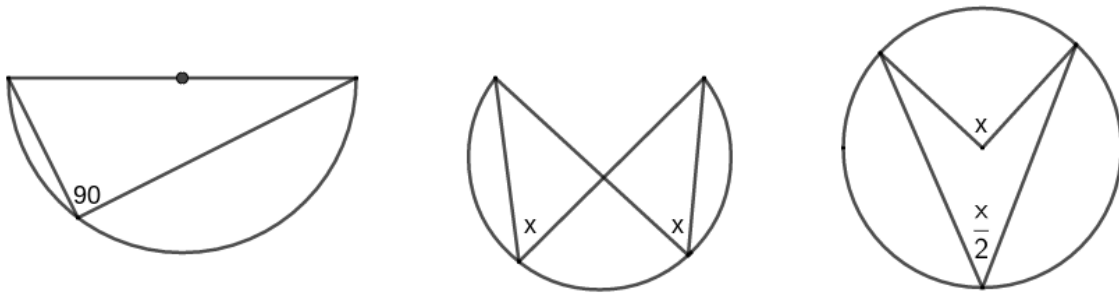
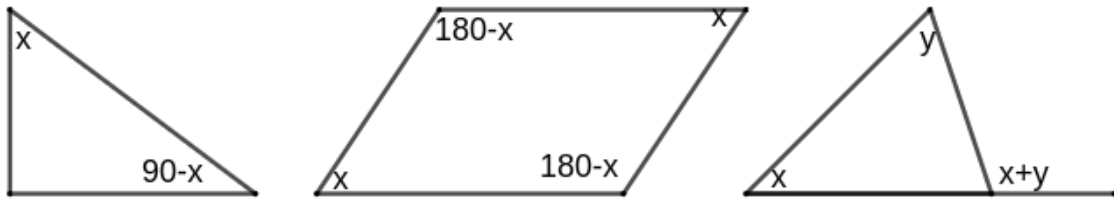
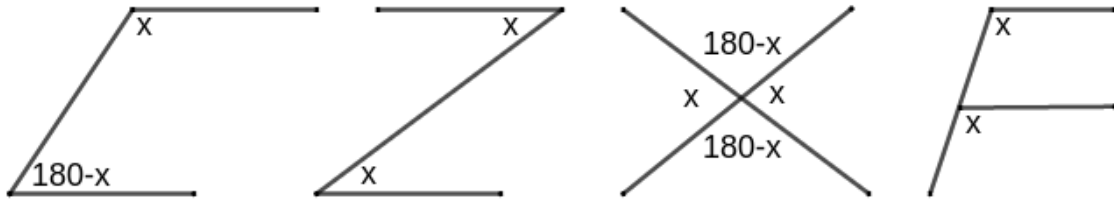
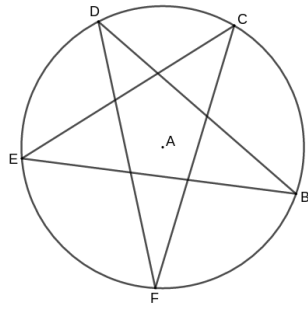


**SSLC 2019
CIRCLE AND TANGENTS
CONCEPTS-PROBLEMS-PROOFS**



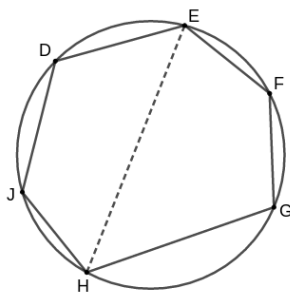
CIRCLES AND TANGENTS CONCEPTS AND PROOF

1) Prove that $\angle B + \angle C + \angle D + \angle E + \angle F = 180^\circ$



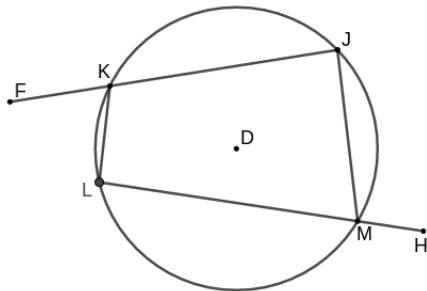
Hint: $\angle B = \frac{1}{2}(\text{-----})$, $\angle C = \frac{1}{2}(\text{-----})$ etc
 $\angle B + \angle C + \angle D + \dots = \frac{1}{2}(\text{-----}) = \text{-----}$

2) Prove that $\angle D + \angle F + \angle H = \angle E + \angle G + \angle J$



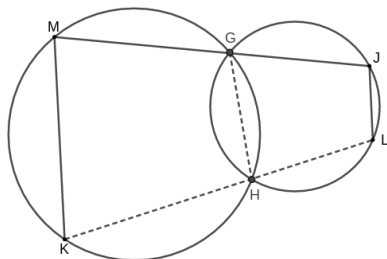
Hint: Let $\angle JHE = a$, $\angle GHE = b$, Then $\angle D = \text{-----}$
 $\angle F = \text{-----}$, $\angle D + \angle F + \angle H = \text{-----}$,
hence $\angle J + \angle E + \angle G = 720 - (\text{-----})$

3) Prove that $\angle FKL + \angle HMJ = 180^\circ$



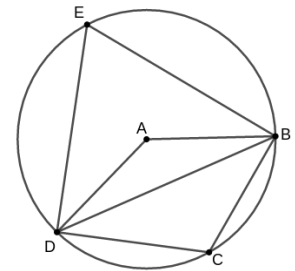
Hint: Let $\angle JMH = x$, then $\angle LMH = \text{-----}$
 $\angle LKJ = \text{-----}$, $\angle FKL = \text{-----}$.

4) In figure $MK \parallel LJ$. Show that H is in the line KL



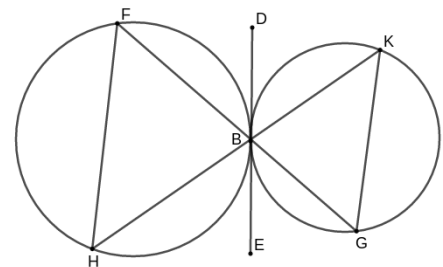
Hint: draw GH, KH, LH. Let $\angle M = x$, then $\angle J = \text{-----}$, because $MK \parallel JL$.
Also $\angle KHG = \text{-----}$, $\angle GHL = \text{-----}$
 $\angle KHG + \angle LHG = \text{-----}$, hence KHL is -----

5) Prove that $\angle DEB + \angle ADB = 90^\circ$
and $\angle DCB - \angle ADB = 90^\circ$.



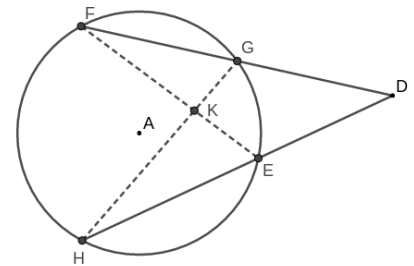
Hint: Let $\angle ADB = x$, then $\angle ABD = \text{-----}$
 $\angle DAB = \text{-----}$, $\angle DEB = \text{-----}$
 $\angle DCB = \text{-----}$

6) In figure Show that $FH \parallel KG$



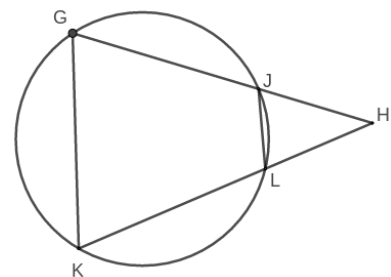
Hint: Let $\angle H = x$ then $\angle FBD = \text{-----}$, $\angle EBG = \text{-----}$
 $\angle BKG = \text{-----}$. Hence HF, GK are -----

7) In figure show that $\angle FKH + \angle FDH = \angle FAH$



Hint: Let $\angle FAH = x$, then $\angle FGH = \text{-----}$,
 $\angle FEH = \text{-----}$, $\angle KGD = \text{-----}$, $\angle KED = \text{-----}$
But $\angle KGD + \angle KED + \angle GKE + \angle GDE = \text{-----}$
 $\angle GKE + \angle GDE = \text{-----}$. $\angle FKH + \angle GDE = \text{-----}$

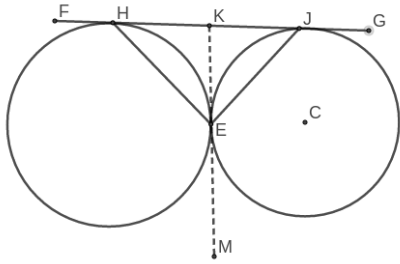
8) In figure, $HJ = HL$. Show that $GJ = KL$, $GK \parallel JL$



Hint: we have $HJ \times HG = \text{-----} \times \text{-----}$
given $HJ = HL$, hence ----- = -----
Let $\angle HJL = x$, then $\angle HLJ = \text{-----}$
 $\angle JLK = \text{-----}$ $\angle JGK = \text{-----}$, hence $JL \parallel GK$
GJLK is a -----

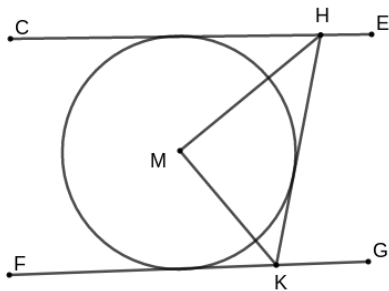
CIRCLES AND TANGENTS CONCEPTS AND PROOF

9) In figure, Show that HEJ is a right triangle.



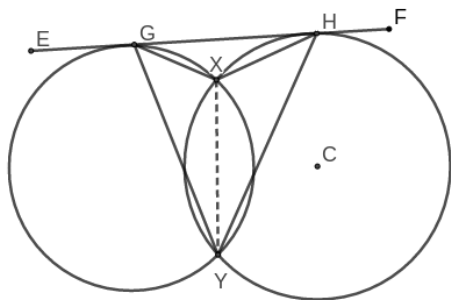
Hint: Let $\angle HEK = x$, $\angle JEK = y$ then
 $\angle KHE = \dots\dots\dots$, $\angle KJE = \dots\dots\dots$
 but $\angle HEJ + \angle EJH + \angle JHE = \dots\dots\dots$
 hence $x + y = \dots\dots\dots$, $\angle HEJ = \dots\dots\dots$

10) In figure, Show that HMK is a right triangle.



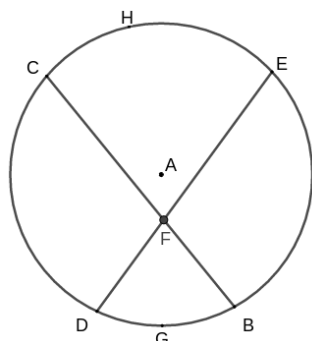
Hint: Let $\angle MHK = x$, $\angle MKH = y$. Then
 $\angle M = \dots\dots\dots$, $\angle MHC = \dots\dots\dots$, $\angle MKF = \dots\dots\dots$
 Given $CE \parallel FG$ hence, $\angle CHK + \angle FKH = \dots\dots\dots$
 $2x + 2y = \dots\dots\dots$, hence $x + y = \dots\dots\dots$, $\angle M = \dots\dots\dots$

11) Show that $\angle GXH + \angle GYH = 180^\circ$.



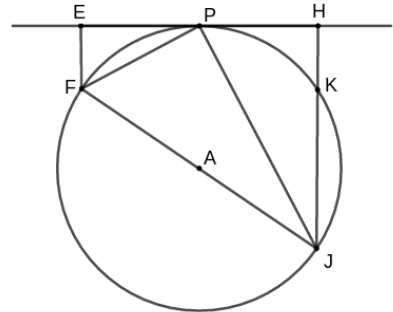
Hint: Let $\angle HGX = x$, $\angle GHX = y$, then
 $\angle GYX = \dots\dots\dots$, $\angle HYX = \dots\dots\dots$, $\angle GYH = \dots\dots\dots$
 Also, $\angle GXH = \dots\dots\dots$

12) In figure A is centre. Show that $\angle CAE + \angle DAB = 2\angle CFE$



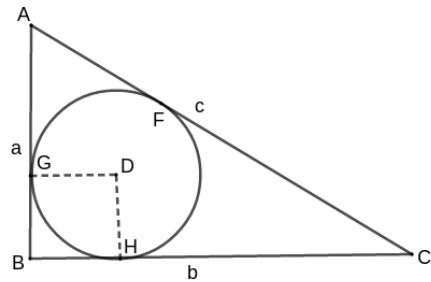
Hint: join CD. $\angle D = \frac{1}{2}(\dots\dots\dots)$, $\angle C = \frac{1}{2}(\dots\dots\dots)$
 but, $\angle CFE = \angle D + \angle C$ (Exterior angle law)
 hence $\angle CFE = \frac{1}{2}(\dots\dots\dots + \dots\dots\dots)$
 $2(\angle CFE) = \dots\dots\dots + \dots\dots\dots$

13) EH is a tangent. $\angle PEF = \angle PHJ = 90^\circ$. Show that $FJ^2 = EF^2 + EP^2 + PH^2 + HJ^2$.



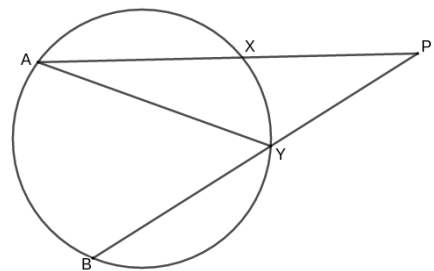
Hint: Since A is centre $\angle FPJ = \dots\dots\dots$
 By pythagorus theorem,
 $FP^2 = EF^2 + EP^2$, $PJ^2 = \dots\dots\dots$
 $FJ^2 = \dots\dots\dots = \dots + \dots + \dots + \dots$

14) In figure show that In-radius of the right triangle equals $\frac{1}{2}(a+b-c)$



Hint: Let radius $GD = r$. Then $BH = r$, $BG = r$
 $HC = b - r$, $CF = b - r$. Similarly $GA = \dots\dots\dots$
 $AF = \dots\dots\dots$. But we have $AF + FC = c$.
 Hence $r = \dots\dots\dots$

15) Prove that difference of central angles of small arcs AB and CD is double of $\angle P$



Hint: Let O be the centre. We have $\angle AYB = \angle A + \angle P$
 hence $\angle P = \angle AYB - \angle A$
 $= \frac{1}{2}\angle AOB - \frac{1}{2}(\dots\dots\dots)$
 $2\angle P = (\dots\dots\dots) - \angle XOY$