## JAIN COLLEGE

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## SUBJECT: BasicMaths

## II P U C MOCKI

Timings Allowed: 3 Hrs15 Minutes
Total Marks: 100
Instructions: i) The question paper has 5 parts. $A, B, C, D, E$. Answer all the parts.
ii) Part A carries 10 marks. Part B carries 20 marks, Part C and Part D carries 30 marks and Part E carries 10 marks.
iii) Write the question number properly as indicated in the question paper.

I Answer All

1. If $\mathrm{A}=\begin{array}{ll}3 & 1 \\ 2 & 4\end{array}, B=\begin{gathered}-1 \\ 3\end{gathered}$, Find AB
2. Find ' r ' if $15 \mathrm{C}_{\mathrm{r}+3}=15 \mathrm{C}_{2 \mathrm{r}-3}$
3. Negate : " If a number is multiple of 9 , then it is multiple of 3 "
4. Write third proportion to 8 and 32
5. Write formula for index of learning
6. Find $\cos 75^{0}$
7. Find the radius of circle $x^{2}+y^{2}-2 x-6=0$
8. Evaluate $\lim _{x \rightarrow-1} \frac{x^{3}+1}{2 x^{2}+5 x+3}$
9. If $\mathrm{y}=2 \quad \bar{x}-\cos 2 \mathrm{x}+2$. Find $\frac{d y}{d x}$
10. Evaluate $\frac{1+x^{3}}{x} \mathrm{dx}$

II Answer any TEN
11. If $\mathrm{A}=\begin{array}{cc}2 & -1 \\ -1 & 2\end{array}$, Show that $A^{2}-4 \mathrm{~A}+3 \mathrm{I}=0$
12. In how many ways can 6 red and 4 white marbles be chosen from a bag containing 10 red and 6 white marbles
13. IF $\mathrm{P}(\mathrm{A})={ }^{1}{ }_{2}, P B={ }_{3}, P A \cup B={ }^{7}$ 12. Find $\mathrm{P}\left({ }^{A} B\right)$
14. Write converse, Contra positive of " If a triangle is equilateral, then it is an Isosceles triangle
15. If $a: b=3: 5, b: c=15: 23$, Find $a: c$
16. The banker's gain on certain bill due six months hence is Rs. 10 , the rate of interest being $10 \%$ p.a., .Find the face value of the bill
17. If $\cos x=4{ }_{5}, x$ is acute, Find $\cos 3 x$
18. Transform $2 \sin 40^{0}$. $\cos 20^{\circ}$ into sum
19. Find equation of circle whose end points of its diameter are $(3,4)$ and $(1,-2)$
20. Find ' k ' if $f x=\frac{\frac{e^{2 x}-1}{5 x}, x \neq 0}{k / 2, x=0}$ is continuous at $\mathrm{x}=0$
21. If $\mathrm{S}=\overline{t-1}(\mathrm{t}=$ time, $\mathrm{s}=$ distance $)$.Find velocity
22. If total cost $c(x)=x^{2}+2 x+1$, Find (i) Marginal cost (ii)Average cost
23. Evaluate $\frac{1}{x \log x} d x$
24. Evaluate $x e^{x} d x$

III Answer any TEN
25. If $A=\begin{array}{cc}-1 & 2 \\ 3 & 4\end{array}$, Verify $A .(\operatorname{adjA})=(\operatorname{adjA}) . A=I A I . I$
26. Find inverse of $\begin{array}{ll}1 & 3 \\ 2 & 4\end{array}$
27. Find the number of permutation of letters of the word "COMMISSION" , If the word (i) Start with M and end with N (ii) $2 \mathrm{~S}^{\prime}$ s are together (iii) 2 o's are not together
28. A team of 11 players has to be selected from 14 players of which only 2 can play as wicket keeper? Given each team must have exactly one wicket keeper, how many different teams can be made?
29. A sum of Rs. 2415 has to be divided among three persons $A, B, C$ in such proportion that A's share to B's share as $4: 5, \mathrm{~B}$ 's share to C's share as $9: 16$. How much does each get?
30. A bill of Rs. 50000 was drawn on 10-04-2014 at 3 months and was discounted on 1-05-2014 @ $12 \%$ p,a.,. For what sum was the bill discounted and also find the Banker's gain
31. Find the interest earned on Rs. 4897.50 caash invested in $15 \%$ stock at 81.5 brokerage given is 0.125
32. The owner of departmental store purchased an article of Rs. 1500 at 4\% VATand sell it at Rs. 1700 to the customer at 4\% VAT. How much amount did the shopkeeper deposit to the Government as VAT?
33. Find the equation of the parabola given that the ends of latus rectum are $L(3,6)$ and $\mathrm{L}^{1}(-3,6)$
34. If $\mathrm{x}=\operatorname{acos}^{4} \mathrm{t}, \mathrm{y}=\mathrm{b} \sin ^{4} \mathrm{t}$. Find $\frac{d y}{d x}$ at $\mathrm{t}=\pi 4$
35. The height of a cone is 30 cm and it is constant , the radius of the base is increasing at the rate $0.25 \mathrm{~cm} / \mathrm{sec}$. Find the rate of increase of volume of the cone when the radius is 10 cm .
36. The cost function $C(x)=500 x-20 x^{2}+\frac{x^{3}}{3}$ where ' $x$ ' is the number of output.Calculate the output when marginal cost is equal to average cost
37. Evaluate $\frac{1}{e^{x}+e^{-x}} d x$
38. Evaluate $\frac{1}{\bar{x}+x} d x$

## PART D

## IV ANSWER ANY SIX

5X6=30
39. Find the coefficient of $x^{-11}$ in the expansion of $\bar{x}-\frac{2}{x}^{17}$
40. Resolve into partial fractions $\frac{1+2 x}{x+2^{2}(x-1)}$
41. Prove that $\sim(p \leftrightarrow q) \equiv\left(p^{\wedge} \sim q\right) V\left(q^{\wedge} \sim p\right)$
42. If 15 men working 12 hrs per day perform job in 16 days. How long will it take for 21 men working 10 hrs daily to do the same job
43. A company requires 1000 hrs to produce the first 30 engines. If the learning effect is $90 \%$, then Find the total labour cost to produce a total of 120 engines @ Rs. 20 per hr.
44. Using Graphical method, Solve LPP Minimize $\mathrm{Z}=1.5 \mathrm{X}+2.5 \mathrm{Y}$, subjected to constraints $\mathrm{X}+3 \mathrm{Y} \geq 3$, $X+Y \geq 2$ and $X, Y \geq 0$
45. Show that $\frac{\sin ^{3} \theta+\sin 3 \theta}{\sin \theta}+\frac{\cos ^{3} \theta-\cos 3 \theta}{\cos \theta}=3$
46. Find equation of circle passing through $(1,1),(2,-1)$ and $(3,2)$
47. IF $\mathrm{e}^{\mathrm{Y}}=\sin (\mathrm{x}+\mathrm{y})$, Prove that $\frac{d y}{d x}=\frac{\cos x+y}{e^{y}-\cos x+y}$
48. Find the area enclosed by $y^{2}=4 x$ and $x^{2}=4 y$

## PART E

V ANSWER ANY ONE
49. (a)Evaluate $\lim _{x \rightarrow a} \frac{x^{n}-a^{n}}{x-a}=n a^{n-1}$ for all rationals ( n is $+\mathrm{ve},-\mathrm{ve}$, rationals)
(b)Find the value of $(0.98)^{3}$ using Binomial theorem upto 5 decimals
50. (a) Salesman Venki has the following record of sales during 3 months of July, August, Sepetember for three products $\mathrm{A}, \mathrm{B}, \mathrm{C}$ which have different rates of commission

| Month | Sales in units |  |  | Total |
| :--- | :--- | :--- | :--- | :--- |
|  | A | B | C | Commission(Rs) |
| July | 100 | 100 | 100 | 700 |
| August | 200 | 300 | 200 | 1700 |
| September | 400 | 900 | 100 | 3700 |

Using Matrix method, Find out the sales of commission on items A,B,C received by Venki (b) A person standing on bank of a river observes that the angle subtended by a tree on the opposite bank is $60^{\circ}$. When he returns 40 mts from the bank he finds the angle to be $30^{\circ}$. Find the height of the tree and breadth of the river

