

## Second Year - March 2018

Time : 2 Hours
Cool-off time : 15 Minutes

## Part - III <br> STATISTICS

Maximum : 60 Scores

## General Instructions to Candidates:

- There is a 'Cool-off time' of 15 minutes in addition to the writing time.
- Use the 'Cool-off time' to get familiar with questions and to plan your answers.
- Read questions carefully before answering.
- Read the instructions carefully.
- Calculations, figures and graphs should be shown in the answer sheet itself.
- Malayalam version of the questions is also provided.
- Give equations wherever necessary.
- Statistical tables can be used in the examination hall.
- Electronic devices except non-programmable calculators are not allowed in the Examination Hall.


## 






 உளைமி円ிெஸை๐.





(Questions 1 to 9 carries 2 Scores each. Answer any 8 questions.) (Scores : $8 \times 2=16$ )

1. Choose the correct answer :
(a) If Z is a standard normal variable, then $\mathrm{P}(\mathrm{Z}>0)$ is :
(i) 0
(ii) 1
(iii) -1
(iv) 0.5
(b) The p.d.f. of a random variable X is

$$
\mathrm{f}(x)=\frac{1}{3 \sqrt{2 \pi}} \mathrm{e}^{\frac{-(x-20)^{2}}{18}},-\infty<x<\infty
$$

The mean of X is :
(i) 3
(ii) 20
(iii) 18
(iv) 9
$(1+1)$
2. Match the following :

## A

## B

(i) No correlation
(a) Rank Correlation coefficient
(ii) $\frac{\operatorname{cov}(x, y)}{\sigma_{x} \times \sigma_{y}}$
(b) $\mathrm{r}= \pm 1$
(iii) $1-\frac{6 \Sigma \mathrm{~d}^{2}}{\mathrm{n}^{3}-\mathrm{n}}$
(c) Correlation coefficient
(iv) Perfect correlation
(d) $\mathrm{r}=0$
3. The following data relate to the Scores obtained by 10 students in Statistics (X) and Economics (Y) for a class test :
$\Sigma \mathrm{X}=247, \Sigma \mathrm{Y}=263, \Sigma \mathrm{X}^{2}=7345, \Sigma \mathrm{Y}^{2}=7537, \Sigma \mathrm{XY}=7259$.
Calculate the correlation coefficient.
4. The probability distribution of a random variable X is

$$
\mathrm{f}(x)= \begin{cases}\mathrm{k} x, & 0 \leq x \leq 2 \\ 0, & \text { otherwise }\end{cases}
$$

Find the value of k .
5. Calculate the simple arithmetic mean price index number for the data given below :

| Item | Units | Price in 2015 | Price in 2017 | Price relative |
| :--- | :--- | :---: | :---: | :---: |
| Milk | litre | 36 | 40 | 111.11 |
| Sugar | kg | 35 | 43 | 122.86 |
| Egg | Dozen | 48 | 53 | 110.42 |



（€ற్మురియ゙ ： $8 \times 2=16$ ）


（i） 0
（ii） 1
（iii）－ 1
（iv） 0.5

$\mathrm{f}(x)=\frac{1}{3 \sqrt{2 \pi}} \mathrm{e}^{\frac{-(x-20)^{2}}{18}},-\infty<x<\infty$

（i） 3
（ii） 20
（iii） 18
（iv） 9


A

（ii）$\frac{\operatorname{cov}(x, y)}{\sigma_{x} \times \sigma_{y}}$
（iii） $1-\frac{6 \Sigma \mathrm{~d}^{2}}{\mathrm{n}^{3}-\mathrm{n}}$


## B


（b） $\mathrm{r}= \pm 1$

（d） $\mathrm{r}=0$


$\Sigma \mathrm{X}=247, \Sigma \mathrm{Y}=263, \Sigma \mathrm{X}^{2}=7345, \Sigma \mathrm{Y}^{2}=7537, \Sigma \mathrm{XY}=7259$ ．



 ゃつறுమ ：

| ற（\％ | ®カカ円 | 2015 ¢ை வile | 2017 ๑ை வி¢ |  |
| :---: | :---: | :---: | :---: | :---: |
| －10\％ | － | 36 | 40 | 111.11 |
| வவைை | カை．）（0）O． | 35 | 43 | 122.86 |
| 035 | aumua | 48 | 53 | 110.42 |

6. In a regression analysis the following results are obtained :

$$
\mathrm{b}_{\mathrm{y} x}=0.23, \gamma=0.45, \sigma_{x}=10
$$

Find the standard deviation of $y$.
7. An automobile manufacturer claims that a particular model gets $23 \mathrm{~km} /$ litre mileage. A consumer agency, using a sample of 50 automobiles of the model, finds the sample mean to be $21.8 \mathrm{~km} / \mathrm{litre}$ and variance $7.84 \mathrm{~km} / \mathrm{litre}$. Does this data agree with the claim of the manufacturer at $5 \%$ level of significance.
8. The trend equation of a time series with origin 2010 is $y=18.04 x+126.55$. Shift the origin to 2015.
9. In a certain sampling inspection, the total number of defectives found in 10 samples of 100 each is 170 . Calculate the control limits for np-chart.
(Questions 10 to 16 carries 3 Scores each. Answer any 6 questions). $\quad$ (Scores : $6 \times 3=18$ )
10. A random variable X has the following probability distribution :

| $x$ | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(x)$ | 0.5 | 0.3 | 0.2 |

Find the mean and variance of the random variable.
11. A population consists of the values $13,11,15,17$ and 18 . Consider all possible samples of size 2 by SRSWOR. Show that sample mean is an unbiased estimate of population mean.
12. The weights of a particular kind of apple sold at a fruit market are normally distributed with mean weight 100 gm and standard deviation 20 gm .
(a) Find the probability that a randomly chosen apple has weight between 70 gm and 110 gm .
(b) In one day, if 1000 apples are sold, estimate how many apple weigh greater than 110 gm ?
13. Calculate the Laspyre's index number for the following data by taking 2015 as base year.

| Commodity | 2015 |  | 2016 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Price | Quantity | Price | Quantity |
| A | 12 | 100 | 15 | 120 |
| B | 6 | 210 | 7 | 240 |
| C | 10 | 110 | 13 | 150 |

9020
4


$$
\mathrm{b}_{\mathrm{y} x}=0.23, \gamma=0.45, \sigma_{x}=10
$$


















| $x$ | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(x)$ | 0.5 | 0.3 | 0.2 |














| nowm。 | 2015 |  | 2016 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | هile |  | هile | ๙冂®๐ை゙ |
| A | 12 | 100 | 15 | 120 |
| B | 6 | 210 | 7 | 240 |
| C | 10 | 110 | 13 | 150 |

14. (a) Choose the correct answer.

The probability of rejecting $\mathrm{H}_{0}$ when it is true is called
(i) Level of confidence
(ii) Level of significance
(iii) Power of the test
(iv) None of these
(b) In the past, a machine has produced washers having a mean thickness of 0.05 cm . To determine whether the machine is in proper working, a sample of 10 washers is taken of which the mean thickness is 0.053 cm and standard deviation 0.003 cm . Test the hypothesis that the machine is working in proper order $(\alpha=0.01)$.
15. You are given the values of sample mean ( $\bar{x}$ ) and Range (R) for 10 samples of size 5 each. Construct the control limits for R-chart and comment on the state of control of the process variability.

| Sample No. | $:$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\bar{x}$ | $:$ | 43 | 49 | 37 | 44 | 45 | 37 | 51 | 46 | 43 | 47 |
| R | $:$ | 5 | 6 | 5 | 7 | 7 | 4 | 8 | 6 | 4 | 6 |

16. (a) Choose the correct answer.

Which component of time series is associated with the sale of wool in winter?
(i) Trend
(ii) Cyclic variations
(iii) Seasonal variations
(iv) Irregular variations
(b) The owner of a construction company is examining the number of homes completed in each of the last 7 months in 2017.

| Month : | June | July | August | September | October | November | December |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> Homes : | 6 | 7 | 9 | 8 | 9 | 10 | 12 |

Calculate the trend values by 3 yearly moving average method.
(Questions 17 to 21 carries 4 Scores each. Answer any 4 questions.) (Scores : $4 \times 4=16$ )
17. (a) Find the Second derivative of $\mathrm{y}=x^{3}+7 x^{2}+10 x+6$.
(b) Find k if $\int_{0}^{\mathbf{k}} x^{2} \mathrm{~d} x=9$.













 வாロロ日 கூก

| momilua mo． | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\bar{x}$ | 43 | 49 | 37 | 44 | 45 | 37 | 51 | 46 | 43 | 47 |
| R | 5 | 6 | 5 | 7 | 7 | 4 | 8 | 6 | 4 | 6 |




（i）ه（sึశ్రో


（iv）（ேவவாกிற வృகி மைாைைலิ




| ロวญ๐： | June | July | August | September | October | November | December |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ヘils మఝ゙ด ๑円円ை ： | 6 | 7 | 9 | 8 | 9 | 10 | 12 |


$(1+2)$


k

9020
P．T．O．
18. (a) From past experience it is observed that only $0.2 \%$ of the candidates are selected in a recruitment process. If 1000 candidates appeared in the test, find the probability that 3 persons are selected.
(b) The incidence of occupational decease in an industry is such that the workers have $20 \%$ chance of suffering it. What is the probability that out of 6 workers chosen at random, 4 will suffer from the decease.
19. (a) Choose the correct answer.

The variance of a chi-square variable with degrees of freedom 6 is :
(i) 3
(ii) 6
(iii) 9
(iv) 12
(b) Write any 3 relationships among Normal, $\mathrm{t}, \chi^{\mathbf{2}}$ and F variables.

$$
(1+3)
$$

20. (a) Choose the correct answer.

The test statistic ' $t$ ' is said to be an unbiased estimator for $\theta$ if $\mathrm{E}(\mathrm{t})=$ $\qquad$
(i) 0
(ii) 1
(iii) $\theta$
(iv) $\theta^{2}$
(b) $\quad x_{1}, x_{2}, x_{3}, x_{4}$ is a random sample of size 4 taken from a population with mean $\mu$ and standard deviation $\sigma$.
$\mathrm{t}_{1}=\frac{x_{1}+x_{2}+x_{3}+x_{4}}{4}$ and $\mathrm{t}_{2}=\frac{2 x_{1}+x_{2}+x_{3}+x_{4}}{5}$ are two unbiased estimates of $\mu$.
Which of them is the most efficient one ?
21. The following table shows the grades given by a doctor for 10 patients :

| Patient | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of years of <br> Smoking | 15 | 22 | 25 | 28 | 31 | 33 | 36 | 39 | 42 | 48 |
| Lung damage <br> grade | 30 | 50 | 55 | 32 | 57 | 35 | 60 | 72 | 70 | 75 |

Calculate the coefficient of rank correlation between no. of years of smoking and lung damage grade.









พிஸிிய" கวก
(i) 3
(ii) 6
(iii) 9
(iv) 12



 $\mathrm{E}(\mathrm{t})=$ $\qquad$

(i) 0
(ii) 1
(iii) $\theta$
(iv) $\theta^{2}$


$\mathrm{t}_{1}=\frac{x_{1}+x_{2}+x_{3}+x_{4}}{4}$ and $\mathrm{t}_{2}=\frac{2 x_{1}+x_{2}+x_{3}+x_{4}}{5}$





| Cou介 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| வృகா\|el msmbe வฮెกМணைวิ | 15 | 22 | 25 | 28 | 31 | 33 | 36 | 39 | 42 | 48 |
|  <br>  <br>  | 30 | 50 | 55 | 32 | 57 | 35 | 60 | 72 | 70 | 75 |



(Questions 22 to 24 carries 5 Scores each. Answer any 2 questions). (Scores: $2 \times 5=10$ )
22. (a) Fill in the blanks.

The geometric mean of regression coefficients is $\qquad$ .
(b) The price ( $x$ ) and demand (y) have the two regression equations,

$$
3 x+2 y=26 \text { and } 6 x+y=31
$$

Find (i) the correlation coefficient
(ii) the average price and average demand.
23. (a) Choose the correct answer.

ANOVA is a technique used for testing the
(i) equality of two variances.
(ii) equality of more than two variances.
(iii) equality of two means.
(iv) equality of more than two means.
(b) The following table gives the yield on 9 sample fields under three variety of seeds A, B and C.

| A | B | C |
| :---: | :---: | :---: |
| 20 | 18 | 25 |
| 21 | 20 | 28 |
| 23 | 17 | 22 |

Test whether the average yield one same at $5 \%$ level of significance.
(Table value of F at $5 \%$ level, $\mathrm{F}_{(2,6)}=5.14$ )

$$
(1+4)
$$

24. In a sample survey of public opinion, answers to the questions :
(1) Do you drink ?
(2) Are you in favour of local sale of liquor?
are tabulated below.

| Question 2 | Question 1 |  |
| :---: | :---: | :---: |
|  | Yes | No |
| Yes | 56 | 31 |
| No | 18 | 6 |

Test whether the drinking habit and the favour of local sale of liquor are independent. ( $\alpha=0.05$ ).
 อாைைのツுளைらை）．


 $\qquad$ ๔ฺறை．
（b）விఅய ถைอஸ＂，
$3 x+2 y=26$ and $6 x+y=31$











| A | B | C |
| :---: | :---: | :---: |
| 20 | 18 | 25 |
| 21 | 20 | 28 |
| 23 | 17 | 22 |








வડ̧ી

| Question 2 | Question 1 |  |
| :---: | :---: | :---: |
|  | Yes | No |
| Yes | 56 | 31 |
| No | 18 | 6 |




