## CIRCLES

## SECTION A 3 MARKS EACH

1. If two non parallel sides of a trapezium are equal then prove that it is cyclic.
2. In a cyclic trapezium prove that the non parallel sides are equal.
3. Prove that any four vertices of the regular pentagon are cyclic.
4. Prove that any cyclic parallelogram is rectangle.
5. In a right triangle prove that the sum of the lengths of the legs is equal to the sum of the diameters of the inscribed and the circumscribed circle.
6. The bisector of $<B$ of the isosceles triangle $A B C$ where $A B=A C$ meets the circle at $P$. prove that $C Q=C A$.

7. in the figure below, if $O$ is the centre rove that $x+y=z$

8. In the figure ABCD is a parallelogram, prove $\mathrm{AE}=\mathrm{AD}$.

9. In the figure AB is the diameter and CD is equal to the radius of the circle, prove that $<\mathbf{P}=60$.

10.in the figure $\mathrm{AB}=\mathrm{AP}, \mathrm{AD} \backslash \mathrm{BC}, \mathrm{AP} \backslash \backslash \mathrm{CD}$, prove that ABCD is cyclic.

11.In the figure find $a, b$ and $c$ ?

12.in the figure below, $\mathrm{AE} \backslash \backslash \mathrm{CB}$ find $<\mathrm{BCD}$ ?

13.in the figure if $y=2 x$, find $x$ ?

14.in the figure prove that
$\mathbf{C E}=\mathbf{A E}+\mathbf{B F}+\mathbf{C D}=1 / 2$ perimeter of ABC


B
D
C
15. A circle of radius 3 cm touches other circle of radius ' $r$ ' with centers $A$ and $B$ respectively. Find value of ' $r$ ' and length of perpendicular bisector of $A B$, if $A B=2 \mathrm{~cm}$ and $r>3$.
16.PQ and RS are the two parallel chords of a circle and the lines RP and SQ meet at $O$. prove $O P=O Q$

17. In the figure below $<\mathrm{ABQ}=<\mathrm{ACQ}$, Prove that $<\mathrm{AQC}=90 \mathrm{o}+112$ of $<$ BAC

18.A circle is touching the side $B C$ of a $\triangle A B C$ at $P$ and is touching $A B$ and $A C$ when produced at $Q$ and $R$ respectively. Prove that

$$
A Q=\frac{1}{2}(\text { perimeter of } \Delta \boldsymbol{A B C})
$$


19. In the figure below $S Q$ is the diameter if $<S P R=x$ and $\angle Q R P=y$, show that $x+2 y=90^{\circ}$.

20. Bisector $A$ of $\angle B A C$ of $\triangle A B C$ passes through the centre $O$ of the circum circle of $\triangle \mathrm{ABC}$ (fig-1). Prove that

$A B=A C$
Fig.-1
SECTION C 6 MARKS EACH
21.If all the sides of the parallelogram touch a circle then prove that parallelogram is a rhombus.
22.In the figure below, $\mathrm{AD} \backslash \backslash \mathrm{BE}$. Prove that $<\mathrm{DFE}=90$.

23. Two circles intercept each other at $P$ and $Q$. on $Q P$ produced there is a point $A$ from where the tangents $A B$ and $A C$ are drawn to both the circles. Prove that $\mathbf{A B}=\mathbf{A C}$.
24.In the figure below $A B=A C$, if $D$ is the mid point of $A C$, prove that $4 A P=$ AB.

25.In the figure below, $<\mathrm{ABC}=90, \mathrm{BD}$ is perpendicular to AC , prove that. a) $\mathrm{AC} \times \mathrm{AD}=\mathrm{AB}^{2}$ b) $\mathbf{A C} \times \mathbf{C D}=\mathrm{BC}^{2}$.


