

Marking Scheme

SUMMATIVE ASSESSMENT – I (2015-16)
Mathematics (Class – X)

General Instructions:

1. The Marking Scheme provides general guidelines to reduce subjectivity and maintain uniformity. The answers given in the marking scheme are the best suggested answers.
2. Marking be done as per the instructions provided in the marking scheme. (It should not be done according to one's own interpretation or any other consideration).
3. Alternative methods be accepted. Proportional marks be awarded.
4. If a question is attempted twice and the candidate has not crossed any answer, only first attempt be evaluated and 'EXTRA' be written with the second attempt.
5. In case where no answers are given or answers are found wrong in this Marking Scheme, correct answers may be found and used for valuation purpose.

खण्ड-अ / SECTION-A

प्रश्न संख्या 1 से 4 में प्रत्येक का 1 अंक है।

Question numbers 1 to 4 carry one mark each

1	$\frac{DA}{AE} = \frac{DB}{BW}$ $\frac{4}{8} = \frac{x}{24-x}$ $24-x = 2x$ $3x = 24$ $x = 8 \text{ cm} = DB = 8 \text{ cm}$	1
2	$1 + \cos^2\theta = \frac{5}{4}$	1

$$\cos^2 \theta = \frac{5}{4} - 1 = \frac{1}{4}$$

$$\theta = 60^\circ$$

3 1

1

4

C.I.	1400-1550	1550-1700	1700-1850	1850-2100
<i>f</i>	8	15	21	8
<i>c.f.</i>	8	23	44	52

1

$$\frac{\sum f}{2} = 26 \Rightarrow \text{Median class} = 1700 - 1850$$

खण्ड-ब / SECTION-B

प्रश्न संख्या 5 से 10 में प्रत्येक के 2 अंक हैं।

Question numbers 5 to 10 carry two marks each.

5

Let if possible, $2 + 3\sqrt{5}$ is rational

2

$$2 + 3\sqrt{5} = \frac{a}{b}, \text{ where } a \text{ and } b \text{ are integers and } b \neq 0$$

$$\Rightarrow \sqrt{5} = \frac{a-2b}{3b}$$

Which is contradiction as $\sqrt{5}$ is irrational and $\frac{a-2b}{3b}$ is rational

Hence $2 + 3\sqrt{5}$ is irrational

6

Let us find HCF of $70 - 5 = 65$ and $125 - 8 = 117$

2

$$Q 117 > 65$$

$$\therefore 117 = 65 \times 1 + 52$$

$$\Rightarrow 65 = 52 \times 1 + 13$$

$$\Rightarrow 52 = 13 \times 4 + 0$$

Q remainder = 0

\therefore HCF = 13.

7 $\alpha + \beta = 7$ _____ (1) 2

$$\alpha\beta = k$$
 _____ (2)

$$\alpha - \beta = 1$$
 _____ (3) (given)

(1) and (3) give $\alpha = 4, \beta = 3$

From (2), $k = 12$.

8 $\frac{AY}{AC} = \frac{AY}{AY + YC} = \frac{2}{2+6} = \frac{1}{4}, \frac{AX}{AB} = \frac{1}{4}$ 2

$$\frac{AX}{XB} = \frac{AY}{YC}$$

By converse of B.P.T., $XY \parallel BC$

9 $\frac{\operatorname{cosec} 13^\circ}{\sec 77^\circ} - \frac{\cot 20^\circ}{\tan 70^\circ} = 1 - 1 = 0$ 2

10 Getting $\sum f = 50, \sum fx = 220$ 2
Mean $\bar{x} = \frac{\sum fx}{\sum f} = \frac{220}{50} = 4.4$

खण्ड-स / SECTION-C

प्रश्न संख्या 11 से 20 में प्रत्येक के 3 अंक हैं।

Question numbers 11 to 20 carry three marks each.

- | | |
|----|---|
| 11 | Let a be any positive integer. 3 |
|----|---|

By Euclid lemma

$$a = 6q, 6q + 1, 6q + 2, 6q + 3, 6q + 4, 6q + 5$$

$$\text{Now } a^2 = 36q^2 = 6m$$

$$a^2 = (6q + 1)^2 = 36q^2 + 12q + 1 = 6(6q^2 + 2q) + 1 = 6m + 1$$

$$a^2 = (6q + 2)^2 = 36q^2 + 24q + 4 = 6m + 4$$

$$a^2 = (6q + 3)^2 = 36q^2 + 36q + 9 = 6m + 3$$

$$a^2 = (6q + 4)^2 = 36q^2 + 48q + 16 = 6m + 4$$

$$a^2 = (6q + 5)^2 = 36q^2 + 60q + 25 = 6m + 1$$



Hence square of any positive integer cannot be of the form $6m + 2$ or $6m + 5$.

- | | |
|----|---|
| 12 | Multiply (1) by 4 and (2) by 2 and add 3 |
|----|---|

$$4(5x - 2y) + 2(3x + 4y) = 11 \times 4 + 2 \times 4$$

$$26x = 52$$

$$\Rightarrow x = 2$$

$$y = -\frac{1}{2}$$

- | | |
|----|---|
| 13 | Division 3 |
|----|---|

$$\text{Quotient} = 4x - 10, \text{Remainder} = -3$$

	Verification	
14	(i) $2x + 5y = 8$ (ii) $4x - 10y = 8$ (iii) $4x - 10y = 7$	3
15	In $\triangle ABC$, $XY \parallel AB$ $\therefore \frac{AX}{XC} = \frac{AY}{YB}$ _____ (1) $\frac{AX}{XC} = 1$ (given) _____ (2)	3
	(1) and (2) give $AY = YB$ Y is middle point of AB	
16	$\triangle ABC \sim \triangle PQR$ $\frac{AB}{PQ} = \frac{BC}{QR} = \frac{CA}{RP} = \frac{\text{perimeter of } VABC}{\text{perimeter of } VPQR}$ $\frac{BC}{5} = \frac{180}{50}$	3

BC = 18 cm

17 To get $\cos \theta = \frac{8}{17}$, 3

$$\text{L.H.S} = \frac{3 - 4 \sin^2 \theta}{4 \cos^2 \theta - 3} = \frac{3 - 4 \cdot \left(\frac{15}{17}\right)^2}{4 \cdot \left(\frac{8}{17}\right)^2 - 3} = \frac{-33}{-611} = \frac{33}{611}$$

18 Getting $\frac{\sin \theta (1 - 2 \sin^2 \theta)}{\cos \theta (2 \cos^2 \theta - 1)}$ 3

$$= \frac{\tan \theta (\cos^2 \theta - \sin^2 \theta)}{(\cos^2 \theta - \sin^2 \theta)} = \tan \theta$$

19	Production more than/equal to	c.f	3
50		100	
55		98	
60		90	
65		78	
70		54	
75		16	

and ogive

20	C.I.	f_i	x_i	$u_i =$	$f_i u_i$	3
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			$\frac{x_i - a}{h}$	
20-30	8	25	-2	-1
30-40	6	35	-1	-6
40-50	x	45	0	0
50-60	11	55	1	11
60-70	y	65	2	$2y$

$$\sum f_i u_i = -20 + 11 + 2y \\ = 2y - 11$$

$$\sum f_i = 25 + x + y = 50 \Rightarrow x + y = 25$$

$$\text{Let } a = 45$$

$$\text{Mean} = a + \frac{\sum f_i u_i}{\sum f_i} \times h$$

$$48 = 45 + \frac{2y - 11}{50} \times 10$$

$$5 \times 3 = 2y - 11$$

$$y = 13$$

Put value of y in (1)

$$x = 12$$

खण्ड-द / SECTION-D

प्रश्न संख्या 21 से 31 में प्रत्येक के 4 अंक हैं।

Question numbers 21 to 31 carry four marks each.

- | | | |
|----|--|---|
| 21 | Length of the rectangular courtyard = 18.72 cm
Breadth of the rectangular courtyard = 13.20 cm
For least no. of tiles, tiles must be of maximum size
Using Euclid division
$\therefore \text{HCF}(1872, 1320) = 24 \text{ cm}$
$\therefore \text{No of tiles} = \frac{\text{Area of courtyard}}{\text{Area of one tile}}$ | 4 |
|----|--|---|

$$= \frac{1872 \times 1320}{24 \times 24}$$

$$= 4290$$

22 Let cost of 1 chair = ₹ x and cost of 1 table = ₹ y 4

$$\text{ATQ } 4x + 3y = 2100 \quad (1)$$

$$5x + 2y = 1750 \quad (2)$$

Multiplying (1) by 2 and (2) by 3

$$8x + 6y = 4200 \quad (3)$$

$$15x + 6y = 5250 \quad (4)$$

$$(4) - (3) \Rightarrow 7x = 1050 \Rightarrow x = 150$$

On putting value of x in (1), $y = 500$

Cost of chair and table = ₹ 150, ₹ 500

23 $f(x) = 4x^2 - 8kx + 8x - 9$ 4

$$= 4x^2 - 8(k-1)x - 9$$

∴ zeros are negative of each other

$$\therefore \alpha = -\beta$$

$$\Rightarrow \alpha + \beta = 0$$

$$\Rightarrow -\frac{b}{a} = 0$$

$$\Rightarrow \frac{8(k-1)}{4} = 0$$

$$\Rightarrow k-1 = 0$$

$$\Rightarrow k = 1$$

$$\therefore kx^2 + 3kx + 2$$

$$= x^2 + 3x + 2$$

$$= (x+1)(x+2)$$

$$\therefore \text{zeros} = -1, -2$$

24 Let No. of workers = $g(x)$

4

$$\therefore g(x) = \frac{p(x) - r(x)}{q(x)}$$

$$= \frac{6x^4 + 8x^3 + 17x^2 + 21x + 7 - x - 2}{2x^2 + 5}$$

$$= \frac{6x^4 + 8x^3 + 17x^2 + 20x + 5}{2x^2 + 5}$$

$$= 3x^2 + 4x + 1$$

Values - leadership, concern for fellow being.

25 In $\triangle ABC$, $DP \parallel BC$, so by B.P.T.

4

$$\frac{AD}{DB} = \frac{AP}{PC} \quad \text{--- (1)}$$

In $\triangle ABC$, $EQ \parallel AC$, so by B.P.T.

$$\frac{BE}{EA} = \frac{BQ}{QC} = \frac{AD}{EA} \quad \text{--- (2)} \quad (QAD = BE)$$

from (1) and (2)

$$AD = \frac{AP \times DB}{PC} = \frac{BQ \times EA}{CQ}$$

$$\frac{AP}{PC} = \frac{BQ}{QC} \quad (\text{Q } DB = AB - AD = AB - BE = AE)$$

So, by converse of B.P.T.

$$PQ \parallel AB$$

- 26 Given and T.P, const ; proof

4

$$AC^2 = 12^2 = 144$$

$$AB^2 + BC^2 = (6\sqrt{3})^2 + (6)^2 = 36 \times 3 + 36 = 36 \times 4 = 144$$

$$\Rightarrow AB^2 + BC^2 = AC^2 \therefore \Delta ABC \text{ is rt } \Delta \text{ at } .B$$

$$\therefore \angle B = 90^\circ$$

- 27 Changing $\cos 55^\circ$, $\tan 75^\circ$, $\tan 13^\circ$, $\tan 23^\circ$ by complimentary angle 2

4

Simplification 2

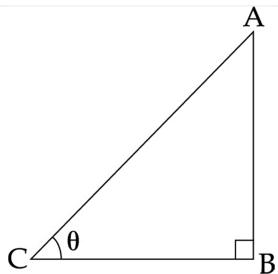
- 28 $x+y = 2 \sec A$ and $x-y = 2 \sin A$

4

$$\left(\frac{2}{x+y}\right)^2 + \left(\frac{x-y}{2}\right)^2 = \sin^2 A + \cos^2 A = 1$$

- 29

4



In ΔABC

$$AB^2 + BC^2 = AC^2$$

$$\Rightarrow \frac{AB^2}{AC^2} + \frac{BC^2}{AC^2} = 1$$

$$\Rightarrow \sin^2\theta + \cos^2\theta = 1$$

$$\text{Now } \sin^4\theta - \cos^4\theta = (\sin^2\theta)^2 - (\cos^2\theta)^2$$

$$\begin{aligned} &= (\sin^2\theta + \cos^2\theta)(\sin^2\theta - \cos^2\theta) \\ &= 1 \cdot (\sin^2\theta - \cos^2\theta) \\ &= 1 - \cos^2\theta - \cos^2\theta \\ &= 1 - 2\cos^2\theta = \text{RHS} \end{aligned}$$

30

$$\text{Mode} = l + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times i$$

$$= 45 + \frac{33 - 31}{66 - 31 - 17} \times 10$$

$$= 45 + \frac{2}{18} \times 10$$

$$= 46.1$$

4

31

C. I.	f_i	$u_i = \frac{x_i - 54}{4}$	$f_i u_i$
40-44	4	-3	-12
44-48	6	-2	-12
48-52	10	-1	-10
52-56	14	0	0
56-60	10	1	10
60-64	8	2	16
64-68	6	3	18
68-72	2	4	8

4

	$\Sigma f_i = 60$		$\Sigma f_i u_i = 18$
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Let a = assumed mean = 54

$$\text{Mean} = 54 + \frac{18}{60} \times 4 = 55.2$$

$$\text{Maximum frequency} = 14 \Rightarrow \text{Modal class} = 52 - 56$$

$$\text{Mode} = 52 + \frac{14 - 10}{28 - 10 - 10} \times 4 = 54$$

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