## GENERAL INSTRUCTIONS :

(i) Duration of Test is 3 hrs .
(ii) The Test booklet consists of 90 questions. The maximum marks are 360 .
(iii) There are three parts in the question paper A, B, C consisting of Physics, Chemistry and Mathematics having 30 questions in each part of equal weightage. Each question is allotted 4 (four) marks for each correct response.
(iv) One fourth ( $1 / 4$ ) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
(v) Pattern of the Questions :

Section - I : Straight Objective Questions; Section - II : Assertion - Reason Type Questions
[PART-A:PHYSICS]

## SECTION - I

## Straight Objective Questions

This section contains 25 multiple choice questions numbered 1 to 25 . Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

## Choose the correct answer :

1. For a circular motion, select correct option.
(1) $\vec{v}=\vec{\omega} \times \vec{r}$
(2) $\vec{v}=\vec{r} \times \vec{\omega}$
(3) $\vec{a}_{T}=\vec{r} \times \vec{\alpha}$
(4) $\vec{a}_{c}=\frac{d}{d t}|\vec{v}|$
(Where all the symbols have their usual meaning)
2. A particle is projected with velocity $u$ at an angle with horizontal. After a time of $\frac{u}{g \sqrt{3}}$ (in seconds), the direction of motion makes an angle of $30^{\circ}$ with the horizontal. Find the angle with horizontal at which particle is projected.
(1) $75^{\circ}$
(2) $60^{\circ}$
(3) $45^{\circ}$
(4) $30^{\circ}$
3. Find the acceleration of 1 kg block as shown in figure.

(1) $5 \mathrm{~ms}^{-2}$
(2) $\frac{10}{3} \mathrm{~ms}^{-2}$
(3) $10 \mathrm{~ms}^{-2}$
(4) $\frac{5}{3} \mathrm{~ms}^{-2}$
4. A block of mass $m \mathrm{~kg}$ is placed in an elevator on a horizontal surface. The elevator is moving at an acceleration of $6 \hat{i}+7 \hat{j}$ (in $\mathrm{m} / \mathrm{s}^{2}$ ). Find the frictional force acting on the block. ( $g=10 \mathrm{~m} / \mathrm{s}^{2}$ and $\mu=0.5$ )
(1) 6 m newton
(2) $7 m$ newton
(3) $8 m$ newton
(4) 8.5 m newton
5. Block $A$ of mass $m$ can slide on rough surface of block $B$ of same mass. The block $B$ moves on a smooth horizontal surface. The coefficient of friction between $A$ and $B$ is $\mu$. Find the required force in horizontal direction by which block $A$ is pulled so that both the blocks move together.

(1) Any value
(2) $\frac{1}{2} \mu m g \cos ^{2} \theta$
(3) $2 \mu \mathrm{mg} \cos ^{2} \theta$
(4) $2 m g \cos \theta(\mu \cos \theta+\sin \theta)(\cos 2 \theta-\mu \sin 2 \theta)$
6. A particle is dropped from height $H$. At a point, its kinetic energy is $x$ times of its potential energy. Find the speed of the particle at that point.
(1) $[2 g x H]^{1 / 2}$
(2) $\left[2 g \frac{(x+1) H}{x}\right]^{1 / 2}$
(3) $\left[\frac{2 g H}{x+1}\right]^{1 / 2}$
(4) $\left[\frac{2 g x H}{x+1}\right]^{1 / 2}$
7. A particle of mass $m_{1}$ collides head on with a stationary particle of mass $m_{2}$. If $\frac{m_{1}}{m_{2}}>e$, where $e$ is the coefficient of restitution, then
(1) $m_{1}$ will return back
(2) $m_{1}$ will move in same direction
(3) $m_{1}$ will stop
(4) Unpredictable
8. A sphere of radius $r$ starts pure rolling on a rough horizontal surface with translational velocity $v_{0}$, rotating with angular velocity $\omega$ in clockwise direction. A particle of mass $m$ sticking with sphere at $A$ with $O A=\frac{r}{2}$ in the start of the motion gets detached at position $B$. What will be velocity of particle at $B$ ?

(1) $\frac{v_{0}}{2}$ to the left
(2) $\frac{v_{0}}{2}$ to the right
(3) $v_{0}$ to the left
(4) $\frac{\omega r}{2}$ to the left
9. On an inclined plane of angle $60^{\circ}$ with horizontal, a rigid body rolls down the plane from the rest without slipping. It has a linear acceleration equal to $\frac{g}{\sqrt{3}}$. Find the rigid body.
(1) Sphere
(2) Spherical shell
(3) Disc
(4) Ring
10. The mass of a satellite is $\frac{M}{81}$ and radius is $\frac{R}{4}$ where $M$ and $R$ are the mass and radius of its planet. The distance between surface of planet and its satellite will be at least greater than
(1) $1.25 R$
(2) $12.5 R$
(3) $10.5 R$
(4) $5 R$
11. A shell loses its weight in water. If $X$ is the fraction of its volume which is hollow and $W$ is the weight of water displaced. Find the correct graph.
(1)

(2)

(3)

(4)

12. A mass $m$ is undergoing SHM in vertical direction about the mean position with amplitude $A$ and angular velocity $\omega$. At a distance $y$ from the mean position, the mass detaches from the spring. Assume that the spring contracts and does not obstruct the motion of $m$. Find the distance $y_{0}$ (measured from the mean position) such that the height attained by the block is maximum $\left(A \omega^{2}>g\right)$
(1) $\frac{g}{\omega^{2}}$
(2) $\frac{2 g}{\omega^{2}}$
(3) $\frac{g}{2 \omega^{2}}$
(4) $\frac{2 \sqrt{2} g}{\omega^{2}}$
13. A satellite in equitorial plane is rotating in the direction of earth's rotation with time interval between its two consecutive appearances overhead of an observer as time period of rotation of the earth, $T_{E}$. What is the time period of the satellite?
(1) $T_{E}$
(2) $2 T_{E}$
(3) $\frac{T_{E}}{2}$
(4) $\frac{2 T_{E}}{3}$
14. A particle executes S.H.M. between amplitude $+A$ and $-A$. Find the position $+x$ of particle such that time taken by it from 0 to $+x$ and to go from $+x$ to $+A$ is same. The time is considered from equilibrium position
(1) $\frac{A}{2}$
(2) $\frac{A}{\sqrt{2}}$
(3) $\frac{A}{2 \sqrt{2}}$
(4) $\frac{A \sqrt{2}}{4}$
15. Phase difference between displacement and acceleration in SHM, is
(1) $\frac{\pi}{2}$
(2) $\pi$
(3) $\frac{3 \pi}{2}$
(4) Zero
16. Which of the following graphs correctly represents the variation of $\beta=-\frac{(d V / d P)}{V}$ with $P$ for an ideal gas at constant temperature?
(1)

(2)

(3)

(4)

17. A hemispherical surface of radius $R$ is placed with its cross section perpendicular to a uniform electric field $\vec{E}$ as shown. Flux linked with its curved surface is
(1) Zero
(2) $2 \pi R^{2} E$
(3) $\pi R^{2} E$
(4) $\frac{E}{2 \varepsilon_{0}}$
18. Two capacitors of capacitance $C$ and $\frac{C}{2}$ are connected with a $V$ volt battery, as shown


The work done in charging fully both the capacitors, is
(1) $2 C V^{2}$
(2) $\frac{1}{4} \mathrm{CV}^{2}$
(3) $\frac{3}{2} C V^{2}$
(4) $\frac{1}{2} C v^{2}$
19. The electric potential at a point $(x, y, z)$ is given by $V=-x^{2} y-x z^{3}+4$. The electric field at that point is
(1) $\vec{E}=\left(2 x y-z^{3}\right) \hat{i}+x y^{2} \hat{j}+3 z^{2} x \hat{k}$
(2) $\vec{E}=\left(2 x y+z^{3}\right) \hat{i}+x^{2} \hat{j}+3 x z^{2} \hat{k}$
(3) $\vec{E}=2 x y \hat{i}+\left(x^{2}+y^{2}\right) \hat{j}+\left(3 x z-y^{2}\right) \hat{k}$
(4) $\vec{E}=23 \hat{i}+x y z \hat{j}+z^{2} \hat{k}$
20. Potentiometer wire of length 1 m is connected in series with $490 \Omega$ resistance and 2 V battery. If $0.01 \mathrm{~V} / \mathrm{cm}$ is the potential gradient, then resistance of potentiometer wire is
(1) $490 \Omega$
(2) $790 \Omega$
(3) $590 \Omega$
(4) $690 \Omega$
21. The angle of dip at the magnetic equator is
(1) $0^{\circ}$
(2) $90^{\circ}$
(3) $45^{\circ}$
(4) $180^{\circ}$
22. In the figure shown, $X$ and $Y$ are two identical bulbs then

(1) Bulb $X$ glows brighter than $Y$
(2) Bulb $Y$ glows brighter than $X$
(3) Both glow with equal brightness
(4) Which glows brighter cannot be predicted
23. A concave and a convex lens have the same focal length of 20 cm and are put in contact to form a lens combination. The combination is used to view an object of 5 cm length kept at 20 cm from the lens combination as compared to the object, the image will be
(1) Magnified and inverted
(2) Reduced and erect
(3) Of the same size as the object and would be erect
(4) Of the same size as the object but would be inverted
24. The wavelength of radiation emitted is $\lambda_{0}$ when an electron in hydrogen atom jumps from $3^{\text {rd }}$ to $2^{\text {nd }}$ orbit. If in the hydrogen atom itself, the electron jumps from $4^{\text {th }}$ orbit to $2^{\text {nd }}$ orbit, wavelength of emitted radiation will be
(1) $\frac{25}{16} \lambda_{0}$
(2) $\frac{17}{20} \lambda_{0}$
(3) $\frac{20}{27} \lambda_{0}$
(4) $\frac{16}{25} \lambda_{0}$
25. To use a transistor as an amplifier
(1) Both emitter-base and collector base junctions are forward biased
(2) Both emitter-base junction and collector base junction are reverse biased
(3) Emitter base junction is forward biased and collector base junction is reverse biased
(4) Collector base junction is forward biased and emitter-base junction is reverse biased

## SECTION - II

## Assertion - Reason Type Questions

Directions: Questions number 26 to 30 are AssertionReason type questions. Each of these questions contains two statements. Statement-1 (Assertion) and Statement-2 (Reason). Each of these questions also has four alternative choices, only one of which is the correct answer. You have to select the correct choice.
26. Statement-1 : In series LCR a.c. circuit, at resonance, current and voltage are in same phase.
and
Statement-2 : In series LCR circuit, resonance frequency does not depend on the value of resistance and hence current at resonance, does not depend on resistance.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True
27. Statement-1 : When monochromatic light is incident on a metal, the kinetic energy of the emitted photoelectrons are different.

## and

Statement-2 : Kinetic energy of emitted photoelectrons from inside the metallic surface, varies due to their collision with other atoms in the metal.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True
28. Statement-1 : Electromagnetic waves with frequencies more than the critical frequency of ionosphere, cannot be used for communication, using sky wave propagation.

## and

Statement-2 : The refractive index of the ionosphere becomes very high for frequencies higher than the critical frequency.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True
29. Statement-1 : Electric field strength due to symmetric charge distributions can be determined using Gauss' law.
and
Statement-2 : Gauss law is valid only for symmetric charge distributions.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement- 2 is True
30. Statement-1 : In adiabatic expansion, temperature of gas always decreases
and
Statement-2 : In adiabatic process, exchange of heat is zero.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True

## [PART-B : CHEMISTRY]

## SECTION - I

## Straight Objective Questions

This section contains 25 multiple choice questions numbered 31 to 55 . Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.
31. $\mathrm{K}_{\mathrm{sp}}$ of AgCl and AgBr is respectively $10^{-10}$ and $10^{-13}$ then what will be equilibrium constant of reaction given?
$\mathrm{Cl}^{-}(\mathrm{aq})+\mathrm{AgBr}(\mathrm{s}) \rightleftharpoons \mathrm{Br}^{-}(\mathrm{aq})+\mathrm{AgCl}(\mathrm{s})$
(1) $10^{-3}$
(2) $10^{3}$
(3) $10^{6}$
(4) 1
32. White $\mathrm{P} \xrightarrow[\text { Combustion }]{\text { Air }} \mathrm{A} \xrightarrow{\mathrm{H}_{2} \mathrm{O}} B$

Basicity of acid will be
(1) 2 only
(2) 3 only
(3) 1 only
(4) 2 and 3 only
33. Which of the following have highest melting point? (All are dissolved in 1 kg solvent)
(1) 1 mole $\mathrm{CH}_{3} \mathrm{COOH}$
(2) 1 mole ${\underset{C l}{C l}}_{\mathrm{CH}_{2}}-\mathrm{COOH}$
(3) 1 mole $\mathrm{CCl}_{3}-\mathrm{COOH}$
(4) Equal in all of these
34. Choose correct statement regarding NaCl structure
(1) $\mathrm{Cl}^{-}$shows ccp packing
(2) $\mathrm{Na}^{+}$shows ccp packing
(3) Number of $\mathrm{Cl}^{-}$per unit cell is 4
(4) All of these
35. n factor of $\mathrm{KMnO}_{4}$ as oxidizing agent in acidic medium will be
(1) 0
(2) 1
(3) 3
(4) 5
36. Choose the correct pair regarding entropy
(1) $\mathrm{H}_{2} \mathrm{O}_{2}$ (gas) $>\mathrm{H}_{2} \mathrm{O}_{2}$ (liquid)
(2) $\mathrm{H}_{2} \mathrm{O}>\mathrm{H}_{2} \mathrm{O}_{2}$ (gas)
(3) $\mathrm{H}_{2} \mathrm{O}>\mathrm{H}_{2} \mathrm{O}_{2}$ (liquid)
(4) $\mathrm{CH}_{4}>\mathrm{C}_{2} \mathrm{H}_{6}$
37. The quantum number can be used to calculate spherical node in an orbital
(1) $n$ and $m$
(2) $I$ and $m$
(3) $n$ and $s$
(4) $n$ and $I$
38. Correct sequence regarding energy of molecule orbital in CO is
(1) $\sigma 1 s<\sigma^{*} 1 s<\sigma 2 s<\sigma^{*} 2 s<\pi 2 p_{x}=\pi 2 p_{y}$
(2) $\sigma 1 s<\sigma^{*} 1 s<\sigma 2 s<\pi 2 p_{x}=\pi 2 p_{y}<\sigma^{*} 2 s$
(3) $\sigma 1 \mathrm{~s}<\sigma^{*} 1 \mathrm{~s}<\sigma^{*} 2 \mathrm{~s}<-2 p_{z}<\pi 2 p_{x}=\pi 2 p_{y}$
(4) $\sigma 1 s<\sigma^{*} 1 s<-2 p_{z}<\sigma^{*} 2 s<\pi 2 p_{x}$
39. The most stable free radical is
(1)

(2)

(3)

(4)

40. Out of the following which complex is paramagnetic?
(1) $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{6}\right]^{+3}$
(2) $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{-4}$
(3) $\left[\mathrm{Cr}(\mathrm{CN})_{6}\right]^{-3}$
(4) $\mathrm{V}(\mathrm{CO})_{6}^{-}$
41. The compound which can exhibit geometrical isomerism?
(1) $\mathrm{N}_{2} \mathrm{~F}_{2}$
(2) $\mathrm{CH}_{3}-\mathrm{CH}=\mathrm{C}=\mathrm{C}=\mathrm{CH}-\mathrm{CH}_{3}$
(3)

(4) All of these
42.


Product B in this reaction is
(1)

(2)

(3)

(4)

43. Wilkinson catalyst is
(1) $\mathrm{PtCl}_{3}\left(\mathrm{C}_{2} \mathrm{H}_{4}\right)^{-}$
(2) $\left[\mathrm{Rh}\left(\mathrm{PPh}_{3}\right)_{3} \mathrm{Cl}\right]$
(3) $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$
(4) $\mathrm{Fe}_{4}\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]_{3}$
44. Which of the following is a polymer of $\beta$ glucose?
(1) Cellulose
(2) Starch
(3) Maltose
(4) Glactose
45. In given, which compounds can act as Lewis acid?
a. $\mathrm{BCl}_{3}, \mathrm{BeCl}_{2}$
b. $\mathrm{PCl}_{3}, \mathrm{XeF}_{2}, \mathrm{AlBr}_{3}$
c. $\mathrm{B}(\mathrm{OH})_{3}, \mathrm{XeF}_{4}, \mathrm{PCl}_{5}$
(1) $a \& b$
(2) $a \& c$
(3) $a, b \& c$
(4) $b \& c$
46.


Total number of expected product (excluding stereoisomer) formed in this reaction
(1) 2
(2) 1
(3) 4
(4) 3
47. Which of the following undergo/goes Cannizzaro reaction?
(1)

(2)

(3)

(4) Both (2) \& (3)
48. In zero order, 1st order and 2nd order reactions the initial half life periods are same for all these reactions, then which show(s) 99.99\% completion in minimum time?
(1) 1st order
(2) 2nd order
(3) Zero order
(4) Equal in all these
49. Which one of the following shows highest solubility in hot conc. NaOH ?
(1) $\mathrm{La}(\mathrm{OH})_{3}$
(2) $\mathrm{Nb}(\mathrm{OH})_{3}$
(3) $\mathrm{Sm}(\mathrm{OH})_{3}$
(4) $\mathrm{Lu}(\mathrm{OH})_{3}$
50. Kohlrausch's law is applicable to a dilute solution of
(1) KCl in hexane
(2) Acetic acid in hexane
(3) HCl in water
(4) Benzoic acid in benzene
51. A dilute silver nitrate solution is added to a slight excess of Nal, a solution of Agl is formed whose surface absorb
(1) $\vdash$
(2) $\mathrm{NO}_{3}^{-}$
(3) $\mathrm{Na}^{+}$
(4) $\mathrm{Ag}^{+}$
52. The correct order of acidity of the compounds is
I.

II.

III.

(1) I $>$ II $>$ III
(2) II $>$ III $>$ I
(3) III $>$ I $>$ II
(4) II $>$ I $>$ III
53. Out of following most soluble compound
(1) $\mathrm{NaHCO}_{3}$
(2) $\mathrm{KHCO}_{3}$
(3) $\mathrm{RbHCO}_{3}$
(4) $\mathrm{CsHCO}_{3}$
54.


How many different products expected in this reaction?
(1) 1
(2) 3
(3) 2
(4) 4
55. Biodegradable polyamide polymer is
(1) Nylon 2 nylon 6
(2) PHBV
(3) Teflon
(4) Both (1) \& (2)

## SECTION - II

## Assertion - Reason Type Questions

Directions : Questions number 56 to 60 are AssertionReason type questions. Each of these questions contains two statements. Statement-1 (Assertion) and Statement-2 (Reason). Each of these questions also has four alternative choices, only one of which is the correct answer. You have to select the correct choice.
56. Statement-1 : When KCl is heated, lilae (blue colour) appear.
and
Statement-2 : On heating, ZnO becomes yellow.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True
57. Statement-1 : For the detection of nitrogen in pyridine Duma method can be used.
and
Statement-2 : Pyridine is aromatic.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True
58. Statement-1 : $1^{\circ}$ amine and $2^{\circ}$ amine can be distinguished by carbylamine reaction.
and
Statement-2 : In carbylamine reaction, carbene is reaction intermediate.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement- 1 is False, Statement- 2 is True
59. Statement-1: $\mathrm{BF}_{3}$ is more acidic than $\mathrm{BCl}_{3}$. and

Statement-2 : F is more electronegative than Cl .
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True
60. Statement-1 : Solid $\mathrm{PBr}_{5}$ is ionic compound.
and
Statement-2 : In solid state of $\mathrm{PBr}_{5}$, hybridization of $P$ is $s p^{3} d$.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True

## [PART-C: MATHEMATICS]

## SECTION - I

## Straight Objective Questions

This section contains 25 multiple choice questions numbered 61 to 85 . Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.
61. Let $p$ be the statement, " $x$ is an irrational number", $q$ be the statement, " $y$ is a prime number" and $r$ be the statement, " $x$ is a rational iff $y$ is not a prime number", then $r$ is equivalent to
(1) $\sim(p \leftrightarrow q)$
(2) $p \leftrightarrow q$
(3) $\sim p \leftrightarrow q$
(4) $p \leftrightarrow \sim q$
62. If $\omega$ is a non-real cube root of unity, then the value of the expression

$$
\begin{aligned}
& (1-\omega)\left(1-\omega^{2}\right)+2(2-\omega)\left(2-\omega^{2}\right) \\
& \quad+3(3-\omega)\left(3-\omega^{2}\right)+\ldots . n \text { times }
\end{aligned}
$$

is
(1) $\frac{n(n+1)\left(3 n^{2}+7 n+8\right)}{12}$
(2) $\frac{1}{4} n^{2}(n+1)^{2}+n$
(3) $\frac{1}{4} n(n+1)^{2}-n$
(4) $\frac{1}{4} n(n+1)^{2}+n$
63. The number of real values of $x$ which satisfy the equation $\left|\frac{x}{x+1}\right|+x=\left|\frac{x^{2}}{x+1}\right|$ is
(1) 0
(2) 1
(3) 2
(4) 3
64. The value of the series $5 \times 1^{4}+5 \times 2^{4}+5 \times 3^{4}+$ $\ldots+5 \times n^{4}$ is equal to
(1) $\frac{1}{6} n(n+1)(2 n+1)\left(3 n^{2}+1\right)$
(2) $\frac{1}{6} n(n+1)(2 n+1)\left(3 n^{2}-1\right)$
(3) $\frac{1}{6} n(n+1)(2 n+1)\left(3 n^{2}+3 n-1\right)$
(4) $\frac{1}{6} n(n+1)(2 n+1)\left(3 n^{2}+2 n-1\right)$
65. The sum of all real roots of the equation

$$
\log _{2}\left(3^{2 x-2}+7\right)=2+\log _{4}\left(3^{2 x-2}+2.3^{x-1}+1\right)
$$

is
(1) 0
(2) 1
(3) 2
(4) 3
66. The number of real values of $x$ of the equation $x^{2}=\left[x^{2}\right]+[x]$ is
(1) 0
(2) 1
(3) 2
(4) Infinite
67. If $m$ and $n$ are two integers lying between 1 and 200, then how many different numbers of the form $7^{m}+7^{n}$ is divisible by $10 ?$
(1) 2000
(2) 20000
(3) 40000
(4) 10000
68. The value of $n$ for which coefficients of $x^{7}$ and $x^{8}$ are equal in the expansion of $\left(3+\frac{x}{2}\right)^{n}$ is
(1) 45
(2) 35
(3) 55
(4) 65
69. Let $S$ denotes the set of all different values of $\alpha$ for which the system of equations, $\alpha x+y+z=0$, $x+\alpha y+z=0$ and $x+y+\alpha z=0$ has infinite number of solutions, then $\sum_{i \in S} \alpha_{i}$ is equal to
(1) 1
(2) 3
(3) 2
(4) -1
70. A bag contains three tickets numbered 1,2 and 3. A ticket is drawn at random and put back in the bag and this is done four times. The probability that the sum of the numbers drawn is odd, is
(1) $\frac{40}{81}$
(2) $\frac{41}{81}$
(3) $\frac{14}{27}$
(4) $\frac{13}{81}$
71. If $\vec{a}$ and $\vec{b}$ are two unit vectors inclined at angle $\theta$ to each other and $|\vec{a}-\vec{b}|<\sqrt{2}$, then $\theta$ lies between
(1) $\left[0, \frac{\pi}{2}\right)$
(2) $\left(\frac{\pi}{2}, \pi\right]$
(3) $\left(\frac{2 \pi}{3}, \pi\right)$
(4) $\frac{\pi}{2}$
72. If $f(x)=g^{-1}(x)$ and $g(x)=x^{3}+\sqrt{e^{x}}$, then the value of $f^{\prime}(1)$ is equal to
(1) 1
(2) 2
(3) 3
(4) 0
73. The number of points, where the function $f(x)=x|x|$ is not differentiable, is/are
(1) 0
(2) 1
(3) 2
(4) Infinite
74. The value of $\int_{0}^{\pi / 2} \frac{\sin 8 x \cdot \log (\cot x)}{\cos 2 x} d x$ is equal to
(1) $\pi$
(2) $2 \pi$
(3) 0
(4) $\frac{\pi}{2}$
75. The value of $\int_{4}^{8} \frac{\log x}{x} d x$ is
(1) $\log 2$
(2) $\frac{1}{2}(\log 2)(\log 32)$
(3) $\log 32$
(4) $\frac{\log 32}{\log 2}$
76. The solution of the differential equation $x^{2} \frac{d y}{d x}+x y=\sin x$ is
(1) $y=\frac{1}{x} \int \frac{\sin x}{x} d x+c$
(2) $y=\frac{c}{x}+\int \frac{\sin x}{x} d x$
(3) $y=\frac{c}{x}+\frac{2}{x} \int \frac{\sin x}{x} d x$
(4) $y=\frac{c}{x}+\frac{1}{x} \int \frac{\sin x}{x} d x$
77. If $I=\int \operatorname{cosec}^{4} x \cdot \sec ^{2} x d x$

$$
=\alpha \tan x+\beta \cot ^{3} x-\gamma \cot x+c,
$$

then the value of $\alpha+3 \beta+\gamma$ is
(1) 2
(2) -2
(3) 0
(4) 1
78. If the tangent at $P(1,1)$ on $y^{2}=x(x-2)^{2}$ meets the curve again at $Q$, then the distance between $P$ and $Q$ is
(1) $\frac{5 \sqrt{5}}{4}$
(2) $\frac{5 \sqrt{5}}{8}$
(3) $\frac{5 \sqrt{5}}{16}$
(4) $\frac{5 \sqrt{5}}{2}$
79. If $f(x)=|x+3|-|x|+|x-1|$, then which one of the following option is not true?
(1) $f(x)>0$ for all real values of $x$
(2) $f(x)$ has a local maximum at $x=0$
(3) $f(x)$ has a local maximum at $x=-3$
(4) $f(x)$ has a local minimum at $x=1$
80. A natural number $x$ is chosen at random from the first hundred natural numbers, then the probability that $x$ satisfies $\frac{\left(x^{2}+1\right)(x-10)(x-40)}{\left(x^{2}+9\right)^{100}(x-30)^{2}(x-20)^{201}} \geq 0$ is
(1) $\frac{61}{100}$
(2) $\frac{11}{100}$
(3) $\frac{70}{100}$
(4) $\frac{71}{100}$
81. If $f(x)= \begin{cases}\frac{A \sin x+B \sin 2 x+\sin 3 x}{x^{5}} & , x \neq 0 \\ 1 & , x=0\end{cases}$
is continuous at $x=0$, then the value of $A+B$ is
(1) 0
(2) 1
(3) 2
(4) 3
82. The function $f: R \rightarrow R$ given by $f(x)=3 x-2 \sin x$ is
(1) Bijective
(2) Into
(3) Even
(4) Many one
83. The equation of tangents to the hyperbola $3 x^{2}-y^{2}=3$ which are parallel to the line $y=2 x$ are
(1) $y=2 x+3$ and $y=2 x+2$
(2) $y=2 x+1$ and $y=2 x-1$
(3) $y=2 x+3$ and $y=2 x+1$
(4) $y=2 x+2$ and $y=2 x-1$
84. A circle $C_{1}$ of radius 2 units rolls on the outside of the circle $C_{2}: x^{2}+y^{2}+4 x=0$, touching it externally, if $C_{3}$ is the locus of centre of outer circle $C_{1}$, then the area of the quadrilateral formed by a pair of tangents from a point on $\mathrm{C}_{3}$ to the circle $C_{2}$ with a pair of radii at the points of contact of tangent is
(1) $4 \sqrt{3}$ square units
(2) $3 \sqrt{3}$ square units
(3) $2 \sqrt{3}$ square units
(4) $\sqrt{3}$ square units
85. If one of the lines given by the equation $2 x^{2}+\alpha x y+3 y^{2}=0$ coincide with one of the lines given by $2 x^{2}+\beta x y-3 y^{2}=0$ and other lines represented by them be perpendicular, then the value of $\alpha+\beta$ is
(1) -4
(2) 4
(3) 6
(4) -2

## SECTION - II

## Assertion - Reason Type Questions

Directions : Questions number 86 to 90 are AssertionReason type questions. Each of these questions contains two statements. Statement-1 (Assertion) and Statement-2 (Reason). Each of these questions also has four alternative choices, only one of which is the correct answer. You have to select the correct choice.
86. Statement-1 : The variance of the first $n$ natural numbers is $\frac{n^{2}-1}{12}$.
and
Statement-2 : The sum of first $n$ natural numbers is $\frac{n(n+1)}{2}$ and the sum of squares of first $n$ natural numbers is $\frac{n(n+1)(2 n+1)}{6}$.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True
87. Statement-1 : $(p \vee \sim q) \vee(\sim p \vee q)$ is a tautology. and

Statement-2 : $(p \wedge \sim q) \wedge(\sim p \wedge q)$ is a contradiction.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True
88. Statement-1 : $3 \sin ^{-1}\left(\frac{1}{3}\right)+\sin ^{-1}\left(\frac{3}{5}\right)<\frac{2 \pi}{3}$ and $\tan ^{-1}(2 \sqrt{3}-1)>\frac{\pi}{3}$.
and
Statement-2: $2 \cos ^{-1} x=\cos ^{-1}\left(2 x^{2}-1\right)$ if
$0 \leq x \leq 1$.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True
89. Statement-1 : If $\frac{\sin ^{4} x}{2}+\frac{\cos ^{4} x}{3}=\frac{1}{5}$, then $\tan ^{2} x=\frac{1}{3}$.
and
Statement-2 : $\sin ^{2} x+\cos ^{2} x=1$, for all $x \in R$.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True
90. Statement-1: In a $\triangle A B C$, if

$$
\frac{2 \cos A}{a}+\frac{\cos B}{b}+\frac{2 \cos C}{c}=\frac{a^{2}+b^{2}}{a b c}
$$

then angle $B$ is $90^{\circ}$.
and
Statement-2 : In a $\triangle A B C, \cos A=\frac{b^{2}+c^{2}-a^{2}}{2 b c}$.
(1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
(2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
(3) Statement-1 is True, Statement-2 is False
(4) Statement-1 is False, Statement-2 is True

## Aakash <br> Medical||ITT-JEE|Foundations <br> (Divisions of Aakash Educational Services Ltd.)

Regd. Office : Aakash Tower, Plot No.-4, Sec-11, MLU, Dwarka, New Delhi-110075
Ph.: 011-47623456 Fax : 011-47623472
MOCK TEST
for
JEE (MAIN)
ANSWERS

| Physics |  | Chemistry |  | Mathematics |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | (1) | 31. | (1) | 61. | (2) |
| 2. | (2) | 32. | (1) | 62. | (1) |
| 3. | (2) | 33. | (3) | 63. | (2) |
| 4. | (1) | 34. | (4) | 64. | (3) |
| 5. | (4) | 35. | (4) | 65. | (4) |
| 6. | (4) | 36. | (1) | 66. | (2) |
| 7. | (2) | 37. | (4) | 67. | (4) |
| 8. | (2) | 38. | (2) | 68. | (3) |
| 9. | (3) | 39. | (4) | 69. | (4) |
| 10. | (1) | 40. | (3) | 70. | (1) |
| 11. | (1) | 41. | (4) | 71. | (1) |
| 12. | (1) | 42. | (1) | 72. | (2) |
| 13. | (3) | 43. | (2) | 73. | (1) |
| 14. | (2) | 44. | (1) | 74. | (3) |
| 15. | (2) | 45. | (3) | 75. | (2) |
| 16. | (1) | 46. | (3) | 76. | (4) |
| 17. | (3) | 47. | (4) | 77. | (1) |
| 18. | (3) | 48. | (3) | 78. | (2) |
| 19. | (2) | 49. | (4) | 79. | (3) |
| 20. | (1) | 50. | (3) | 80. | (4) |
| 21. | (1) | 51. | (1) | 81. | (2) |
| 22. | (2) | 52. | (3) | 82. | (1) |
| 23. | (3) | 53. | (4) | 83. | (2) |
| 24. | (3) | 54. | (4) | 84. | (1) |
| 25. | (3) | 55. | (1) | 85. | (3) |
| 26. | (3) | 56. | (2) | 86. | (1) |
| 27. | (1) | 57. | (4) | 87. | (2) |
| 28. | (1) | 58. | (4) | 88. | (2) |
| 29. | (3) | 59. | (4) | 89. | (4) |
| 30. | (2) | 60. | (3) | 90. | (4) |

