## ANSWER KEYS

## CHEMISTRY

1. a 2.a
2. b
3. b
4. d
5. d 7.a
$\begin{array}{lll}\text { 8. b } & \text { 9.a } & \text { 10. } \mathrm{c} \\ \text { 11.a }\end{array}$
12.b 13. a
14.a 15.d
6. d 17.a
18.a 19. c 20.d
7. d
8. c
23.a 24.a
25.a 26. c
9. d 28.b 29.c 30.b

## PHYSICS

 27. c 28.b 29.b $30 . \mathrm{c}$
## MATHEMATICS

| 1. d | 2. C | 3. b | 4. b | 5. d | 6. d | 7. c | 8. C | 9. d | 10. d | 11. b | 12. d | 13. a |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 14. a | 15. b | 16. a | 17. b | 18. d | 19. b | 20. a | 21. a | 22. c | 23. a | 24. d | 25. b | 26. c |
| 27. b | 28. a | 29. d | 30. a |  |  |  |  |  |  |  |  |  |

## CHEMISTRY

## Sol 1.

In option (1) 0.5 mole of HCI in solution is neutralized by 0.25 mole of NaOH , heat liberated $\Delta \mathrm{H}_{1}=$ $1 / 4$ of 57.1 kJ . In option (2) $\mathrm{HNO}_{3}$ is in combination of 0.2 mole of $\mathrm{HNO}_{3}$ with 0.2 mole of KOH solution; heat liberated $\Delta \mathrm{H}_{2}=1 / 5$ of 57.1 kJ . In option 1 and 2 , therefore less amount of heat is released.

## Sol 2.

The standard reduction electrode potential of zinc electrode is most negative, so this metal can undergo oxidation most easily and thus can displace tin, lead and copper from their aqueous solution.

## Sol 3.

The electron energy in a hydrogen atom is given as
$\mathrm{E}_{\mathrm{n}}=\frac{-2 \pi^{2} m e^{4} z^{2}}{n^{2} h^{2}}$
$E_{n}=\frac{-1312}{n^{2}} \mathrm{~kJ} / \mathrm{mol} \frac{-1312}{2^{2}}=-328 \mathrm{~kJ} / \mathrm{molor} 3.28 \times 10^{5} \mathrm{~J} / \mathrm{mol}$

## Sol 4.

Volume occupied in a FCC structure $=74 \%$ the percent of void space $=100-74=26 \%$

## Sol 5.

For the reaction, $A_{2}(g)+2 B_{2}(g)=4 C(g) K=\frac{[c]^{4}}{\left[A_{2}\right]\left[B_{2}\right]^{2}}$
For backward reaction $\frac{1}{k}=\frac{\left[A_{2}\right]\left[B_{2}\right]^{2}}{[c]^{4}}$
For the reaction: $2 \mathrm{C}(\mathrm{g}) \rightleftharpoons 1 / 2 \mathrm{~A}_{2}(\mathrm{~g})+\mathrm{B}_{2}(\mathrm{~g}) ; \mathrm{K}^{\prime}=\frac{\left[A_{2}\right]^{1 / 2}\left[B_{2}\right]}{[C]^{2}}=\frac{1}{\sqrt{K}}=\frac{1}{\sqrt{2}}$
Sol 6.
A buffer solution is one which resists changes in pH when small quantities of an acid or an alkali are added to it.

## Sol 7.

For a second order reaction; Rate $=k[A]^{2}$
$5 \times 10^{-5}=\mathrm{k}(0.25)^{2}=\mathrm{kx} 0.0625$
$\mathrm{k}=5 \times 10^{-5} / 0.625 \times 10^{-1}=8 \times 10^{-4} \mathrm{~mol}^{-1}$

## Sol 8.

Chemiluminescence is the emission of light (luminescence), as the result of a chemical reaction, as the result of a chemical reaction, Reverse of it is the absorption of light for a chemical reaction, i.e., a photochemical reaction

## Sol 9.

$\mathrm{O}_{2}$ has unpaired electrons in antibonding molecular orbital.

## Sol 10.

The pH a buffer solution containing 0.1 m acetic acid and 0.01 M sodium acetate can be calculated as

$$
p H=p K_{a}+\log \frac{[\text { salt }]}{[\text { salt }]}
$$

$=4.74+\log \frac{0.1}{0.01}=4.74+\log 10^{-1}$
$=4.74-1=3.73$

Sol 11.

In $\mathrm{BF}_{3}, \mathrm{~B}$ is $\mathrm{sp}^{2}$ - hybridized; in $\mathrm{NH}_{3}, \mathrm{~N}$ is $\mathrm{sp}^{3}$ - hybridized

## Sol 12.


$4 \mathrm{FeCI}_{3}+3 \mathrm{~K}_{4}\left[\mathrm{Fe}(\mathrm{CN})_{6}\right] \rightarrow \mathrm{Fe}_{4}\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]_{3}+12 \mathrm{KCI}$
Prussain blue
Sol 13.
$\mathrm{CaO}+\mathrm{SiO}_{2} \rightarrow \mathrm{CaSiO}_{3}$ (slag)
Sol 14.
$\mathrm{N}_{2} \mathrm{H}_{5}{ }^{+}$contains a coordinate bond between N and H .


Sol 15.
$\mathrm{Na}_{2} \mathrm{O}_{2}, \mathrm{H}_{2} \mathrm{O}_{2}, \mathrm{BaO}_{2}$ contain peroxide linkages.

## Sol 16.

Argon is the most abundant inert gas in atmosphere.

## Sol 17.

The greenhouse effect is widely used to describe the trapping of exess heat by the rising concentration of carbon dioxide in the atmosphere The carbon dioxide strongly absorbs infrared and does not allow as much of it to escape into space.

## Sol 18.

Salts with smaller sized cations have more lattice energy.

## Sol 19.

When octahedral holes are occupied in a ccp arrangement, the coordination number is 6 , i.e., 6 nearest neighbors.

Sol 20.
20 volume $\mathrm{H}_{2} \mathrm{O}_{2}$ is a solution of $\mathrm{H}_{2} \mathrm{O}_{2}$, 1L of which gives 20 L of $\mathrm{O}_{2}$ at STP.
$2 \mathrm{H}_{2} \mathrm{O}_{2} \rightarrow 2 \mathrm{H}_{2} \mathrm{O}+\mathrm{O}_{2}$
2x 34g 22.4 at STP
22.4 L of $\mathrm{O}_{2}$ is obtained from 68 g of $\mathrm{H}_{2} \mathrm{O}_{2} 20 \mathrm{~L}$ of $\mathrm{O}_{2}$ will be obtained from $\frac{68}{22.4} \times 20=60.71 \mathrm{~g}$ thus 20 volume $\mathrm{H}_{2} \mathrm{O}_{2}$ contains 60.71 g of $\mathrm{H}_{2} \mathrm{O}_{2}$

Sol 21.
Pyrex glass is a mixture of sodium aluminum borosilicate.
Sol 22.
$\mathrm{SO}_{3}+\mathrm{H}_{2} \mathrm{O}(1) \rightarrow \mathrm{H}_{2} \mathrm{SO}_{4}$
$\mathrm{P}_{2} \mathrm{O}_{5}+\mathrm{H}_{2} \mathrm{O}(1) \rightarrow 2 \mathrm{HPO}_{3}$
$\mathrm{N}_{2} \mathrm{O}(\mathrm{g})+\mathrm{H}_{2} \mathrm{O}(1) \rightarrow \mathrm{H}_{2} \mathrm{~N}_{2} \mathrm{O}_{2}$ (hypontrous acid)
$\mathrm{B}_{2} \mathrm{O}_{3}+\mathrm{H}_{2} \mathrm{O}(1) \rightarrow 2 \mathrm{HBO}_{2}$
Sol 23.
$2 \mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}+\mathrm{AgBr} \rightarrow \mathrm{Na}\left[\mathrm{Ag}\left(\mathrm{S}_{2} \mathrm{O}_{3}\right)_{2}\right]+\mathrm{NaBr}$

Sol. 24
Fullerene is an allotrope of carbon.


## Sol. 25

$\left[\mathrm{Ni}(\mathrm{CN})_{4}\right]^{2-}$ is a square planer complex, it is diamagnetic.


Sol. 26
$\left[\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2}\right] \mathrm{CuLi}+\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{Br} \rightarrow\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}+\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{Cu}+\mathrm{LiBr}$

## Sol. 27

$\mathrm{NH}_{3}{ }^{+}$in anilinium ion is meta directing.

## Sol. 28

$\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CN}+\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{COO} \mathrm{CH}_{2} \mathrm{CH}_{3}+\mathrm{NH}_{3}$

## Sol. 29

Mol. wt. $2 \times$ VD $=2 \times 73=146$
Number of carbon atoms $=\frac{49.3}{12} \times \frac{146}{100}=6$
Number of hydrogen atoms $=\frac{6.84}{1} \times \frac{146}{100}=6$
Number of oxygen atoms $=\frac{100-(49.3+6.84)}{16} \times \frac{146}{100}=4$
Molecular formula of the compound is $\mathrm{C}_{6} \mathrm{H}_{10} \mathrm{O}_{4}$

Black phosphorous is the most thermodynamically stable allotropic form of phosphorus. The atoms are linked together in puckered sheets, like graphite. Because of these structural similarities black phosphorus is also flaky like graphite and possess other similar properties.


## PHYSICS

## Sol. 1

$[X]=\left[\epsilon_{0}\right][L]\left[\frac{V}{[T]}\right]$
$=\left[M^{-1} A^{2} L^{-3} T^{4}\right][L]\left[M L^{2} T^{-3} A^{-1}\right]$
$=[A]$
$=$ current

## Sol. 2

We know that $v=\sqrt{2 g h}$
$\therefore h=\frac{u^{2}}{2 g}=\frac{(29.4)^{2}}{2 \times 9.8}=44.1 \mathrm{~m}$
Again $h^{\prime}=u t+\frac{1}{2} g t^{2}$
As $h^{\prime}=0$
We get $0=29.4 t-\frac{1}{2} \times 9.8 \times t^{2}$
$\Rightarrow \mathrm{t}=65$

## Sol. 3

Using law of conservation of momemtum
$1 \times V_{g}=200 \times 10^{-3} \times 5$
$\Rightarrow V_{g}=\frac{1 m}{s}$

Sol. 4
Given $l_{z}=2 I_{d}$
Or $I_{d}=\frac{I_{Z}}{2}$
Also $l_{z}=M \frac{\left(l^{2}+l^{2}\right)}{12}$
$=\frac{M l^{2}}{6}$
$\Rightarrow I_{d}=\frac{M l^{2}}{12}$
Similarly $2 I_{m}=I_{2} \Rightarrow \mathrm{I}_{\mathrm{m}}=\frac{I_{2}}{2}=\frac{M l^{2}}{12}$
$\Rightarrow l_{m}=l_{a}$

## Sol. 5

A car running with uniform velocity has a net zero force acting on it.

## Sol. 6

From the law of conversation of angular momentum
$m v_{\max } r_{\text {min }}=m v_{\text {min }} \boldsymbol{T}_{\text {max }}$
i.e. $\frac{V_{\max }}{V_{\min }}=\frac{r_{\max }}{r_{\min }}$
$=\frac{a(1+e)}{a(1-e)}=\frac{1+e}{1-e}$

## Sol. 7

It is obvious from the relation
$V=\sqrt{2 g h}$
That v depends upon g and h.it also depends upon viscosity but not on density

## Sol. 8

Given $O R^{2}=l^{2}-\left(\frac{l}{2}\right)^{2}$
$=\left[l\left(1+\alpha_{2} t\right)\right]^{2}-\left[\frac{1}{2}\left(1+\alpha_{1} t\right)\right]^{2}$
Expanding and neglecting terms containing squares and higher powers, we get $\alpha_{1}=4 \alpha_{2}$

Sol. 9
Average kinetic energy of a molecule is given by $K \cdot E \cdot a v=\frac{1}{2} m v_{r m s^{2}}=\frac{1}{2} m\left(\frac{3 R T}{m}\right)$
$=\frac{3}{4} m\left(\frac{2 R T}{m}\right)$
$=\frac{3}{4} m v_{p}^{2}$ as $v_{p}=\sqrt{\frac{2 R T}{m}}$
Sol. 10
When bob passes through the mean positive, tension in the string is maximum
i.e. $T_{\max }=\frac{m v_{\max }^{2}}{1} m g$
$\operatorname{as} v_{\max }=\omega A$
$\therefore T_{\text {max }}=\frac{m(\omega A)^{2}}{l}+m g$
Now $\omega=\sqrt{g / l}$
$\therefore T_{\max }=\frac{m\left[\left(\frac{g}{l}\right) A\right]^{2}}{l}+m g$
$=m g+m \frac{A^{2}}{l^{2}} g=m g\left[1+\left(\frac{A}{l}\right)^{2}\right]$

## Sol. 11

Amplitude of the vibration $=1 \theta$ and $x=A \cos \omega t$
Where $\omega=\sqrt{\frac{g}{l}}$
$\therefore x=l \theta \cos \sqrt{\frac{g}{l}} t$
Ans is (1)
Sol. 12
Given $\mathrm{R}^{3}=1000 \mathrm{r}^{3}$
$\Rightarrow \mathrm{R}=10 \mathrm{r}$
Capacitance of large drop $=\frac{1000 q}{R}=\frac{1000 q}{10 r} 100 C$

Sol. 13
Volume of cylindrical wire
$V=\pi r^{2} l$
New volume, $V^{\prime}=\left(\pi r^{\prime}\right)^{2}(2 l)$
As $V=V^{\prime}$
$\pi r^{\prime 2} 2 l=\pi r^{2} l$
$r^{\prime 2}=r^{2} / 2$
Also Resistance, $\mathrm{R}=\rho \frac{l}{a}=\rho \frac{1}{\pi r^{2}}$
New Resistance, $\mathrm{R}^{\prime}=\rho \frac{21}{\pi\left(\frac{r^{2}}{2}\right)}=4 R$
$\therefore$ change in resistance $=R^{\prime}-R=4 R-R=3 R$
$\%$ change $=\frac{3 R}{R} \times 100=300 \%$

## Sol. 14

The mass m is reduced to half i.e $\mathrm{m} / 2$ for a half needle and length is reduced to $\mathrm{l} / 2$.
$T=2 \pi \sqrt{\frac{l}{M B}}$
And $T^{\prime}=2 \pi \sqrt{\frac{l^{\prime}}{M^{\prime} B}}=2 \pi \sqrt{\frac{l^{\prime}}{M^{\prime} B}}$
Or $\frac{r^{\prime}}{r}=\sqrt{\frac{l^{\prime}}{l} \times \frac{M}{M^{\prime}}}$ Moment of Inertia of thin needle is
$l=\frac{m}{12} \times l^{2} \Rightarrow l^{\prime}=\frac{m}{2 \times 12} \times\left(\frac{l}{12}\right)^{2}$
$\Rightarrow \frac{l^{\prime}}{l}=\frac{1}{8}$
Sol. 15
Ratio of magnetic moments of unbroken needle and a piece is $\frac{M^{\prime}}{M}=\frac{1}{2}$

Ans is (2)

## Sol. 16

$d q=I d t=I_{0}\left(1-e^{-t / T}\right)$
$=\frac{E}{R}\left(1-e^{-t / T}\right)$
$\therefore q=\int_{0}^{T} \frac{E}{R}\left(1-e^{-t / T}\right) d t=\frac{E}{R}\left[t+T e^{-t / T}\right]_{0}^{T}$
$=\frac{E}{R}\left[T+\frac{T}{e}-T\right]=\frac{E}{R} \cdot \frac{T}{e}$
Sol. 17
Bothe the statements are self-explanatory
Sol. 18
Using $\mathrm{E}=\mathrm{h} v$
$1.6 \times 10^{-19} \times 14.4=6.6 \times 10^{-34} \times \mathrm{v}$
$\Rightarrow v=\frac{14.4 \times 1.6 \times 10^{-19}}{6.6 \times 10^{-34}}=3.49 \times 10^{15} \mathrm{HZ}$
Which falls in UV Range

## Sol. 19

Focal length as well as aperture has to be increased to increase both resolving power and magnifying power of a telescope

## So. 20

H Polaroid is prepared by stretching polyvinyl alcohol and then impregnating with iodine

## Sol. 21

Energy rate of incident photon $=$ nhv
Energy rate of reflected photon $=$ nhv
The rate of change of momentum after reflection $=\frac{2 n h v}{c}$
$\Rightarrow$ Force exerted $=\frac{2 n h v}{c}$

## Sol. 22

Refractive index, $0=\frac{\sin (A+\delta m)}{\sin (A / 2)}$
i.e. $\sqrt{3}=\frac{\sin \left(\frac{A+\delta m}{2}\right)}{\sin (60 / 2)}=\frac{\sin (A+\delta m)}{\sin 30}$
$\therefore \sin \frac{(A+\delta m)}{2}=\sqrt{3} \sin 30=\sqrt{3} \times \frac{1}{2}$
$\Rightarrow \frac{A+\delta m}{2}=60^{0} \Rightarrow \mathrm{~A}+\delta_{\mathrm{m}}=120^{\circ}$
Or $60+\delta_{\mathrm{m}}=120^{0}$
$\Rightarrow \delta_{\mathrm{m}}=60^{0}$

## Sol. 23

From the relation $p=\sqrt{2} \mathrm{mE}$
$\frac{P_{\alpha}}{P_{p}}=\sqrt{\frac{2 M_{\alpha} E_{\alpha}}{2 M_{p} E_{p}}}$
$=\sqrt{\frac{2 \times 4 M_{p} \times E_{\alpha}}{2 \times M_{p} \times 16 E_{\alpha}}}=\frac{1}{2}$
But $\frac{\lambda_{p}}{\lambda_{\alpha}}=\frac{P_{\alpha}}{P_{p}} \Rightarrow \frac{\lambda_{p}}{\lambda_{\alpha}}=\frac{1}{2}$

## Sol 24.

We have $\mathrm{N}=\frac{N_{0}}{16}$ and $\mathrm{T}=10$ ? s
$\operatorname{using} \frac{N}{N_{0}}=\left(\frac{1}{2}\right)^{t / T}$
$\left(\frac{1}{2}\right)^{4}=\left(\frac{1}{2}\right)^{t / T} \Rightarrow \frac{t}{T}=4$
Or $t=4 T=4 x 100=400$ ? $s$

## Sol 25.

Whenever a transistor is used In a circuit, the emitter base junction is always forward biased and base collective junction is reverse biased.

Sol 26.

Minimum of three geo synchronous satellites are required to communicate over the whole of earth.

Sol 27.
As $\bar{E}=E . \hat{\imath}$ and $\vec{B}=B \hat{k}$
Velocity of the particle will be along $\mathrm{q} . \vec{E}$ direction
$\Rightarrow \vec{V}=A q E \hat{\imath}$
Magnetic force on the particle will be

$$
\vec{F}=q(\vec{V} \times \vec{B})=q(A q E \hat{\imath}) x(B \hat{k})
$$

$=\mathrm{q}^{2}$ AEB $(\hat{\imath} \times \hat{k})$
$=\mathrm{q}^{2}$ AEB $(-\hat{\jmath})$
As Magnetic force is along negative $y$ - axis, whatever is the sign of $q$. All ions will be deflected towards negative $y$ - direction.

## Sol 28.

In circular orbit of a satellite
Potential Energy $=-2 x$ Kinetic energy
$=-2 \times \frac{1}{2} m v^{2}=-m v^{2}$
The total mechanical energy should be zero for escape from the gravitational pull which implies that kinetic energy should be $+\mathrm{mv}^{2}$

Sol 29.
Let $x$ be the maximum extension of the spring. From conservation of mechanical energy decrease in gravitational potential $=$ increaseinclastic potential energy.
$\Rightarrow M g x=\frac{1}{2} K x^{2}$
or $x=\frac{2 M g}{K}$
Sol 30.

$$
V_{c m}=\frac{m_{1} v_{1}+m_{2} v_{2}}{m_{1}+m_{2}}=\frac{10 \times 14+4 \times 0}{10+4}=\frac{140}{14}
$$

$=10 \mathrm{~m} / \mathrm{s}$.

## MATHEMATICS

Sol 1.

$78=50-(x+y+5)+30-(y+z+5)+20-(x+x+5)+(x+y+z)+5$
$\Rightarrow 78=100-(\mathrm{x}+\mathrm{y}+\mathrm{z})-10$
Hence required answer $=12+5=17$

## Sol 2.

We know that the range of $\sin x$ is $[-1,1]$. Here [ ] refers to greatest integer function, so, the outcomes will only be the integers ranging in $[-1,1]$ which are $[-1,0,1]$

## Sol 3.

Put $\mathrm{z}=\mathrm{xiy}$ in given equality it reduces to $\mathrm{x}^{2}+\mathrm{y}^{2}=1$ which is equation of a circle.
Sol 4.
Since one root is zero, product of roots is also zero, therefore $c=0$
Only one root is zero, so sum of roots is never zero, therefore $b \neq 0$

## Sol 5.

As $\alpha+\beta=4$
Or
$\alpha^{3}+\beta^{2}=(\alpha+\beta)^{3}-3 \alpha ß(\alpha+\beta)=44$
$\Rightarrow 64-3 \mathrm{ab}(4)=44$
$\Rightarrow 12 \alpha ß=20 \Rightarrow \alpha ß=\frac{5}{3} \Rightarrow$ product of roots $=\frac{5}{3}$
$\therefore$ equation is $\mathrm{x}^{2}-4 \mathrm{x}+\frac{5}{3}=0$

## Sol 6.

Applying the transformations
$R 3=(R 1+R 2)-R 3$, we get

$$
\left|\begin{array}{ccc}
a & a+b & a+b+c \\
3 a & 4 a+3 b & 5 a+4 b+3 c \\
2 a & 4 a+2 b & 5 a+4 b+2 c
\end{array}\right|
$$

$B Y R 2=R 2-R 3$

$$
\left|\begin{array}{ccc}
a & a+b & a+b+c \\
a & b & 5 a+4 b+3 c \\
2 a & 4 a+2 b & 5 a+4 b+2 c
\end{array}\right|
$$

Applying R3 = R3-(R1 + R2),

$$
\left|\begin{array}{ccc}
a & a+b & a+b+c \\
a & b & c \\
0 & 3 b & 4 \alpha+3 b
\end{array}\right|
$$

Applying transformation R1 = R1-R2

$$
\left|\begin{array}{ccc}
0 & a & a+b \\
a & b & c \\
0 & 3 b & 4 a+3 b
\end{array}\right|
$$

Expanding with respect to $\mathrm{A}_{21}$, we get
$-a(a(4 a+3 b)-3 b(a+b))=-a^{3}$
We know that $\mathrm{a}=\mathrm{i}$, hence, $\mathrm{i}^{\mathrm{e}}=\mathrm{i}$

## Sol 7.

The number of ways of painting six different faces is $6!$

## Sol 8.

Put $\mathrm{n}=1,2$
${ }^{1} \mathrm{C}_{0}-1 / 2{ }^{1} \mathrm{C}_{1}=1-\frac{1}{2}=1 / 2$

For $\mathrm{n}=2$, we get
${ }^{2} \mathrm{C}_{0}-1 / 2{ }^{2} \mathrm{C}_{1}+{ }^{2} \mathrm{C}_{3}=1-1$ T $1 / 3=1 /$
Only option (3) satisfies the above results.

Sol 10.
$\frac{3+57+\ldots n(\text { terms })}{5+8+11+\ldots .10 \text { terms }}=7$
$\Rightarrow \frac{\frac{n}{2}[6+(n-1) 2]}{\frac{10}{2}[10+(10-1) 3]}=7$
$\Rightarrow \frac{n[n+2]}{5[37]}=7 \Rightarrow \mathrm{n}^{2}+2 \mathrm{n}=35 \times 37$
$\Rightarrow \mathrm{n}^{2}+2 \mathrm{n}-35 \mathrm{x} 37=0 \Rightarrow(\mathrm{n}+37)(\mathrm{n}-35)=0 \Rightarrow \mathrm{n}=35$

## Sol 13.

On applying the L' Hospital rule, we get $\mathrm{Lt}_{\mathrm{x} \rightarrow 0} \sin \mathrm{x}=0$

## Sol 14.

$\operatorname{Rf}^{\prime}(0)=\lim _{\mathrm{h} \rightarrow 0} \frac{r(0+h)-f(0)}{h}=\lim _{h \rightarrow 0} \frac{h \frac{3}{2}-0}{h}$
$=\lim _{h \rightarrow 0} \mathrm{~h}^{1 / 2}=0$
$\operatorname{Lf}^{\prime}(0)=\lim _{h \rightarrow 0} \frac{f^{\prime}(o-h)-f(0)}{-h}$
$=\lim _{h \rightarrow 0} \frac{(h)^{\frac{3}{2}}-0}{(-h)}$
$=\lim _{h \rightarrow 0}(h)^{\frac{1}{2}}=0$
Now lf ${ }^{\prime}(0)=R f^{\prime}(0) \Rightarrow f^{\prime}(0)=0$
Sol 15.
We know that $\mathrm{y}=4 \mathrm{x}-5$ is tangent is $\mathrm{Y}^{2}=\mathrm{px}^{3}+\mathrm{q}$, hence slope of tangent is

$$
\frac{d y}{d x}=\frac{3 p x^{2}}{2 y}
$$

$\left(\frac{d y}{d x}\right)_{(2,3)}=\frac{12 p}{6}$
Slope of tangent $=2 \mathrm{p}$
Slope of given tangent $y=4 x-5$ is equal to 4 Hence $p=2$

Sol 16.

$$
I=\int \sqrt{2 \cos ^{2}\left(\frac{x}{8}\right)} d x
$$

$=\sqrt{2} \int \cos (x / 8) d x=\sqrt{2} \frac{\sin (x / 8)}{1 / 8}+c$
$=8 \sqrt{2} \sin (x / 8)+c$

## Sol 17.

$$
I=\int 1 \cdot \log x d x
$$

$=(\log \mathrm{x}) \mathrm{x}-\int \frac{1}{x} \cdot x d x+c$
$=\mathrm{x} \log \mathrm{x}-\mathrm{x}+\mathrm{c}$
$=\mathrm{x}(\log \mathrm{x}-1)+\mathrm{c}$

## Sol 18.

$$
\begin{gathered}
I=\int_{0}^{\pi} \sqrt{2 \sin ^{2}\left(\frac{x}{2}\right) d x} \\
=\sqrt{2} \int_{0}^{\pi} \sin \left(\frac{x}{2}\right) d x=\sqrt{2}\left[\frac{-\cos \left(\frac{x}{2}\right)}{\left(\frac{1}{2}\right)}\right]_{0}^{\pi} \\
=\sqrt{2}\left[-\cos \frac{\pi}{2}+\cos 0\right]=2 \sqrt{2}
\end{gathered}
$$

## Sol 19.

The order of differential equation $=$ number of arbitrary constants $=2$
Sol 20.

$$
\frac{d y}{d x}+\frac{1}{y \sqrt{1-x^{2}}}=0
$$

$y d y+\frac{d x}{\sqrt{1-x^{2}}}=0$
Integrating

$$
\frac{y^{2}}{2}+\sin ^{-1} x=c
$$

$y^{2}+2 \sin ^{-1} x=c$

## Sol 21.

Given vertices are of a right angled triangle and the orthocenter of a right angled triangle lies on the intersection of perpendicular. i.e. $(0,0)$

## Sol 22.

If denominator of x is less than denominator of y , then it can be started as a vertical ellipse.
The ellipse $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1$ is a vertical ellipse if $\mathrm{a}^{2}<\mathrm{b}^{2}$

## Sol 23.

We can simply check $b$ the options as no two lines are perpendicular to each other hence it must be either rhombus or parallelogram, now we can check the slopes of diagonals as, the diagonals are also not perpendicular, hence it is a parallelogram.

Sol 25.
Repaired probability $=\left(1-\frac{1}{4}\right)\left(1-\frac{1}{3}\right)=1 / 2$
Sol 28.
Points of intersection of curves $\mathrm{y}^{2}=2 \mathrm{x}+1$ andX $-\mathrm{y}=1$ are given by
$(x-1)^{2}=x+1$
$x^{2}-2 z+1=2 x+1$
$x^{2}-4 x=0 \Rightarrow x=0, x=4 \Rightarrow y=-1, y=3$
$\therefore(0,1)$ and $(4,3)$ are points of intersection Limits are
$\frac{y^{2}-1}{2} \leq x \leq y+1,1 \leq y \leq 3$
Required area $=\int_{-1}^{3} \int_{\frac{y^{2}-1}{2}}^{y+1} d x d y=\int_{-1}^{3}\left[(y+1)-\left(\frac{y^{2}-1}{2}\right)\right] d y$

$=\frac{1}{2} \int_{-1}^{3}\left(2 y-y^{2}+2\right) d y=\frac{1}{2}\left[y^{2}-\frac{y^{3}}{3}+3 y\right]_{-1}^{3}$
$=\frac{1}{2}\left[(9-9+9)-\left(1+\frac{1}{3}-3\right)\right]=\frac{16}{3}$
Sol 30.
$1+\log _{e} z+\frac{\left(\log _{e} z\right)^{2}}{2!}+\frac{\left(\log _{e} z\right)^{3}}{3!}+\ldots \ldots=e^{\log _{e} z}\left[\because 1+x+\frac{x^{2}}{2!}+\frac{x^{3}}{3!}\right]+\ldots \ldots \ldots=e^{x}$
$=\mathrm{z}$

