

Total No. of Questions : 58 ]

Code No. : 81-E

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## Subject : MATHEMATICS

( ఇంగ్లిలటో భాష్షంతర / English Version )

దినృంళ : 20. 06. 2011 ]

జురృృథధధ అంళగళః : 100 ]
[ Date: 20. 06. 2011
[ Time : 10-30 A.M. to 1-45 P.M.
[ Max. Marks : 100

FOR OFFICE USE ONLY

| $\begin{gathered} \mathbf{Q} . \\ \text { No. } \end{gathered}$ | Marks | $\underset{\sim}{\mathbf{~ N o}}$ | Marks | $\begin{gathered} \mathbf{Q} . \\ \text { No. } \end{gathered}$ | Marks | $\begin{gathered} \mathbf{Q} . \\ \text { No. } \end{gathered}$ | Marks | $\begin{aligned} & \text { Q. } \\ & \text { No. } \end{aligned}$ | Marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. |  | 14. |  | 27. |  | 40. |  | 53. |  |
| 2. |  | 15. |  | 28. |  | 41. |  | 54. |  |
| 3. |  | 16. |  | 29. |  | 42. |  | 55. |  |
| 4. |  | 17. |  | 30. |  | 43. |  | 56. |  |
| 5. |  | 18. |  | 31. |  | 44. |  | 57. |  |
| 6. |  | 19. |  | 32. |  | 45. |  | 58. |  |
| 7. |  | 20. |  | 33. |  | 46. |  | $\times$ |  |
| 8. |  | 21. |  | 34. |  | 47. |  | $\times$ |  |
| 9. |  | 22. |  | 35. |  | 48. |  | $\times$ |  |
| 10. |  | 23. |  | 36. |  | 49. |  | $\times$ |  |
| 11. |  | 24. |  | 37. |  | 50. |  | $\times$ |  |
| 12. |  | 25. |  | 38. |  | 51. |  | $\times$ |  |
| 13. |  | 26. |  | 39. |  | 52. |  | $\times$ |  |
| Total Marks |  |  |  |  |  |  |  |  |  |
|  | al Marks <br> words |  |  |  |  |  |  | Total |  |
| 1. $\checkmark$ |  |  |  |  | $\checkmark$ |  |  | $\checkmark$ |  |
| 2. $\checkmark$ |  |  |  |  |  |  |  |  |  |
| Signature of Evaluators |  |  | Registration No. |  | Signature of the Deputy Chief |  |  | Signature of the Room Invigilator |  |

General Instructions :
i) The Question-cum-Answer Booklet consists of objective and subjective types of questions having 58 questions.
ii) Space has been provided against each objective type question. You have to choose the correct choice and write the complete answer along with its alphabet in the space provided.
iii) For subjective type questions enough space for each question has been provided. You have to answer the questions in the space.
iv) Follow the instructions given against both the objective and subjective types of questions.
v) Candidate should not write the answer with pencil. Answers written in pencil will not be evaluated. ( Except Graphs, Diagrams \& Maps )
vi) In case of Multiple Choice, Fill in the blanks and Matching questions, scratching / rewriting / marking is not permitted, thereby rendering to disqualification for evaluation.
vii) Candidates have extra 15 minutes for reading the question paper.
viii) Space for Rough Work has been printed and provided at the bottom of each page.
I. Four alternatives are given for each of the following questions / incomplete statements. Only one of them is correct or most appropriate. Choose the correct alternative and write the complete answer along with its alphabet in the space provided against each question.

1. The law which is symbolically stated as $(A \cup B) \cup C=C \cup(A \cup B)$ is
(A) Commutative law
(B) Associative law
(C) Distributive law
(D) De Morgan's law.

Ans. : $\qquad$
2. In a Geometric Progression, if $T_{5}: T_{2}=8: 1$, then the common ratio is
(A) 12
(B) 8
(C) 3
(D) 2 .

Ans. : $\qquad$
3. The Geometric Mean of two numbers is $4 \sqrt{3}$ and Harmonic Mean is 6. Its Arithmetic Mean is
(A) 6
(B) 8
(C) 10
(D) 12 .

Ans. : $\qquad$
4. If $A-B=\left[\begin{array}{ll}3 & 4 \\ 5 & 6\end{array}\right]$ and $B=\left[\begin{array}{ll}0 & 2 \\ 2 & 0\end{array}\right]$ then matrix $A$ is
(A) $\left[\begin{array}{ll}3 & 6 \\ 7 & 6\end{array}\right]$
(B) $\left[\begin{array}{ll}0 & 2 \\ 2 & 0\end{array}\right]$
(C) $\left[\begin{array}{ll}3 & 4 \\ 5 & 6\end{array}\right]$
(D) $\left[\begin{array}{ll}3 & 2 \\ 3 & 6\end{array}\right]$.

Ans. $\qquad$
5. The product of H.C.F. and L.C.M. of two expressions is $6 a^{3} b^{4} c^{2}$. If one expression is $2 a^{3} b^{3} c^{2}$, then the other is
(A) $3 a b c$
(B) $6 b c$
(C) $3 b c$
(D) $3 b$.

Ans. : $\qquad$
6. L.C.M. of $(\sqrt{x}-\sqrt{y})$ and $(x-y)$ is
(A) $\sqrt{x}+\sqrt{y}$
(B) $\sqrt{x}-\sqrt{y}$
(C) $x-y$
(D) $x+y$.

Ans. : $\qquad$
7. The expression $\left(x^{2}+y^{2}+z^{2}-x-y-z\right)$ written using $\sum$ notation is
(A) $\quad \sum\left(x^{2}+x\right)$
(B) $\sum_{x y z} x-x^{2}$
(C) $\quad \sum x^{2}+\sum x$
(D) $\sum\left(x^{2}-x\right)$.
$x y z \quad x y z$
$x y z$

Ans. : $\qquad$
8. If $a+b+c=0$ then the value of $a^{2}+b^{2}-c^{2}$ is
(A) $a b$
(B) $-2 a b$
(C) $2 a b$
(D) $b c$.

Ans. : $\qquad$
9. The rationalising factor of $2 \sqrt[3]{x}$ is
(A) $\sqrt{x}$
(B) $4 \sqrt{x}$
(C) $\sqrt[3]{x^{2}}$
(D) $\sqrt[3]{x}$

Ans. : $\qquad$
10. If $m$ and $n$ are the roots of the quadratic equation $x^{2}-6 x+2=0$, then the value of $(m+n)^{2}$ is
(A) 36
(B) -36
(C) 2
(D) -2 .

Ans. : $\qquad$
11. In the equation $a x^{2}+b x+c=0$, if one root is negative of the other then
(A) $\quad a=0$
(B) $b=0$
(C) $c=0$
(D) $a=c$.

Ans. : $\qquad$
12. $x+\frac{1}{x}=3$ is in the form of
(A) adfected quadratic equation
(B) pure quadratic equation
(C) linear equation
(D) simple equation.

Ans. : $\qquad$
13. If $3 x^{2}-27=0$, then the value of $x^{2}$ is
(A) $\pm 3$
(B) +3
(C) -3
(D) 9 .

Ans. : $\qquad$
14. In the given figure chord $A B=$ chord $C D=8 \mathrm{~cm}$ and $O X=3 \mathrm{~cm}$. Radius $O C=$

(A) 8 cm
(B) 5 cm
(C) 4 cm
(D) 3 cm .

Ans. : $\qquad$
15. $\triangle A B C$ has sides of length $5 \mathrm{~cm}, 6 \mathrm{~cm}$ and 7 cm . The perimeter of $\triangle D E F$ is 360 cm . If $\triangle A B C \mid \| \triangle D E F$, then the ratio of the perimeters of $\triangle A B C$ and $\triangle D E F$ is
(A) $1: 2$
(B) $2: 1$
(C) $1: 20$
(D) $20: 1$.

Ans. : $\qquad$
16. In $\triangle A B C, D, E$ and $F$ are mid-points of $A B, B C$ and $C A$ respectively. If area of $\triangle A B C=60$ sq. cm then area of $\triangle D E F$ is
(A) 15 sq.cm
(B) $30 \mathrm{sq} . \mathrm{cm}$
(C) $45 \mathrm{sq} . \mathrm{cm}$
(D) $60 \mathrm{sq} . \mathrm{cm}$.

Ans. : $\qquad$
17. In the given figure $T P$ and $T Q$ are tangents drawn to the circle with centre $O$. If $\angle P T Q=40^{\circ}$, then $\angle O P Q$ is

(A) $40^{\circ}$
(B) $30^{\circ}$
(C) $20^{\circ}$
(D) $10^{\circ}$.

Ans. $\qquad$
18. In the given figure $A B, A C$ and $P Q$ are tangents to the circle with centre $O$. If the perimeter of $\triangle A P Q=20 \mathrm{~cm}$, then length of $A B$ is

(A) 10 cm
(B) 20 cm
(C) 15 cm
(D) 30 cm .

Ans. : $\qquad$
19. If surface areas of two spheres are in the ratio $25: 36$, then the ratio of their radii is
(A) $625: 1296$
(B) $7: 9$
(C) $6: 5$
(D) $5: 6$.

Ans. : $\qquad$
20. The area of the base of a circular cylinder is 154 sq.cm and height is 10 cm . Its volume is
(A) 144 c.c.
(B) 1540 c.c.
(C) 154 c.c
(D) $15 \cdot 4$ c.c.

Ans. : $\qquad$
II. Fill in the blanks with suitable answers :
$10 \times 1=10$
21. The reciprocals of the terms in Geometric Progression form $\qquad$ .

Ans. : $\qquad$
22. $A$ is a square matrix of order $2 \infty 2$. If $A=A^{\prime}$, then the matrix $A$ is called $\qquad$

Ans.: $\qquad$
23. The value of ${ }^{n} P_{0}$ is $\qquad$ .

Ans. : $\qquad$
24. The formula to find the coefficient of variation is $\qquad$ . .

Ans. : $\qquad$
25. When one algebraic expression is divided by the other, if the last remainder is a constant but not zero, then their H.C.F. is $\qquad$ . .

Ans. : $\qquad$
26. The summation of the terms is denoted by the symbol $\qquad$ . .

Ans. : $\qquad$
27. If two triangles are equiangular then their corresponding sides are $\qquad$ . .

Ans. : $\qquad$
28. The lengths of the tangents drawn to a circle from an external point are $\qquad$ .

Ans. : $\qquad$
29. The formula to find the volume of a sphere is $\qquad$

Ans. : $\qquad$
30. Shape of each face of a hexahedron is $\qquad$

Ans. : $\qquad$
( SPACE FOR ROUGH WORK )
III. 31. $A$ and $B$ are the subsets of the universal set $U$. Draw Venn diagrams to represent
(i) $(A-B)$
(ii) $(A \cup B)^{\prime}$.

2
32. $A=\{2,4,8\}, B=\{1,2,6,8\}$ and $C=\{1,5,6,8\}$ then show that $A-(B \cap C)=(A-B) \cup(A-C)$.
33. The first term of a G.P. is 50 and fourth term is 1350 . Find its fifth term.
34. If $a, H, b$ are in H.P., show that $H=\frac{2 a b}{a+b}$.
35. If $A=\left[\begin{array}{ll}1 & 2 \\ 3 & 4\end{array}\right]$, then find $A^{2}$.
36. If $5 .{ }^{n} P_{3}=4 .{ }^{n+1} P_{3}$, find $n$.
37. Rationalise the denominator and simplify.

$$
\frac{3}{\sqrt{3}-\sqrt{2}}
$$

38. Simplify : $8 \sqrt{\frac{1}{2}}-\frac{1}{2} \sqrt{8}$.
39. Solve for $x$ by using formula :

$$
x^{2}-2 x-2=0
$$

40. Solve for $x$ :

$$
2\left(x^{2}-1\right)=x(1-x) .
$$

41. The perimeter of a rectangle is 36 cm and its area is 80 square cm . Find its length and breadth.
42. Find the value of $k$ so that the equation $49 x^{2}-k x-81=0$, has one root as the negative of the other.
43. Find the values of
i) $\quad\left(3 \approx_{7} 6\right) \approx_{7} 4$
ii) $\quad\left(\begin{array}{lll}4 & f_{11} & 3\end{array}\right) f_{11} 7$.
44. In a circle of radius 3.5 cm , draw two radii such that the angle between them is $70^{\circ}$. Draw two tangents at the non-centre ends of the radii.
45. The radius of the base of a right circular cylinder is doubled and the height is halved. What is the ratio of volume of the new cylinder to that of the original cylinder?
46. Draw a plan of the field from the surveyor's field book given below :

Scale : $25 \mathrm{~m}=1 \mathrm{~cm}$.

|  | To D (in m ) |  |
| :---: | :---: | :---: |
|  | 300 |  |
| to E 50 | 200 | 100 to C |
|  | 150 | 75 to B |
|  | 100 |  |
|  | From A |  |

47. Write the two conditions of traversibility of a network.
48. Draw the graph for the given matrix :

$$
\left[\begin{array}{lll}
0 & 3 & 0 \\
3 & 0 & 2 \\
0 & 2 & 0
\end{array}\right]
$$

IV. 49. Raju is one among 15 boys. In how many ways can a cricket team of 11 be chosen ? How many of these contain Raju ? 3
50. Find the standard deviation of the following frequency distribution :

| C.I. : | $1-5$ | $6-10$ | $11-15$ | $16-20$ |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{f}:$ | 2 | 3 | 4 | 1 |

51. Find the L.C.M. of $\left(a^{3}-3 a^{2}-10 a+24\right)$ and $\left(a^{3}-2 a^{2}-9 a+18\right)$ by division method.
52. If $x y(x+y)=1$, show that $\frac{1}{x^{3} y^{3}}-x^{3}-y^{3}=3$.
53. Prove that the areas of similar triangles have the same ratio as the squares of corresponding altitudes.
54. Prove that if two circles touch each other externally, the point of contact and the centres of the circles are collinear. 3
V. 55. In an Arithmetic Progression the sum of first 10 terms is 175 and the sum of the next 10 terms is 475 . Find the Arithmetic Progression. 4
55. Construct a transverse common tangent to two circles of radii 3 cm and 2 cm , whose centres are 10 cm apart. Measure the length of the tangent. 4
56. Prove that in a right angled triangle, the square on the hypotenuse is equal to the sum of the squares on the other two sides. 4
57. Draw the graphs of $y=x^{2}$ and $y=2 x+3$ and hence solve the equation $x^{2}-2 x-3=0$.

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