## CLASS -IX

MAX MARKS: - 90
SUB: -MATHS (041)

MAX.TIME:-3 Hours

## General Instructions:-

1. All questions are compulsory.
2. The question paper consists of 31 questions divided into five sections $A, B, C, D$ and $E$.
3. (i) Section $A$ comprises of 4 questions of 1 marks each.
(ii)Section B comprises of 6 question of 2 marks each.
(iii) Section C comprises of 8 questions of 3 marks each.
(iv)Section D comprises of 10 questions of 4 marks each.
(v) Section E comprises of 3 questions one carrying 4 marks and two carrying 3 marks each (OTBA) 4. Use of calculator is not permitted.

## SECTION - A

1. If a triangle and a parallelogram are on the same base and between the sameparallels,thenwhat is the ratioof the area of the triangle to the area of the parallelogram?
2. In the figure, $O$ is the centre of the circle and $\angle A O B=80^{\circ}$. The value of $x$ is:

3. A coin is tossed 100 times and head appears 54 times. Then, find the probability of getting a tail.
4. Find the mode of the following marks (out of 10) obtained by 20students:

$$
4,6,5,9,3,2,7,7,6,5,4,9,10,10,3,4,7,6,9,9
$$

## SECTION - B

5. If the point $(3,5)$ lies on the graph of the equation $3 y=k x-6$, find the value of $k$.
6. Prove that equalchords of a circle subtend equal angles at the centre.
7. $A B C D$ is a parallelogram in which $A E \perp D C$ and $C F \perp A D$. If $A B=16 \mathrm{~cm}$, $A E=8 \mathrm{~cm}$ and $C F=10 \mathrm{~cm}$, find $A D$.

8. A bag contains 15 cards bearing numbers $1,2,3,--------14,15$. A card is drawn from the bag. Find the probability that it bears: (i) a prime number (ii) a number less than or equal to 15.
9. Find the mean salary of 20 workers of a factory from the following table:

| Salary (in Rs) | Number of workers |
| :---: | :---: |
| 10000 | 5 |
| 9000 | 8 |
| 8000 | 2 |
| 7000 | 2 |
| 6000 | 3 |
| total | 20 |

10. 1500 families with $\mathbf{2}$ children were selected randomly, and the following data were recorded:

| Number of girls in a family | 2 | 1 | 0 |
| :---: | :---: | :---: | :---: |
| Number of families | 475 | 814 | 211 |

Find the probability of a family, chosen at random, having: (i) $\mathbf{2}$ girls
(ii) no girl

SECTION - C
11. Give the geometric representations of $2 x+9=0$ as an equation(i) in one variable (ii) in two variables.
12. The linear equation that converts Fahrenheit (F) to Celsius (C) is given by the relation

$$
C=\frac{5 F-160}{9}
$$

(i) If the temperature is $35^{\circ} \mathrm{C}$, what is the temperature in Fahrenheit?
(ii) What is the numerical value of the temperature which is same in both the scales?
13. In the figure, $E$ is any point on median $A D$ of a $\triangle A B C$.


Show that ar $(\mathrm{ABE})=$ ar $(\mathrm{ACE})$.
14. The length, breadth and height of a room are $5 \mathrm{~m}, 4 \mathrm{~m}$ and 3 m respectively. Find the cost of white washing the walls of the room and the ceiling at the rate of Rs 7.50 per $\mathrm{m}^{2}$.
15. The slant height and base diameter of a conical tomb are 25 m and 14 m respectively. Find the cost of whitewashing its curved surfaceat the rate of Rs $\mathbf{2 1 0}$ per $\mathbf{1 0 0} \mathbf{m}^{2}$.
16. Construct a triangle $P Q R$ in which $Q R=\mathbf{7 c m}, \angle Q=75^{\circ}$ and $P Q+P R=13 \mathrm{~cm}$.
17. The heights of 50 students, measured to the nearest cm , have been found to be as follows:

| 161 | 150 | 154 | 165 | 168 | 161 | 154 | 162 | 150 | 151 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 162 | 164 | 171 | 165 | 158 | 154 | 156 | 172 | 160 | 170 |
| 153 | 159 | 161 | 170 | 162 | 165 | 166 | 168 | 165 | 164 |
| 154 | 152 | 153 | 156 | 158 | 162 | 160 | 161 | 173 | 166 |
| 161 | 159 | 162 | 167 | 168 | 159 | 158 | 153 | 154 | 159 |

(i)Represent the data given above by a grouped frequency distribution table, taking the class intervals as 160-165, 165-170, etc. (ii) What is the range height of the students?
18. Fifty seeds were selected at random from each of 5 bags of seeds, andwere kept under Standardized conditionsfavorable to germination. After 20 days, the number of seeds which had germinated in each collection were counted and recorded as follows:

| Bag | 1 | 2 | 3 | 4 | 5 |
| :---: | :--- | :--- | :--- | :--- | :--- |
| Number of seeds germinated | 40 | 48 | 42 | 39 | 41 |

What is the probability of germination of:(i) more than 40 seeds in a bag?
(ii) 49 seeds in a bag?
(iii) more than 35 seeds in a bag?

SECTION - D
19. The taxi fare in a city is as follows: For the first kilometre, the fare is Rs 10 and for the subsequent distanceit is Rs $\mathbf{8}$ per km. Taking the distance covered as $\mathbf{x k m}$ and total fare as Rs y , write a linear equation for this information, and draw its graph.
20. Draw the graph of linear equation $4 x+3 y=12$. At what point the graph of the equation cut the $x-$ axisand $y$-axis. If ( $3 m, m-1$ ) is a solution of given equation, find $m$.
21. Prove that the angle subtended by an arc at the centre is double the angle subtended by it at any pointonthe remaining part of the circle.
22. Construct a $\triangle A B C$ in which $\angle B=30^{\circ}, \angle C=90^{\circ}$ and $A B+B C+C A=12 \mathrm{~cm}$.
23. A village, having a population of 4000 , requires 150 litres of water per head per day. Due to lack of sourcesof water, they collect the water into a tank measuring $20 \mathrm{~m} \times 15 \mathrm{~m} \times 6 \mathrm{~m}$ from a river using a long pipe. (i) For how many days will the water of this tank last?
(ii) Which message is conveyed by the people of village?
24. The inner diameter of a cylindrical wooden pipe is 24 cm and its outer diameter is 28 cm . The length of the pipe is 35 cm . Find the mass of the pipe, if $1 \mathrm{~cm}^{3}$ of wood has a mass of 0.6 g .
25. Volume of a right circular cone is $9856 \mathrm{~cm}^{3}$. If diameter of the cone is $\mathbf{2 8} \mathbf{c m}$, find the curved surface area of the cone.
26. $D, E$ and $F$ are respectively the midpoints of the sides $B C, C A$ and $A B$ of a $\triangle A B C$. Show that (i) BDEF is a parallelogram.
(ii) $\operatorname{ar}$ (DEF) $=\frac{1}{4}$ ar (ABC)
27. If two equal chords of a circle intersect within the circle, prove that the segments of the one chord are equal to corresponding segment of the other chord
28. In a city, the weekly observations made in a study on the cost of livingindex are given in the following table\&Draw a frequency polygon for the given data.

| Cost of living index | Number of weeks |
| :---: | :---: |
| $140-150$ | 5 |
| $150-160$ | 10 |
| $160-170$ | 20 |
| $170-180$ | 9 |
| $180-190$ | 6 |
| $190-200$ | 2 |
| Total | 52 |

## SECTION - E (OTBA)

[Theme: Solving Mystery of messed up fields]
29. Listening to Jeevan's Statement, Roshni concluded that his farm might be any Quadrilateral in shape. Doyou agree with her opinion? Justify.
Prove that the quadrilateral formed by joining the mid-points of the sides of a quadrilateral, in order, is a parallelogram.
[4 marks]
30. Listening to Uttapa's Statement, Roshni concluded that his farm might be a Parallelogram in shape. Do you agree with her opinion? Justify. State any four properties of a Parallelogram. [3 marks]
31. Listening to Yousuf 's Statement, Roshni concluded that his farm might be a square in shape. Do you agree with her opinion? Justify. State any two properties of a square.[3 marks]

