## Notes of Online class

## Session 12

Let us think about a property of arithmetic sequence)

- Consider some arithmetic sequences.
$2,5,8,11$
$3,7,11,15,19,23$
$10,15,20,25,30,35,40,45$
All these sequences have even number of terms
We can make pairs by taking terms equidistant from both ends.
$(2,11),(5,8)$.Pair sum is 13 in both pairs.
Can you see this property in other sequences also

If an arithmetic sequence has even number of terms, the sum of the terms equidis tant from both ends are equal.
■If the arithmetic sequence contains odd number of terms there is a term which comes in the middle without pair. This middle term is half of the pair sum
Look at the sequences given below $2,5,8,11,14$
$3,7,11,15,19,23,27$
$10,15,20,25,30,35,40,45,50$
In the first squence, pair sum is $2+14=16$, middle term is half of 16 . It is 8 . Note that the number of terms $n=5$. So middle term is $\frac{5+1}{2}$ th term. That is 3rd term In the second squence, pair sum is $3+27=30$, middle term is half of 30 . It is 15. Note that the number of terms $n=7$. So middle term is $\frac{7+1}{2}$ th term. That is 4 rd term
In the third squence, pair sum is $10+50=60$, middle term is half of 60 . It is 30.Note that the number of terms $n=9$. So middle term is $\frac{9+1}{2}$ th term. That is 5 rd term

## Examples

1) 5 th term of an arithmetic sequence is 38
a) What is the sum of first and nineth terms?
b) What is the sum of second and eigthth terms?
c) If the first term is 10 then what is the common difference?
d) What is the nineth term of the sequence?

## Answer

a) $x_{1}+x_{9}=2 \times x_{5}=2 \times 38=76$

If the arithmetic sequence contains odd number of terms there is a term which comes in the middle without pair. This middle term is half of the pair sum
b) $x_{2}+x_{8}=2 \times x_{5}=2 \times 38=76$

If the arithmetic sequence contains odd number of terms there is a term which comes in the middle without pair. This middle term is half of the pair sum
c) $x_{5}-x_{1}=4 d, 38-10=4 d$
$4 d=28, d=7$
d) $x_{9}+x_{1}=76, x_{9}+10=76, x_{9}=66$
2) The sum of the 1 st and 15 th terms of an arithmetic sequence is 56 .
a) What is the 8 th term of the sequence?
b) What is the sum of second and 14 th terms of the sequence?
c) What is the sum of 7 th and 9 th terms of the sequence?
d) If the first term is 7 then what is the common difference?
e) Write the algebraic form of the sequence

## Answer

a) $x_{8}=\frac{56}{2}=28$
b) $x_{2}+x_{14}=56$
c) $x_{7}+x_{9}=56$
d) $x_{8}-x_{1}=7 d, 28-7=7 d$
$7 d=21, d=3$
e) $x_{n}=d n+(f-d)=3 n+(7-3)=3 n+4$
3) Algebraic form of an arithmetic sequence is $7 n+1$
a) What is the 10 th term of the sequence?
b) What is the sum of 1 st and 19 th terms of this sequence?
c) What is the sum of 9 th and 11 th terms of this sequence?

## Answer

a) $x_{10}=7 \times 10+1=71$
b) $x_{1}+x_{19}=2 \times x_{10}=2 \times 71=142$
c) 142
4) Choose the correct answer.

1) What is the algebraic form of the sequence $2,4,6,8 \cdots$
(a) $n$
(b) $n+2$
(c) $2 n$
(d) $2 n-1$
2) If the difference between 5 th term and 10 th term of an arithmetic sequence is 20 then what is the difference between 10 th term and 20 th term
(a) 10
(b) 20
(c) 30
(d) 40
3) What is the first term of the arithmetic sequence whose algebraic form is $4 n+5$
(a) 4
(b) 5
(c) 9
(d) 1
4) What is the tenth term of the sequence whose algebraic form is $-10 n+100$
(a) -1
(b) 5
(c) 0
(d) 1

## Answer

a) $2 n$

$$
x_{n}=d n+(f-d)=2 n+(2-2)=2 n+0=2 n
$$

b) 40

$$
5 d=20 . \text { So } 10 d=40
$$

c) 9

$$
f=4 \times 1+5=9
$$

d) 0

$$
x_{10}=-10 \times 10+100=-100+100=0
$$

