## PRE-BOARD EXAMINATION-1 (DECEMBER - 2019)

CLASS: IX
MATHEMATICS

Time: $\mathbf{3}$ hours
MAX. MARKS: 80

## General Instructions:

i) All questions are compulsory.
ii) The question paper consists of $\mathbf{4 0}$ questions divided into four sections $\mathbf{A}, \mathbf{B}, \mathbf{C}$, and $\mathbf{D}$.
iii) Section $\mathbf{A}$ comprises of 20questions of $\mathbf{1}$ mark each. Section $\mathbf{B}$ comprises of $\mathbf{6}$ questions of $\mathbf{2}$ marks each. Section $\mathbf{C}$ comprises of $\mathbf{8}$ questions of $\mathbf{3}$ marks each. Section D comprises of $\mathbf{6}$ questions of $\mathbf{4}$ marks each.
iv) Use of calculators is not permitted

## SECTION-A

## Multiple Choice Questions:

1 The value of n for which $\sqrt{n}$ be a rational number is
(a) 2
(b) 4
(c) 3
(d) 5

2 If m and n are two natural numbers and $m^{n}=32$, then $n^{m n}$ is
(a) $5^{2}$
(b) $5^{3}$
(c) $5^{10}$
(d) $5^{12}$

3 The curved surface area of a sphere is $616 \mathrm{~cm}^{2}$. Its radius is
(a) 7 cm
(b) 5 cm
(c) 6 cm
(d) 8 cm

4 If the coordinates of the two points P and Q are $(-2,3)$ and $(-3,5)$, then the value of [(abscissa of P$)-($ abscissa of Q$)]$ is
(a) -2
(b) 1
(c) -1
(d) -5

5 The radius of the circle is 5 cm and the distance of the chord from the centre of the circle is 4 cm then, the length of the chord is
(a) 8 cm
(b) 7 cm
(c) 6 cm
(d) 5 cm

6 If $P(E)=0.37$, then $P(\operatorname{not} E)$ will be
(a) 0.37
(b) 0.63
(c) 0.57
(d)none of these

7 Two parallelograms are on equal bases and between the same parallels. The ratio of their areas is
(a) $1: 2$
(b) $1: 1$
(c) $2: 1$
(d) $3: 1$
(a) $20^{\circ}$
(b) $25^{\circ}$
(c) $30^{\circ}$
(d) $50^{\circ}$

value of $x$ is
$9 \quad$ What is the $\frac{p}{q}$ form of the number $0 . \overline{3}$
(a) $\frac{1}{9}$
(b) $\frac{1}{3}$
(c) 9
(d) 3

10 In the figure if AOB is a diameter of the circle and $\mathrm{AC}=\mathrm{BC}$ then, $\angle \mathrm{CAB}$ is equal to
(a) $35^{\circ}$
(b) $60^{\circ}$
(c) $90^{\circ}$
(d) $45^{\circ}$


## Fill in the blanks :

11 The value of $(\sqrt{11}+\sqrt{7})(\sqrt{11}-\sqrt{7})$ is $\qquad$ .

12 If $a+b+c=0$, then the value of $a^{3}+b^{3}+c^{3}$ is $\qquad$

## OR

Degree of the polynomial $4 x^{4}+0 x^{3}+0 x^{5}+5 x+7$ is $\qquad$ .

13 The length of each side of an equilateral triangle having an area $9 \sqrt{3} \mathrm{~cm}^{2}$ is $\qquad$ -.

14 If $(2,0)$ is a solution of the linear equation $2 x+3 y=k$, then the value of $k$ is
$\qquad$ .

15 The sum of all the probabilities of an event is $\qquad$ ـ.

## Answer the following :

16 Find the value of $a$, if $x-2$ is a factor of $x^{3}-3 x+5 a$.

17 Angles of a triangle are in the ratio 2:4:3. Find he smallest angle of the triangle.

18 In the given figure, AD is the median. Find $\angle \mathrm{BAD}$.


OR
In $\triangle P Q R, \angle P=70^{\circ}$ and $\angle Q=30^{\circ}$. Which side of this triangle is the longest?

20 Express $\sqrt{3} y=2 x$ as linear equation in two variables in standard form.

## SECTION-B

21

Simplify $\left(\frac{64}{125}\right)^{\frac{-2}{3}}$

## OR

Represent $\sqrt{5}$ on the number line.
On one page of a telephone directory, there are 200 phone numbers. The frequency distribution of of their unit digits is given below:

| Unit digit | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 19 | 22 | 23 | 19 | 21 | 24 | 23 | 18 | 16 | 15 |

One of the numbers is chosen at random from the page.

What is the probability that the unit digit of the chosen number is
(i) 5
(ii) less than 3

In the given figure, find x .

(ii) the $y$-axis

Ten observations $6,14,15,17, x+1,2 x-13,30,32,34,43$ are written in ascending order. The median of the data is 24 . Find the value of $x$.

## OR

If the mean of the observations $x, 2 x+1,2 x+5,2 x+9$ is 30 , what is the mean of last two observations?

The base of an isosceles triangle is 12 cm and its perimeter is 32 cm . Find its area.

## SECTION-C

Find the values of a and b in $\frac{3-\sqrt{5}}{3+2 \sqrt{5}}=a \sqrt{5}-\frac{b}{11}$
Show that $2 x+1$ is a factor of the polynomial $2 x^{3}-11 x^{2}-4 x+1$.

29 Plot the points $(x, y)$ given by the following table.

| x | 2 | 4 | -4 | -2 | 6 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| y | 5 | -3 | 3 | 5 | -1 | 2 |

30 If a triangle and a parallelogram are on the same base and between the same parallels, then prove that the area of the triangle is equal to half the area of the parallelogram.

31 Construct a triangle whose sides are $3.6 \mathrm{~cm}, 3.0 \mathrm{~cm}$ and 4.8 cm . Bisect the smallest angle and measure each part.

OR
Draw a line segment $\mathrm{PQ}=8.4 \mathrm{~cm}$. Divide it into 4 equal parts, using ruler and compass.
32 In the given figure, AD is the bisector of $\angle B A C$ and $\angle C P D=\angle B P D$. Prove that $\triangle C A P \cong$ $\triangle B A P$ and $\mathrm{CP}=\mathrm{BP}$.


OR
In the figure below, ABCD is a square and P is the mid-point of $\mathrm{AD} . \mathrm{BP}$ and CP are joined.
Prove that $\angle P C B=\angle P B C$.


33 In the given figure AP and CQ are perpendiculars to the diagonal BD of a parallelogram $A B C D$. Prove that $A P=C Q$.


34 Find the quotient and the remainder when $x^{3}-3 x^{2}+4 x-5$ is divided by $x-2$.

## OR

Without finding the cubes, factorise $(2 r-3 s)^{3}+(3 s-5 t)^{3}+(5 t-2 r)^{3}$

## SECTION-D

35 Prove that the angle subtended by an arc at the centre is double the angle subtended by it at any point on the remaining part of the circle.

36 Construct a $\triangle X Y Z$ in which $\angle Y=40^{\circ}, \angle Z=30^{\circ}$ and $X Y+Y Z+Z X=10 \mathrm{~cm}$
OR
Construct a triangle $A B C$, in which $B C=7 \mathrm{~cm}, \angle B=75^{\circ}$ and $A B+A C=13 \mathrm{~cm}$.
37 Draw the graph of the linear equation $3 x+4 y=6$. At what points the graph cuts the $x$-axis and the $y$-axis.

38 A solid cylinder has total surface area of $462 \mathrm{~cm}^{2}$. Its curved surface area is one third of its total surface area. Find the volume of the cylinder.

OR
The radius and height of a cone are in the ratio $3: 4$ and its volume is $301.44 \mathrm{~cm}^{3}$. Find the radius and slant height of the cone.

39 The lengths of the sides of a triangle are $7 \mathrm{~cm}, 13 \mathrm{~cm}$ and 12 cm . Find the length of perpendicular from the opposite vertex to the side whose length is 12 cm .

## OR

A floral design on a floor is made up of 16 tiles which are triangular, the sides of a triangle being $9 \mathrm{~cm}, 28 \mathrm{~cm}$, and 35 cm . Find the cost of polishing the tiles at the rate of 50 paise per $\mathrm{cm}^{2} .(\sqrt{6}=2.45)$

40 Draw a histogram and frequency polygon for the following data.

| Age (in years) | No. or persons |
| :---: | :---: |
| $0-4$ | 3 |
| $4-8$ | 6 |
| $8-12$ | 8 |
| $12-16$ | 10 |
| $16-20$ | 8 |
| $20-24$ | 5 |
| $24-28$ | 3 |

